

# Gravitational wave signals of DM freeze-out

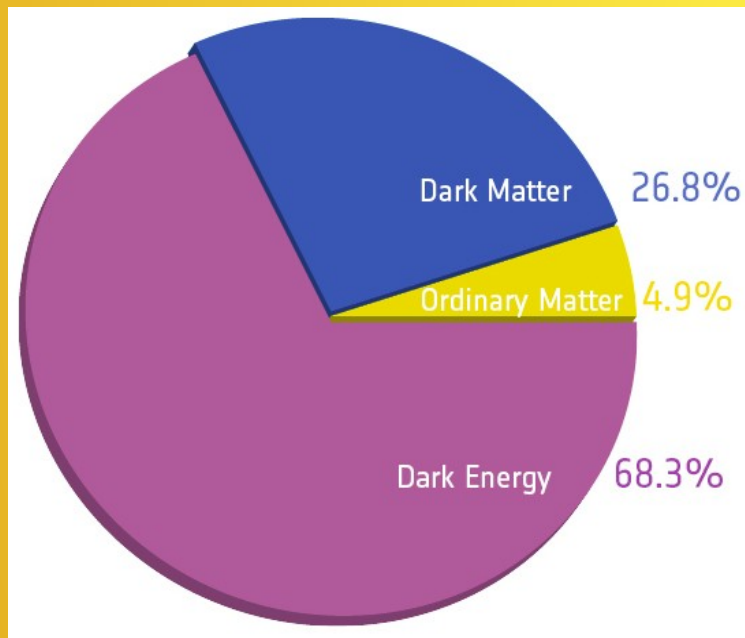
**Po-Yan Tseng (NTHU)**  
**Danny Marfatia (U. of Hawaii)**

**Reference: JHEP02(2021)022 (arXiv:2006.07313)**

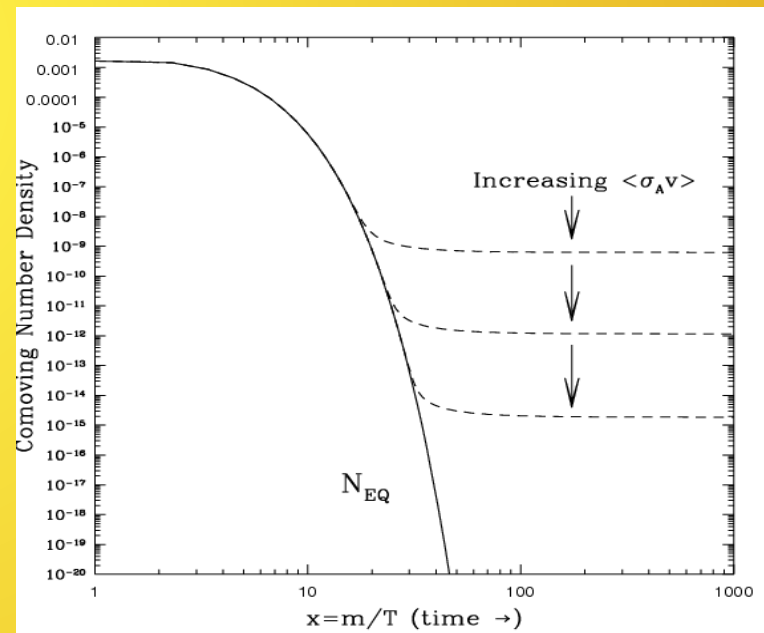
**Asia-Pacific Workshop on Particle Physics and Cosmology**  
**2021, Aug. 2<sup>nd</sup> - Aug. 6<sup>th</sup>**

# Introduction

- DM production: **Thermal freeze-out** mechanism.
- Weakly interacting massive DM (**WIMP**), gives the correct relic density.



