

On the WIMP dark matter signature in old neutron stars

Natsumi Nagata

University of Tokyo



東京大学
THE UNIVERSITY OF TOKYO

Workshop on Physics of Dark Cosmos
Lavalse Hotel, Busan
Oct 21 – 23, 2022

K. Hamaguchi, N. Nagata, K. Yanagi, Phys. Lett. **B795**, 484 (2019).

WIMP dark matter heating in NS

It has been discussed that the signature of WIMP DM may be detected via the **neutron star (NS) temperature observations.**

PHYSICAL REVIEW D **77**, 023006 (2008)

WIMP annihilation and cooling of neutron stars

Chris Kouvaris*

*CERN Theory Division, CH-1211 Geneva 23, Switzerland,
University of Southern Denmark, Campusvej 55, DK-5230 Odense, Denmark
and The Niels Bohr Institute, Blegdamsvej 17, DK-2100 Copenhagen, Denmark*
(Received 27 August 2007; published 28 January 2008)

PHYSICAL REVIEW D **81**, 123521 (2010)

Neutron stars as dark matter probes

Arnaud de Lavallaz* and Malcolm Fairbairn†

Physics, King's College London, Strand, London WC2R 2LS, United Kingdom
(Received 6 April 2010; published 18 June 2010)

PHYSICAL REVIEW D **82**, 063531 (2010)

Can neutron stars constrain dark matter?

Chris Kouvaris* and Peter Tinyakov†

Service de Physique Théorique, Université Libre de Bruxelles, 1050 Brussels, Belgium
(Received 29 May 2010; published 28 September 2010)

PRL **119**, 131801 (2017)

PHYSICAL REVIEW LETTERS

week ending
29 SEPTEMBER 2017

Dark Kinetic Heating of Neutron Stars and an Infrared Window on WIMPs, SIMPs, and Pure Higgsinos

Masha Baryakhtar,¹ Joseph Bramante,¹ Shirley Weishi Li,² Tim Linden,² and Nirmal Raj³
¹*Perimeter Institute for Theoretical Physics, Waterloo, Ontario N2L 2Y5, Canada*
²*CCAPP and Department of Physics, The Ohio State University, Columbus, Ohio 43210, USA*
³*Department of Physics, University of Notre Dame, Notre Dame, Indiana 46556, USA*
(Received 10 April 2017; revised manuscript received 20 July 2017; published 26 September 2017)

Mechanism

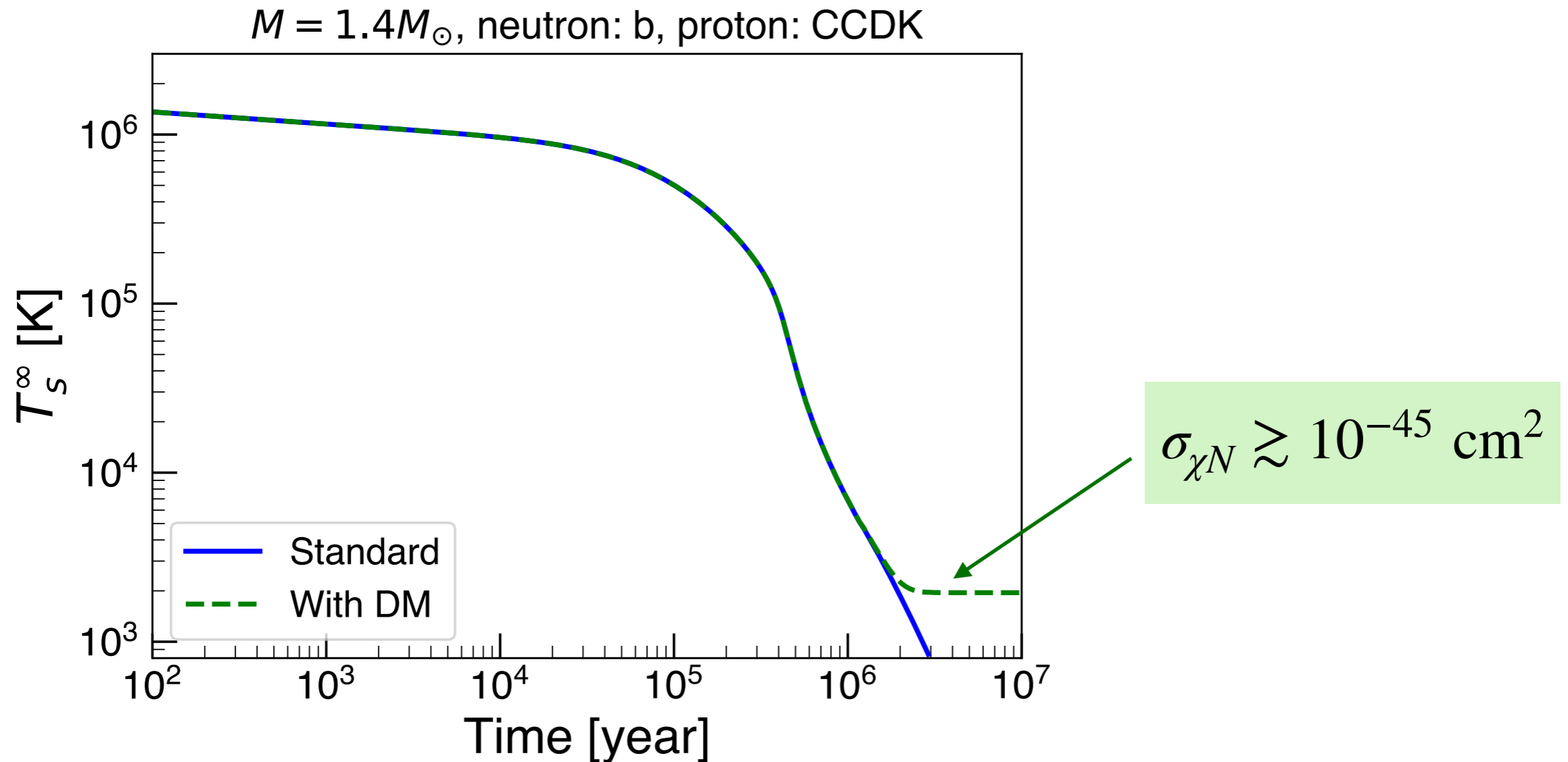
WIMP DM accretes on a neutron star.



Annihilation of WIMPs in the NS core causes **heating effect.**

WIMP dark matter heating in NS

Dark matter heating effect may be observed in **old NSs**.



- In the standard cooling scenario, temperature becomes very low for $t > 10^7$ years.
- With DM heating effect, $T_s^{\infty} \rightarrow \sim 2 \times 10^3$ K at later times.

Questions

It would be nice if we can observe such signature, but is it really possible??

- Observation

In principle, yes, with, e.g., **JWST**. (If we are very lucky)

S. Chatterjee, et.al., arXiv:2205.05048

- Theory

- ▶ Is the standard cooling theory robust?

- ▶ Extra heating source?

Old warm neutron stars?

Recently, “old but warm neutron stars” have been observed.

Milli-second pulsars

▶ J0437-4715: $t_{\text{sd}} = (6.7 \pm 0.2) \times 10^9$ years, $T_s^\infty = (1.25 - 3.5) \times 10^5$ K

O. Kargaltsev, G. G. Pavlov, and R. W. Romani, *Astrophys. J.* **602**, 327 (2004);
M. Durant, *et al.*, *Astrophys. J.* **746**, 6 (2012).

▶ J2124-3358: $t_{\text{sd}} = 11_{-3}^{+6} \times 10^9$ years, $T_s^\infty = (0.5 - 2.1) \times 10^5$ K

B. Rangelov, *et al.*, *Astrophys. J.* **835**, 264 (2017).

Ordinary pulsars

▶ J0108-1431: $t_{\text{sd}} = 2.0 \times 10^8$ years, $T_s^\infty = (1.1 - 5.3) \times 10^5$ K

R. P. Mignani, G. G. Pavlov, and O. Kargaltsev, *Astron. Astrophys.* **488**, 1027 (2008).

▶ B0950+08: $t_{\text{sd}} = 1.75 \times 10^7$ years, $T_s^\infty = (1 - 3) \times 10^5$ K

G. G. Pavlov, *et al.*, *Astrophys. J.* **850**, 79 (2017).

These observations **cannot** be explained in the standard cooling.