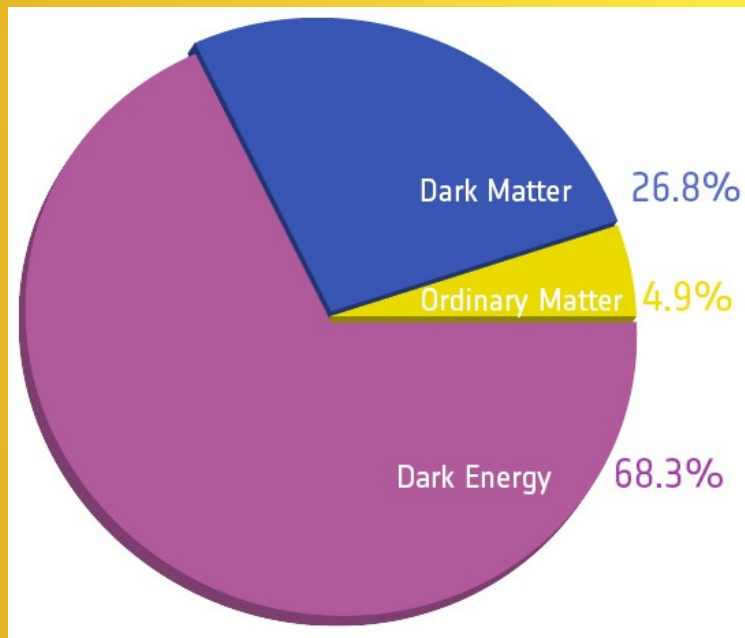
Planck collaboration



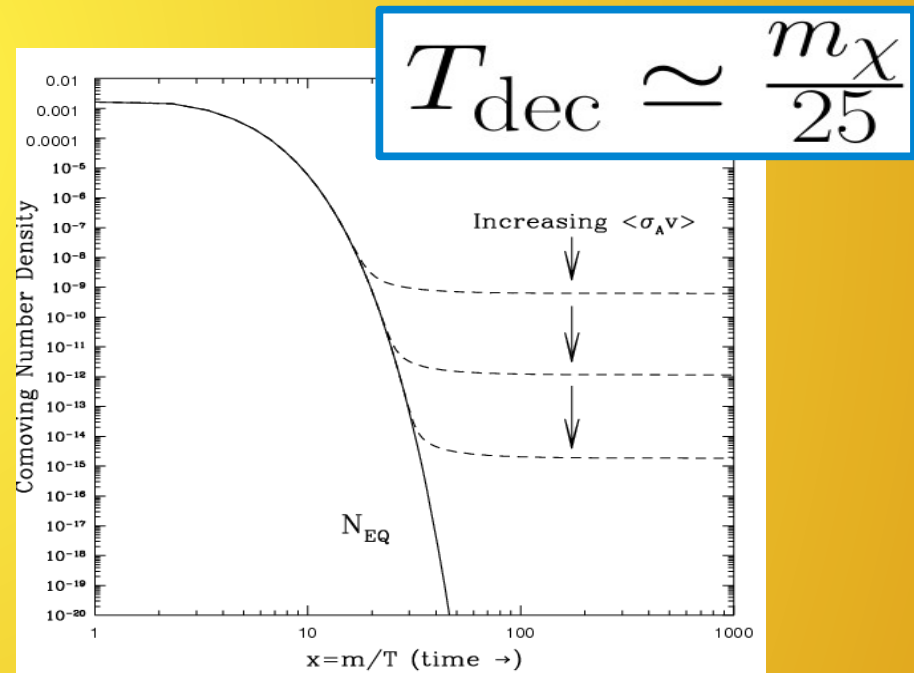
Dan Hooper: 0901.4090

# Introduction

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- Weakly interacting massive DM (**WIMP**), gives the correct relic density.



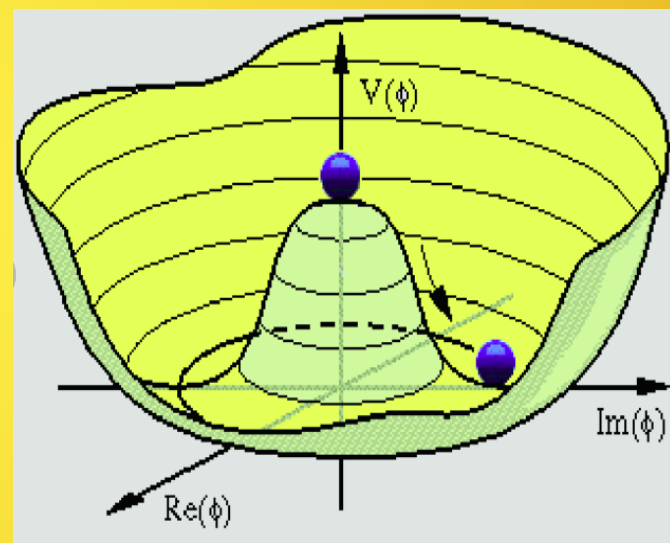
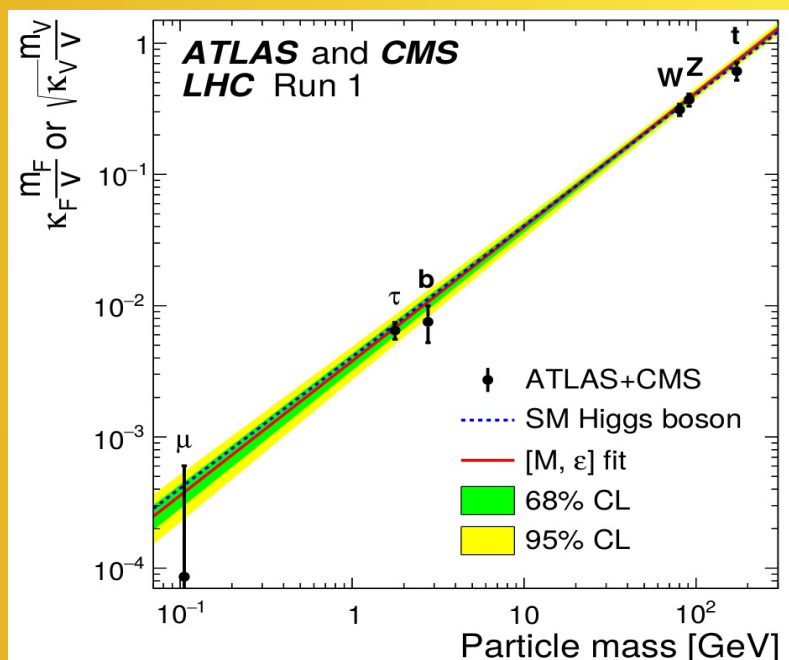
Planck collaboration



Dan Hooper: 0901.4090

# Introduction

- 125 GeV Higgs gives the mass to the SM particles through **spontaneous symmetry breaking**.