Topics of this talk

- We need an extra **heating** source to explain the observations.
- ➔ We find a natural candidate for this.
 - ▶ **Out of β equilibrium effect** was not included in the standard cooling scenario.
 - ▶ This causes **late-time heating**.
 - ▶ The observed data can be explained by this effect.
- Can we still observe the DM heating effect in the presence of this extra heating effect??

Outline of this talk

- Introduction
- Standard Cooling Theory
- Rotochemical Heating
- Results
- Conclusion

Standard Cooling Theory

Standard Cooling of NS

D. Page, J. M. Lattimer, M. Prakash, A. W. Steiner, *Astrophys. J. Suppl.* **155**, 623 (2004);
 M. E. Gusakov, A. D. Kaminker, D. G. Yakovlev, O. Y. Gnedin, *Astron. Astrophys.* **423**, 1063 (2004).

Consider a NS composed of

▶ Neutrons

Form Cooper pairs

▶ Protons

▶ Leptons (e, μ)

● Supposed to be in the β equilibrium.

● In Fermi degenerate states.

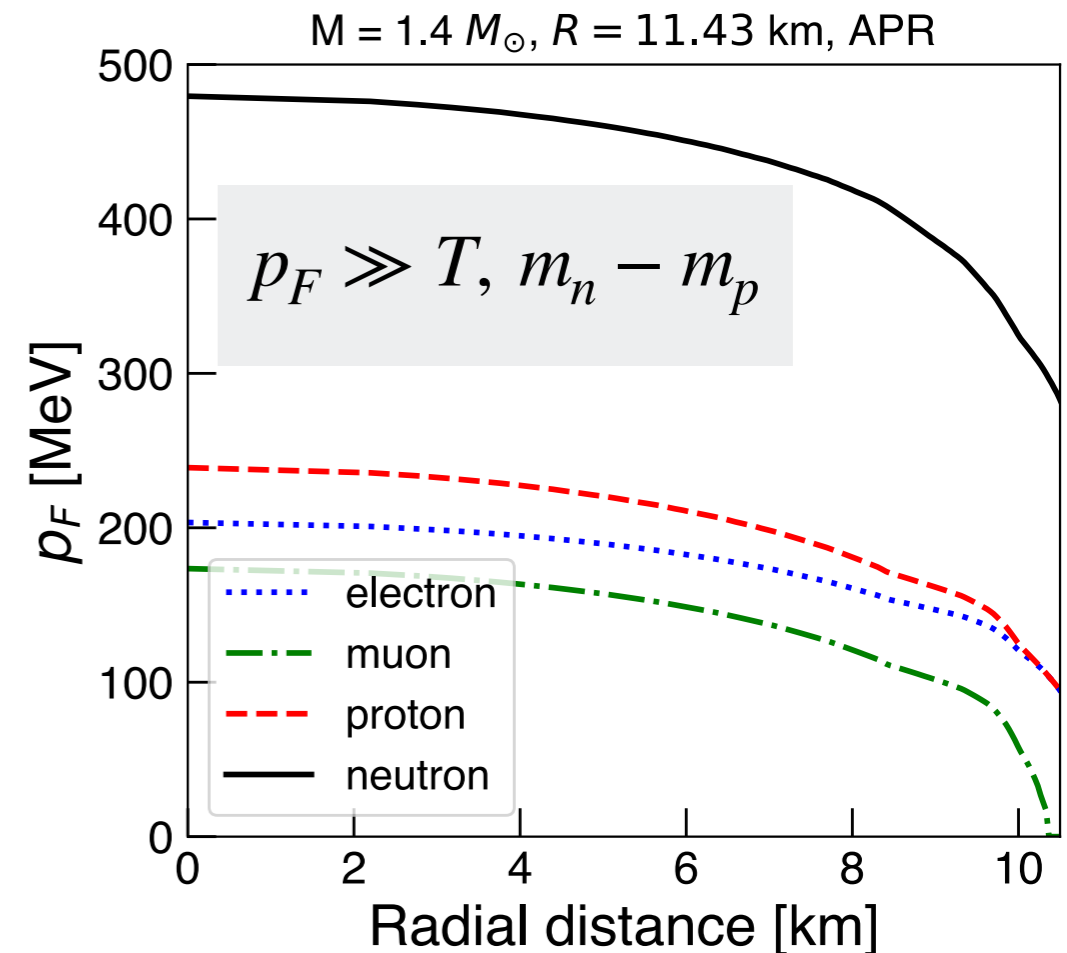
Equation for temperature evolution

$$C(T) \frac{dT}{dt} = -L_\nu - L_\gamma$$

$C(T)$: Stellar heat capacity

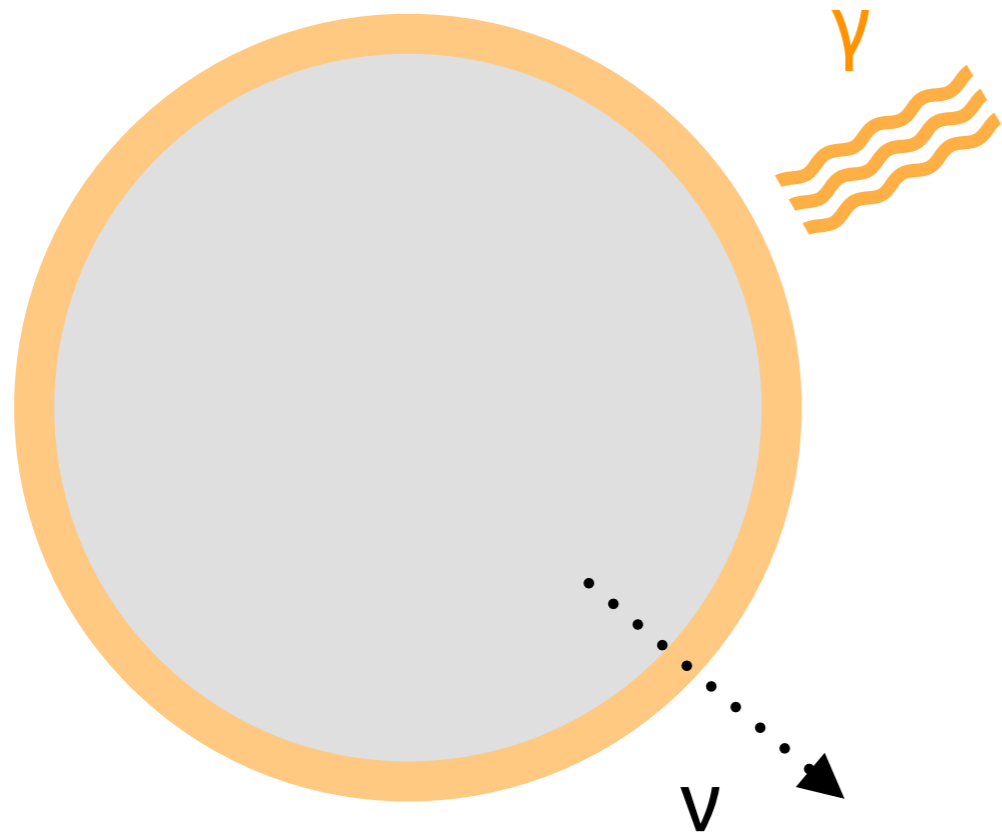
L_ν : Luminosity of neutrino emission

L_γ : Luminosity of photon emission



Cooling sources

Two cooling sources:



Dominant for $t \lesssim 10^5$ years

Photon emission (from surface)

$$L_{\gamma} = 4\pi R^2 \sigma_{\text{SB}} T_s^4$$

Dominant for $t \gtrsim 10^5$ years

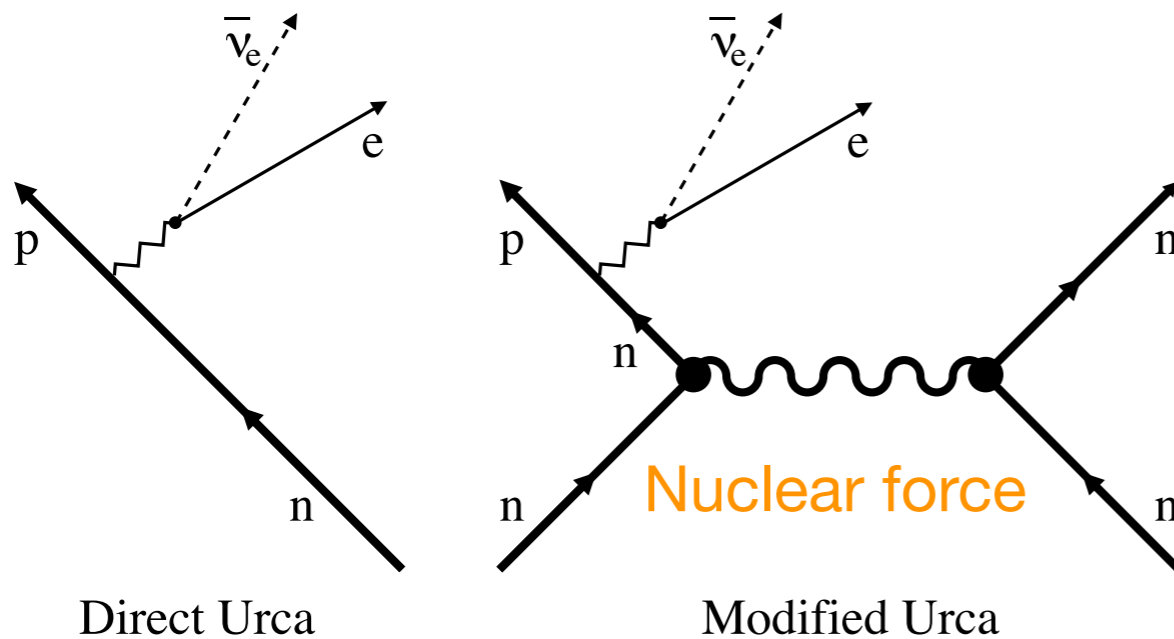
Neutrino emission (from core)

- ▶ Direct Urca process (DURca)
- ▶ Modified Urca process (MURca)
- ▶ Bremsstrahlung
- ▶ PBF process

Occurs when nucleon pairings are formed.

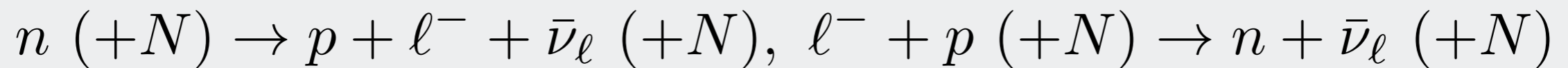
Urca processes

Urca processes keep NSs into β equilibrium:



Chemical equilibrium

$$\mu_n = \mu_p + \mu_e$$



Rapid **Direct Urca** process can occur only in **heavy stars**.

For the APR equation of state, $M \gtrsim 1.97M_\odot$

Effects of nucleon pairings

Nucleons in a NS form **Cooper pairings**.