Dezso Horvath: Higgs and BSM studies at the LHC

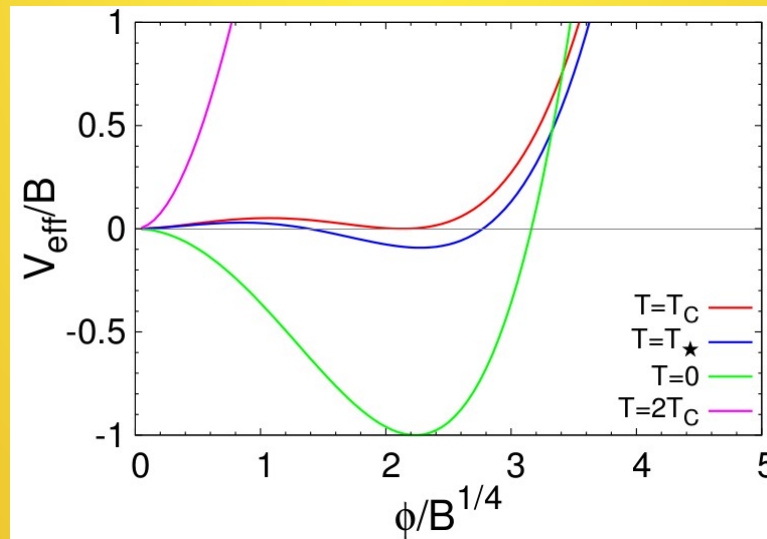
# Introduction

- ♦ The origin of DM mass may come from the **spontaneous symmetry breaking** inducing by another scalar.

$$\mathcal{L} \supset \bar{\chi} i \not{\partial} \chi - g_{\chi} \phi \bar{\chi} \chi - V_{\text{eff}}(\phi, T)$$

$$m_{\chi} \simeq g_{\chi} \langle \phi \rangle$$

- ♦ We consider **1<sup>st</sup> order phase transition (FOPT)**.

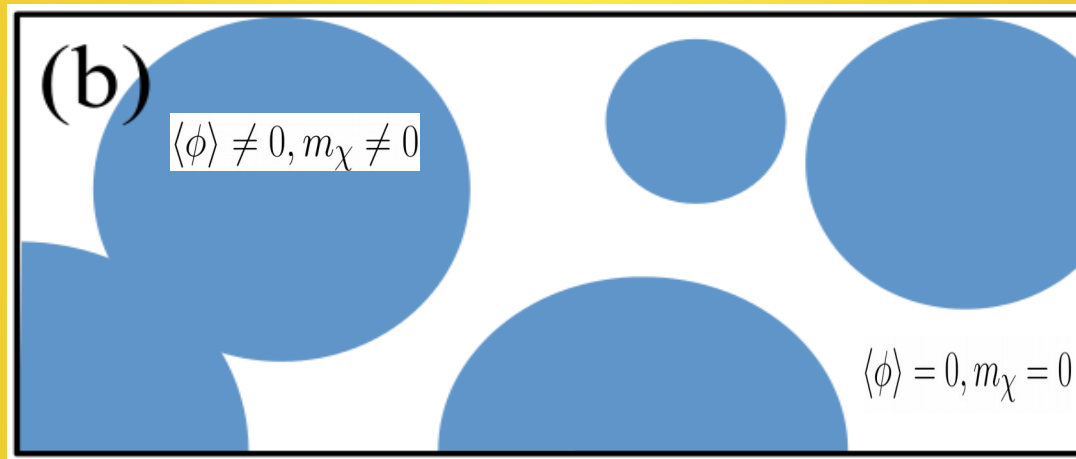


D.Marfatia, P.Y.Tseng

# Introduction

- During **1<sup>st</sup> order phase transition (FOPT)**.

$T_{\star}$



J.P.Hong, S.Jung, K.P.Xie: 2008.04430

# Outline

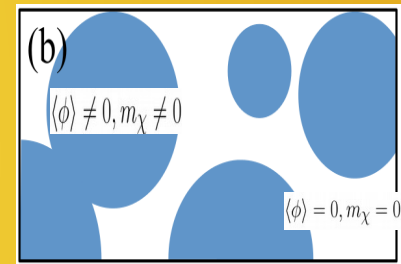
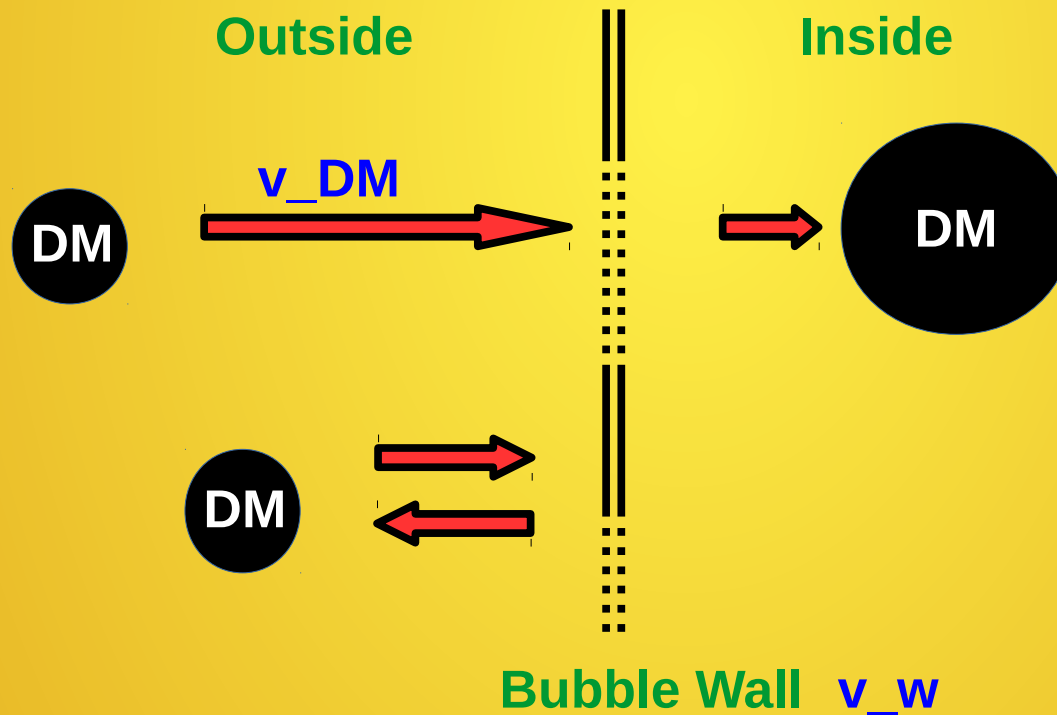
- ◆ Introduction
- ◆ Bubble filtering
- ◆ Gravitational wave production
- ◆ Models
- ◆ Summary

# Bubble filtering



# Bubble filtering

- During **FOPT**, massless (massive) DM particles locate outside (inside) the bubble, and **momentum conservation** must be satisfied at the **bubble wall**.



# Bubble filtering

- If a thermal DM flux is incident on the wall, the number density of DM that enter the bubble is:

$$n_{\chi}^{\text{in}} = n_{\bar{\chi}}^{\text{in}} \simeq \frac{g_{\text{DM}} T_{\star}^3}{\gamma_w v_w} \left( \frac{\gamma_w (1 - v_w) m_{\chi} / T_{\star} + 1}{4\pi^2 \gamma_w^3 (1 - v_w)^2} \right) e^{-\frac{\gamma_w (1 - v_w) m_{\chi}}{T_{\star}}}$$

D.Chway, T.H.Jung, C.S.Shin: 1912.04238

- **DMs are filtered** by the non-relativistic and relativistic bubble wall velocity:

$$n_{\chi}^{\text{in}} = \begin{cases} \sim e^{-m_{\chi}/T_{\star}} & \text{for } v_w \rightarrow 0 \\ \sim e^{-m_{\chi}/(2\gamma_w T_{\star})} & \text{for } m_{\chi}/(\gamma_w T_{\star}) \rightarrow 0 \end{cases}$$

# Bubble filtering

- If  $T_\star < T_{\text{dec}}$ , the DM inside the bubble is decoupled from the thermal bath and become DM relic abundance.
- DM relic abundance today can be calculated by dividing  $n_\chi^{\text{in}} + n_{\bar{\chi}}^{\text{in}}$  by entropy  $s = (2\pi^2/45)g_{\star S}T^3$  :

$$\Omega_{\text{DM}}h^2 \simeq 6.29 \times 10^8 \frac{m_\chi (n_\chi^{\text{in}} + n_{\bar{\chi}}^{\text{in}})}{\text{GeV}} \frac{1}{g_{\star S} T_\star^3}$$

$$\Omega_{\text{DM}}h^2 \simeq \begin{cases} 1.27 \times 10^8 \left( \frac{m_\chi}{\text{GeV}} \right) \left( \frac{g_{\text{DM}}}{g_{\star S}} \right) \left( \frac{m_\chi}{2\gamma_w T_\star} + 1 \right) e^{-\frac{m_\chi}{2\gamma_w T_\star}}, & \text{for } v_w \rightarrow 1 \\ 3.19 \times 10^7 \left( \frac{m_\chi}{\text{GeV}} \right) \left( \frac{g_{\text{DM}}}{g_{\star S}} \right) \left( \frac{1}{v_w} \right) \left( \frac{m_\chi}{T_\star} + 1 \right) e^{-\frac{m_\chi}{T_\star}}, & \text{for } v_w \rightarrow 0. \end{cases}$$