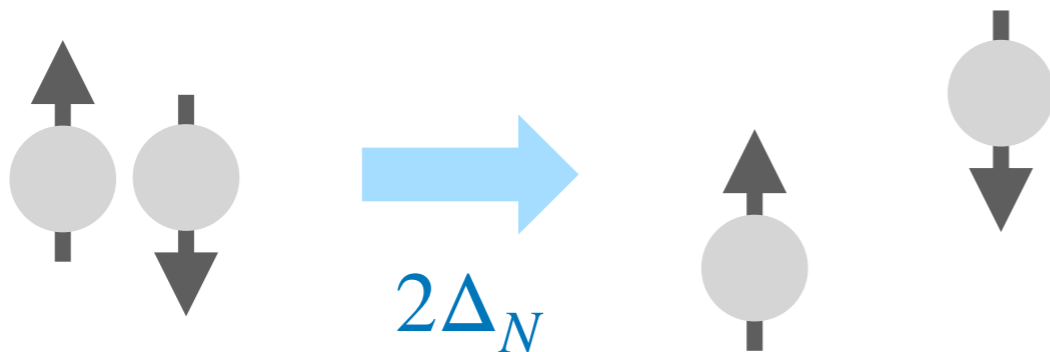
Energy spectrum

$$\epsilon_N(\mathbf{p}) \simeq \sqrt{\Delta_N^2 + v_{F,N}^2 (\mathbf{p} - \mathbf{p}_{F,N})^2}$$

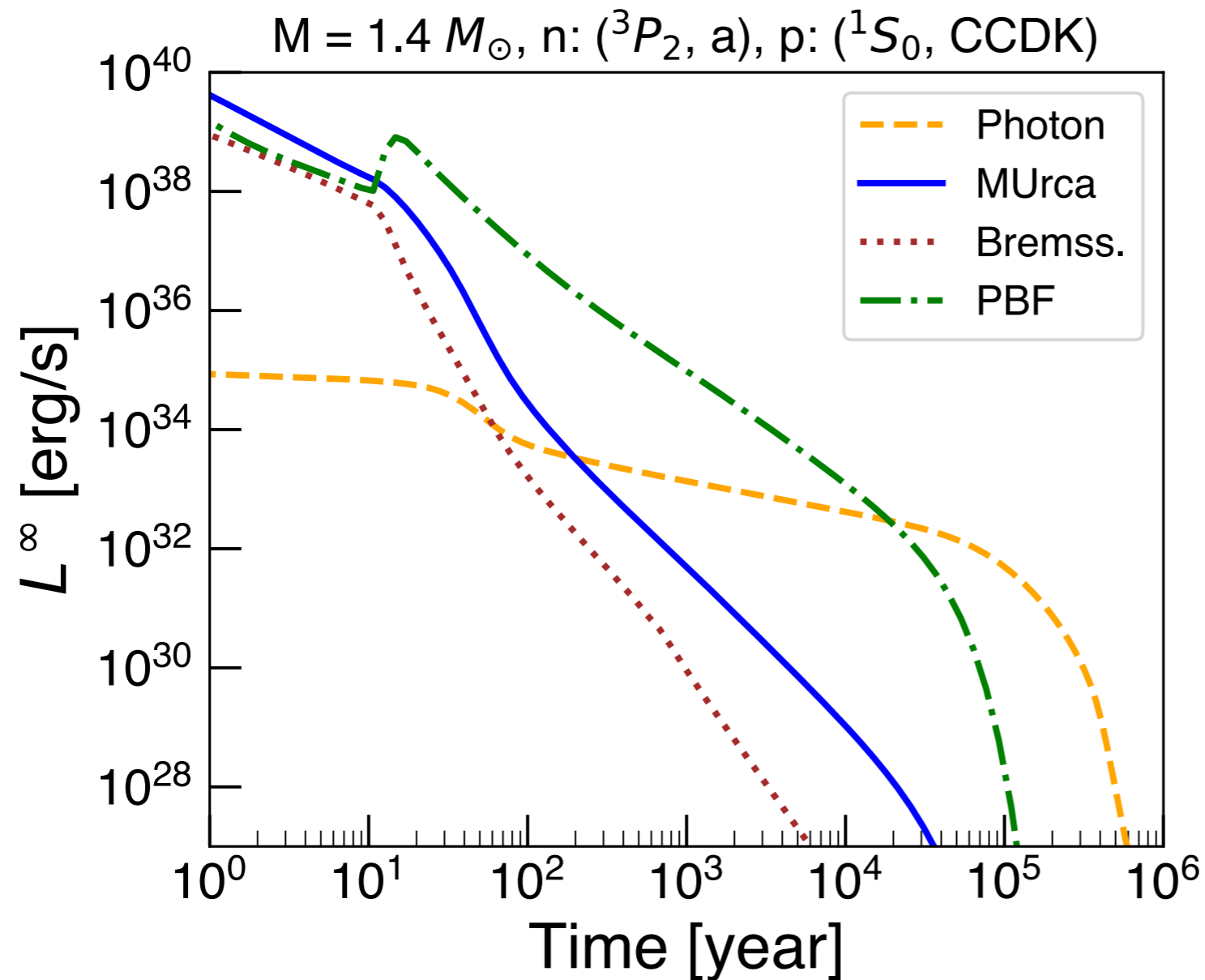
Δ_N : pairing gap

This pairing energy gap highly **suppresses the neutrino emission** at low temperatures.