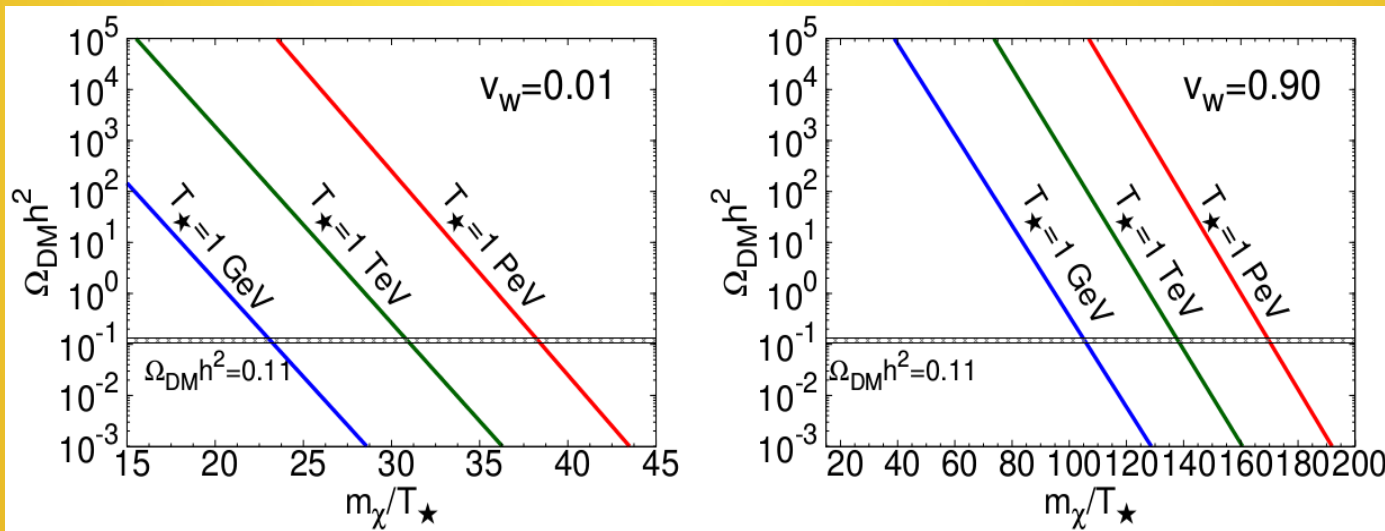
# Bubble filtering

- ♦ If  $T_{\star} < T_{\text{dec}}$ , the DM inside the bubble is decoupled from the thermal bath and become DM relic abundance.
- ♦ DM **relic abundance** today can be calculated by dividing  $n_{\chi}^{\text{in}} + n_{\bar{\chi}}^{\text{in}}$  by entropy  $s = (2\pi^2/45)g_{\star S}T^3$  :
- ♦ For example:  $m_{\chi} \simeq 1 \text{ TeV}, v_w \rightarrow 1$  requires

$$\frac{m_{\chi}}{2\gamma_w T_{\star}} \simeq 27$$

# Bubble filtering

- If  $T_{\star} < T_{\text{dec}}$ , the DM inside the bubble is decoupled from the thermal bath and become DM relic abundance.
- DM relic abundance today can be calculated by dividing  $n_{\chi}^{\text{in}} + n_{\bar{\chi}}^{\text{in}}$  by entropy  $s = (2\pi^2/45)g_{\star}T^3$  :



# Introduction

- ◆ **Sudden DM freeze-out** induced by a FOPT can easily accommodate DM mass above a **PeV**, which is beyond the current DM direct detection and LHC searches.
- ◆ We focus on the **Gravitational Wave (GW)** signals of **Sudden DM freeze-out** with a **FOPT**.

# Gravitational wave production

# Gravitational wave production

- A **FOPT** generates GWs from three processes: I). **Bubble collisions**, II). **Sound wave** in the plasma, III) **Magnetohydrodynamic** (MHD) turbulence.
- The relevant parameters are required to calculate the GW signals:

$$\left\{ \begin{array}{l} T_{\star}, \\ \alpha \equiv \frac{\left(1 - T \frac{\partial}{\partial T}\right) \Delta V_{\text{eff}}|_{T_{\star}}}{\rho(T_{\star})}, \quad \rho \equiv \pi^2 g_{\star} T^4 / 30 \\ \frac{\beta}{H_{\star}} \simeq T_{\star} \frac{d(S_3/T)}{dT} \Big|_{T_{\star}} \\ v_w \end{array} \right.$$



# Gravitational wave production

- A **FOPT** generates GWs from: I). **Bubble collisions**

$$h^2 \Omega_{\text{env}}(f) = 1.67 \times 10^{-5} \left( \frac{H_*}{\beta} \right)^2 \left( \frac{\kappa \alpha}{1 + \alpha} \right)^2 \left( \frac{100}{g_*} \right)^{\frac{1}{3}} \left( \frac{0.11 v_w^3}{0.42 + v_w^2} \right) S_{\text{env}}(f)$$

C.Caprini et. al: 1512.06239

$$S_{\text{env}}(f) = \frac{3.8 (f/f_{\text{env}})^{2.8}}{1 + 2.8 (f/f_{\text{env}})^{3.8}}$$

- The peak frequency is determined by the time scale of **FOPT**  $1/\beta$ :

$$\frac{f_*}{\beta} = \left( \frac{0.62}{1.8 - 0.1 v_w + v_w^2} \right)$$

# Gravitational wave production

- A **FOPT** generates GWs from: I). **Bubble collisions**

$$h^2 \Omega_{\text{env}}(f) = 1.67 \times 10^{-5} \left( \frac{H_*}{\beta} \right)^2 \left( \frac{\kappa \alpha}{1 + \alpha} \right)^2 \left( \frac{100}{g_*} \right)^{\frac{1}{3}} \left( \frac{0.11 v_w^3}{0.42 + v_w^2} \right) S_{\text{env}}(f)$$

C.Caprini et. al: 1512.06239

$$S_{\text{env}}(f) = \frac{3.8 (f/f_{\text{env}})^{2.8}}{1 + 2.8 (f/f_{\text{env}})^{3.8}}$$

- The peak frequency is determined by the time scale of **FOPT**. Then red-shift to present epoch

$$f_{\text{env}} = 16.5 \times 10^{-3} \text{ mHz} \left( \frac{f_*}{\beta} \right) \left( \frac{\beta}{H_*} \right) \left( \frac{T_*}{100 \text{ GeV}} \right) \left( \frac{g_*}{100} \right)^{\frac{1}{6}}$$

Model

# Model: Scalar quartic Model

- ◆ The **finite-temperature** quartic effective scalar potential is:

$$V_{\text{eff}}(\eta, T) = \frac{\mu^2 + DT^2}{2}\eta^2 - \xi T\eta^3 + \frac{\lambda}{4}\eta^4$$

F.C.Adams: [hep-ph/9302321](https://arxiv.org/abs/hep-ph/9302321)

- ◆ Including one-loop Coleman-Weinberg and finite-temperature contributions, potentials of this form are commonly found in *inert singlet*, *inert doublet*, *MSSM*, and *Majoron models*.

# Models: Scalar quartic Model

- ◆ The **finite-temperature** quartic effective scalar potential is:

$$V_{\text{eff}}(\eta, T) = \frac{\mu^2 + DT^2}{2}\eta^2 - \xi T\eta^3 + \frac{\lambda}{4}\eta^4$$

- ◆ Benchmark points:

**Table 1.** Benchmark points (with  $\lambda = 0.1$ ) for the Scalar Quartic Model that give  $\Omega_{\text{DM}}h^2 = 0.11$ .