$$\propto e^{-\frac{\Delta_N}{T}}$$

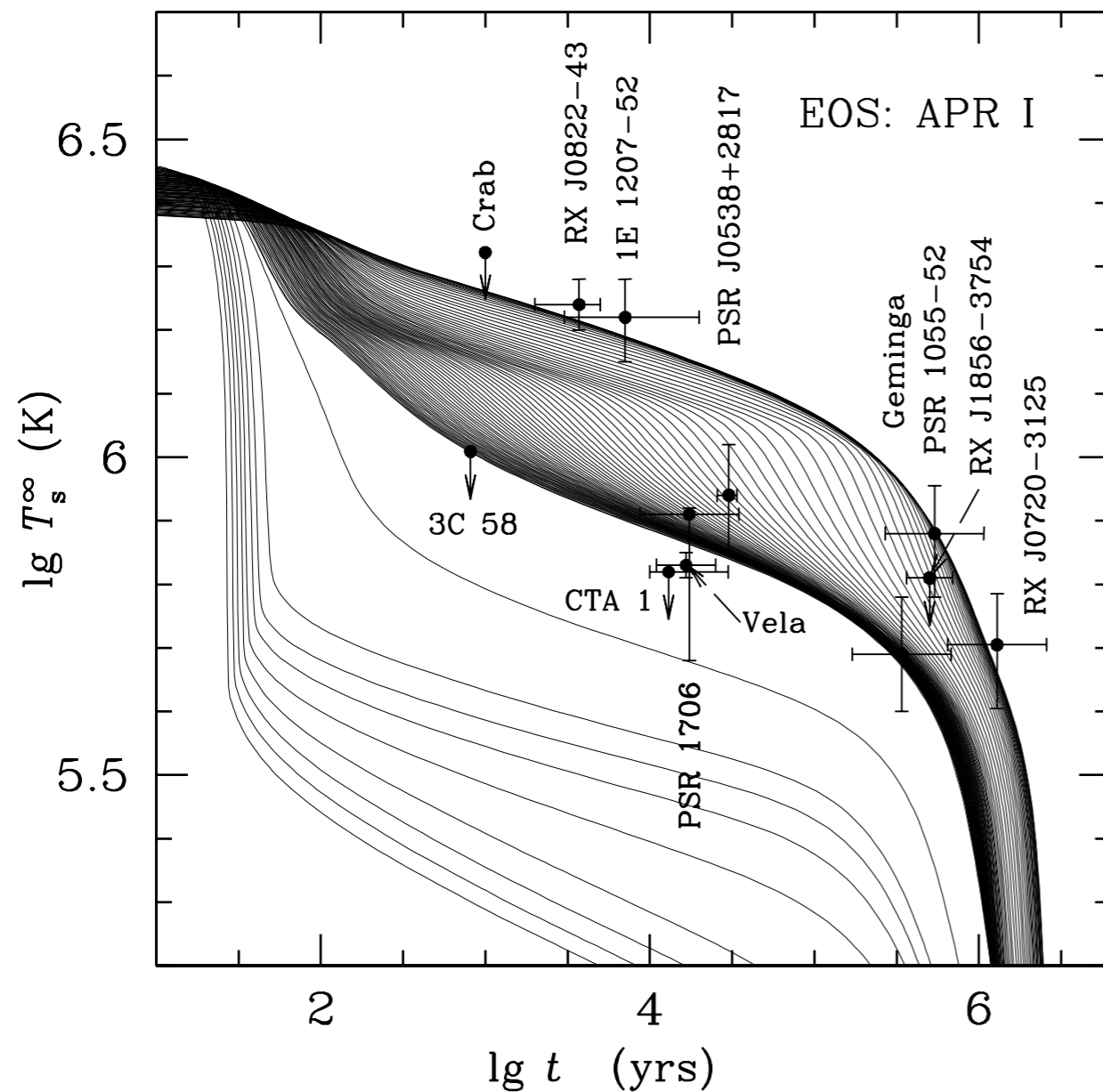


Luminosity



- Photon emission becomes dominant after $\sim 10^5$ years.
- Urca process is extremely suppressed at later times.