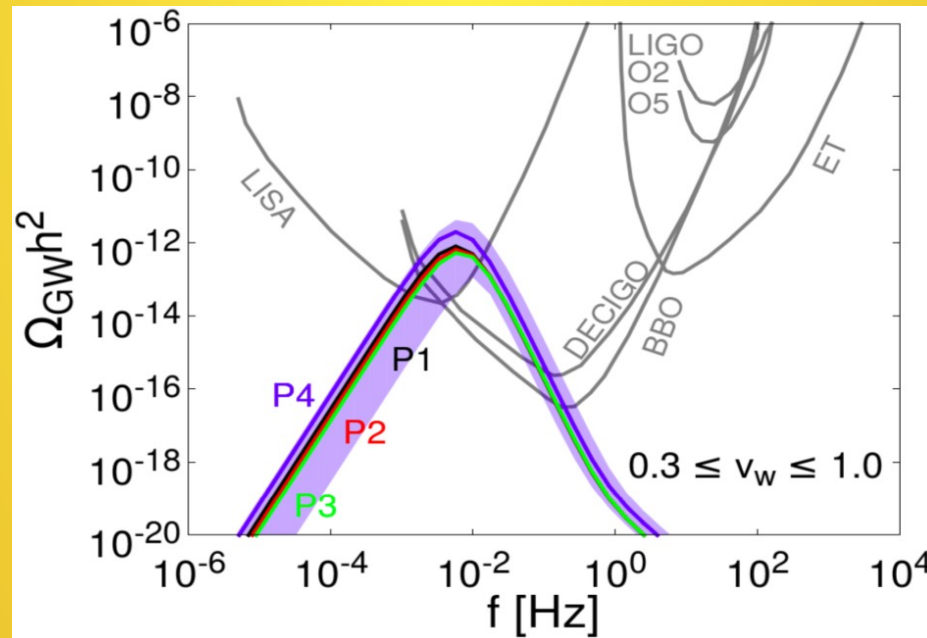
	P1	P2	P3	P4
$\xi$	0.943	0.863	0.796	0.901
$D$	19.7	16.5	14.0	18.0
$g_\chi$	2.97	3.22	3.48	3.31
$\alpha$	0.089	0.082	0.076	0.121
$\beta/H_\star$	1116	1062	1015	1085
$v_\eta/T_\star$	25.71	23.41	21.49	24.51
$v_w$	0.768	0.763	0.760	0.791
$T_\star/\text{GeV}$	21.5	23.8	26.1	22.7
$m_\chi/\text{GeV}$	1642	1799	1953	1838

# Models: Scalar quartic Model

- The **finite-temperature** quartic effective scalar potential is:

$$V_{\text{eff}}(\eta, T) = \frac{\mu^2 + DT^2}{2}\eta^2 - \xi T\eta^3 + \frac{\lambda}{4}\eta^4$$

- GW signals:



D.Marfatia, P.Y. Tseng: 2006.07313

# Summary

- ◆ We studied the **sudden freeze-out DM** as an alternative to the continuous **thermal freeze-out**.
- ◆ A necessary ingredient is a **FOPT** generates DM mass.
- ◆ The **DM relic abundance** may be determined by **bubble filtering**.
- ◆ Because **FOPT** triggers sudden DM freeze-out, **GW** offers a signature.

Thank you!



Back up

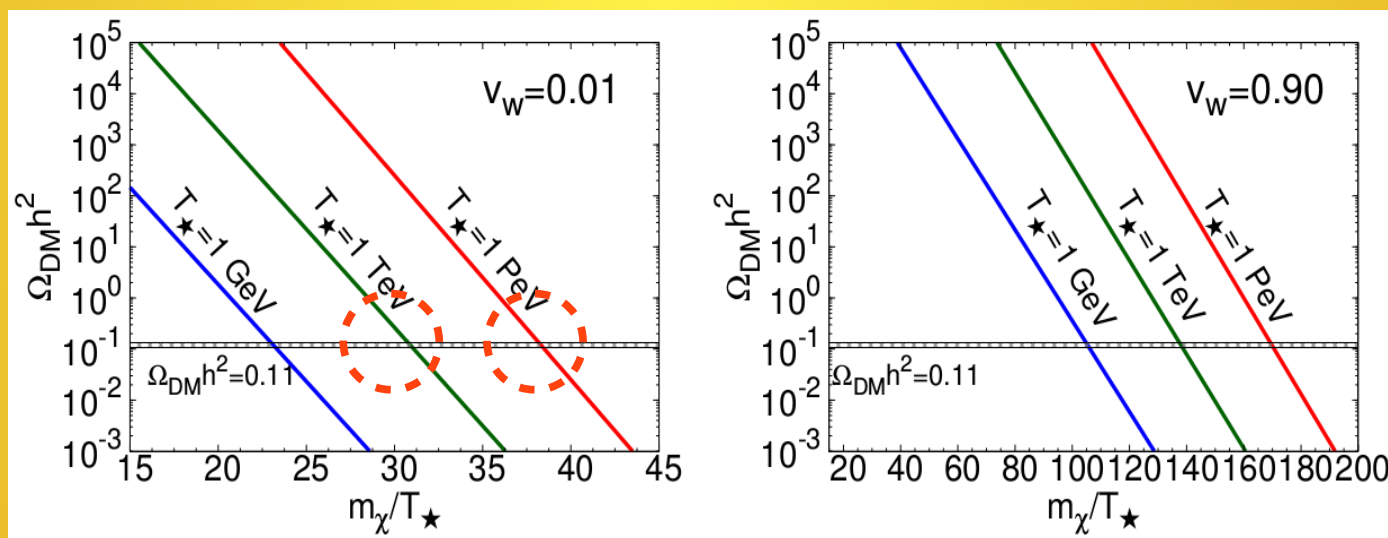
# Introduction

- Only massless **DM** particles carry **kinetic energy** larger than  $m_\chi$  can penetrate the bubble walls and become massive.
- DM inside the bubbles abruptly decouples from the thermal bath if  $T_\star < T_{\text{dec}}$  .
- The bubbles ***filter out*** certain amount of DM and determine the **DM relic abundance**.

# Introduction

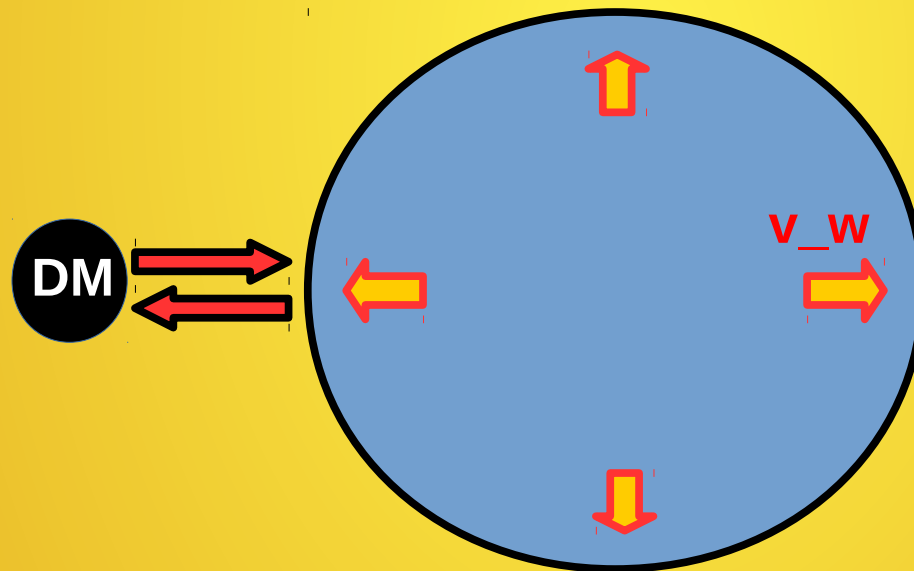
- The  $m_\chi/T_\star$  needed to produce the DM relic abundance depends on the velocity of bubble wall  $v_w$ .

$$T_\star = m_\chi/30 \text{ for } m_\chi = 1 \text{ TeV}, v_w = 0.01$$



# Bubble wall velocity

- Particles reflected by the bubble wall exert pressure on it, and slow down the bubble wall velocity.



# Bubble wall velocity

- ◆ In the **ultrarelativistic** limit, the **pressure** on bubble wall can be obtain from the **light degree of freedom** inside and outside the bubble:

$$P = \frac{d_n g_\star \pi^2}{90} (1 + v_w)^3 \gamma_\omega^2 T_\star^4$$

D.Chway et.al : 1912.04238  
J.R.Espinosa et.al: 1004.4187  
D.Bodeker et.al : 0903.4099

$$d_n \equiv \frac{1}{g_\star} \left[ \sum_{0.2 M_i > \gamma_w T_\star} \left( g_i^b + \frac{7}{8} g_i^f \right) \right]$$

- ◆ The  $v_w$  can be obtained by solving the eq.  $P = \Delta V_{\text{eff}}$  :

$$\alpha = \frac{d_n}{3} (1 + v_w)^3 \gamma_\omega^2$$

$$\alpha \equiv \frac{\left(1 - T \frac{\partial}{\partial T}\right) \Delta V_{\text{eff}}|_{T_\star}}{\rho(T_\star)}, \quad \rho \equiv \pi^2 g_\star T^4 / 30$$

# Bubble wall velocity

- For bubble wall velocity  $v_w$  faster than the sound speed in plasma, but **not ultrarelativistic**, we use the approximation:

P.J.Steinhardt, Phys. Rev. D. 25, 2074 (1982)

$$v_w = \frac{\frac{1}{\sqrt{3}} + \sqrt{\alpha^2 + \frac{2}{3}\alpha}}{1 + \alpha}$$

# Gravitational wave production

- A **FOPT** generates GWs from three processes: I). **Bubble collisions**, II). **Sound wave** in the plasma, III) **Magnetohydrodynamic** (MHD) turbulence.
- The Euclidean action:

$$S_3(T) = 4\pi \int_0^\infty r^2 dr \left[ \frac{1}{2} \left( \frac{d\phi}{dr} \right)^2 + V_{\text{eff}}(\phi, T) \right]$$

- Bubble nucleation rate per unit volume:

$$\Gamma(T) = T^4 \left( \frac{S_3}{2\pi T} \right)^{3/2} e^{-\frac{S_3}{T}}$$

# Gravitational wave production

- A **FOPT** generates GWs from three processes: I). **Bubble collisions**, II). **Sound wave** in the plasma, III) **Magnetohydrodynamic** (MHD) turbulence.
- The fraction of space in the false vacuum:

$$F(t) = \exp \left[ -\frac{4\pi}{3} v_w^3 \int_{t_c}^t dt' (t - t')^3 \Gamma(t') \right]$$

- The percolation temperature  $T_\star$  of **FOPT** is determined by :

$$F(t_\star) = 1/e \simeq 0.37$$



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- The **finite-temperature** quartic effective scalar potential is:

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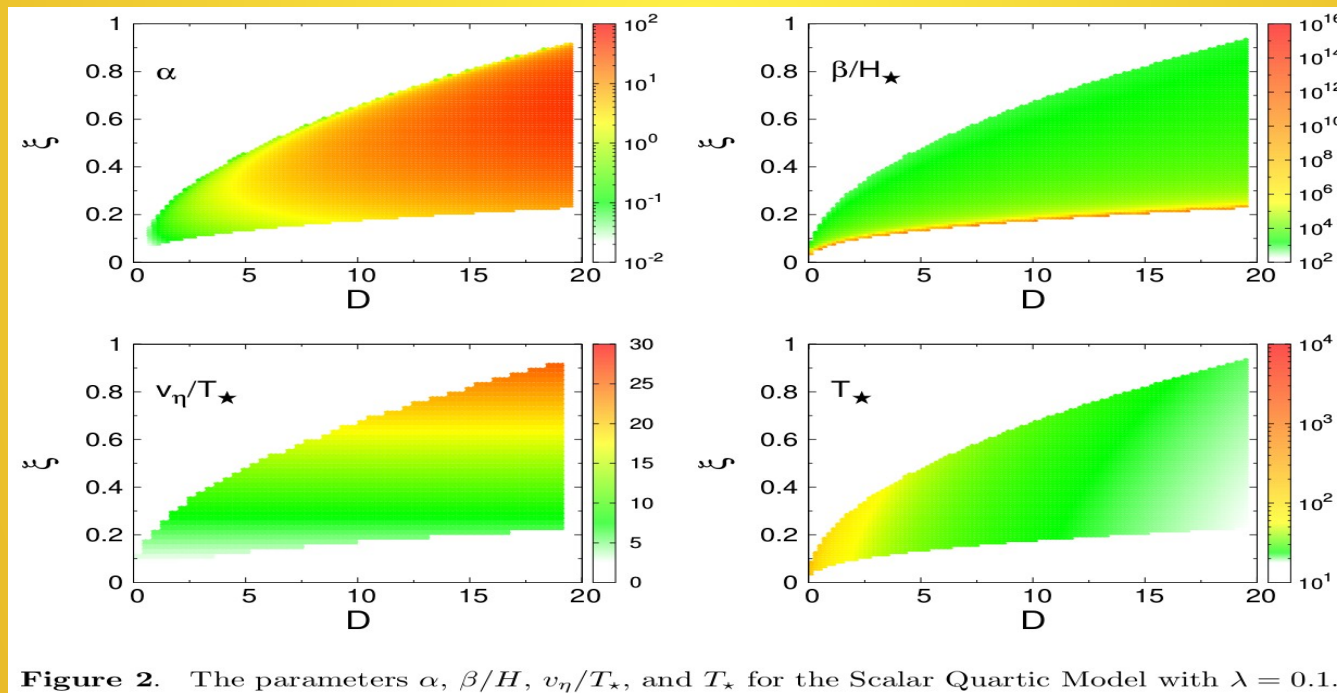


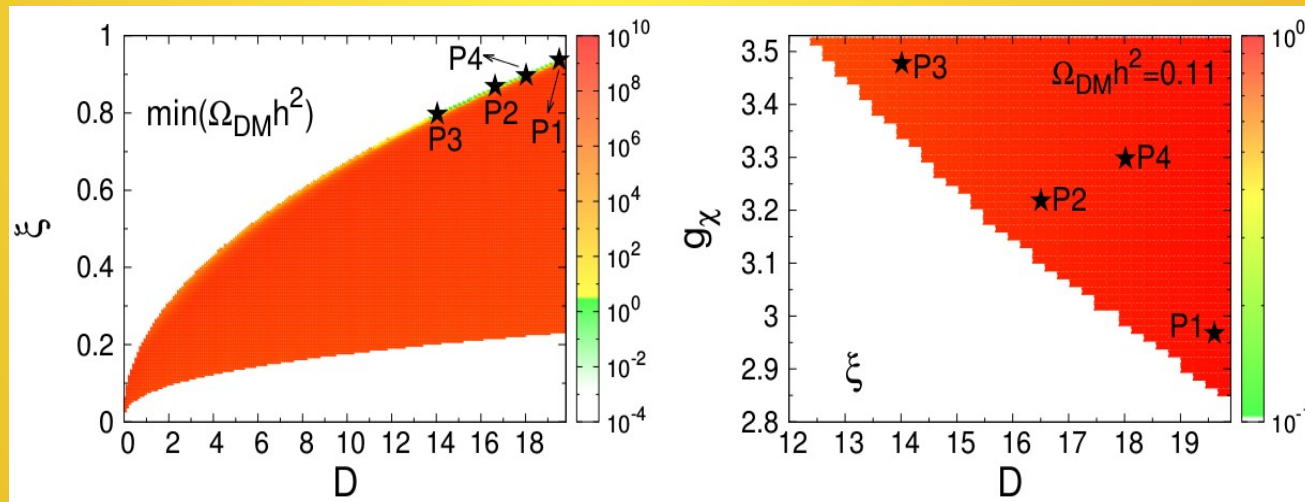
Figure 2. The parameters  $\alpha$ ,  $\beta/H_\star$ ,  $v_\eta/T_\star$ , and  $T_\star$  for the Scalar Quartic Model with  $\lambda = 0.1$ .

# Models: Scalar quartic Model

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- Correct DM relic:



# Models: $SU(2)_X$ model

- In this dimensionless model, the SM gauge group is extended by as  $SU(2)_X$