Success of Standard Cooling



$$M = (1.01 - 1.92)M_{\odot}$$

O. Y. Gnedin, M. Gusakov, A. Kaminker, D. G. Yakovlev,
 Mon. Not. Roy. Astron. Soc. **363**, 555 (2005).

- Temperature gets very low for $t \gtrsim 10^6$ years.
- Consistent with the observations for $t < 10^6$ years. ~ 50 NSs listed.

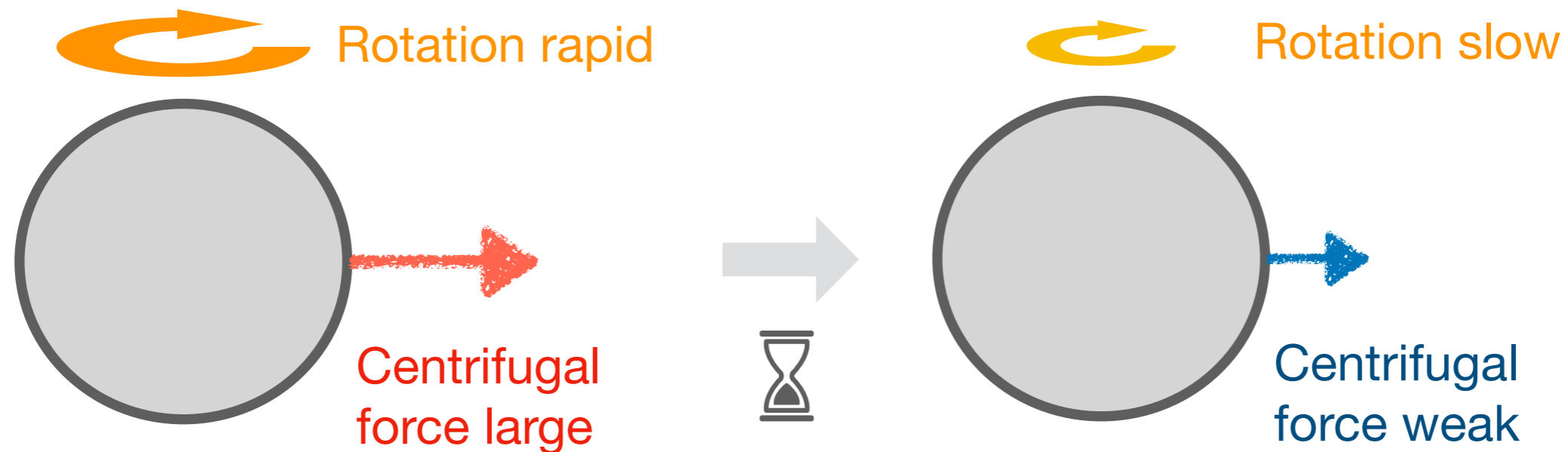
For the latest data, see <http://www.ioffe.ru/astro/NSG/thermal/cooldat.html>

Role of non-equilibrium β processes

Loop hole in standard cooling

In the standard cooling, β equilibrium is assumed.

In a real pulsar



Local pressure changes. **Chemical equilibrium condition changes.**

At low temperatures, the **rate of Urca process is fairly suppressed.**

➔ **Deviation from β equilibrium**

Out of β equilibrium

Deviation from β equilibrium is quantified by

$$\eta_\ell \equiv \mu_n - \mu_p - \mu_\ell \quad (\ell = e, \mu)$$

At early times

Urca processes are rapid.

➔ NS can follow the change in the equilibrium condition.

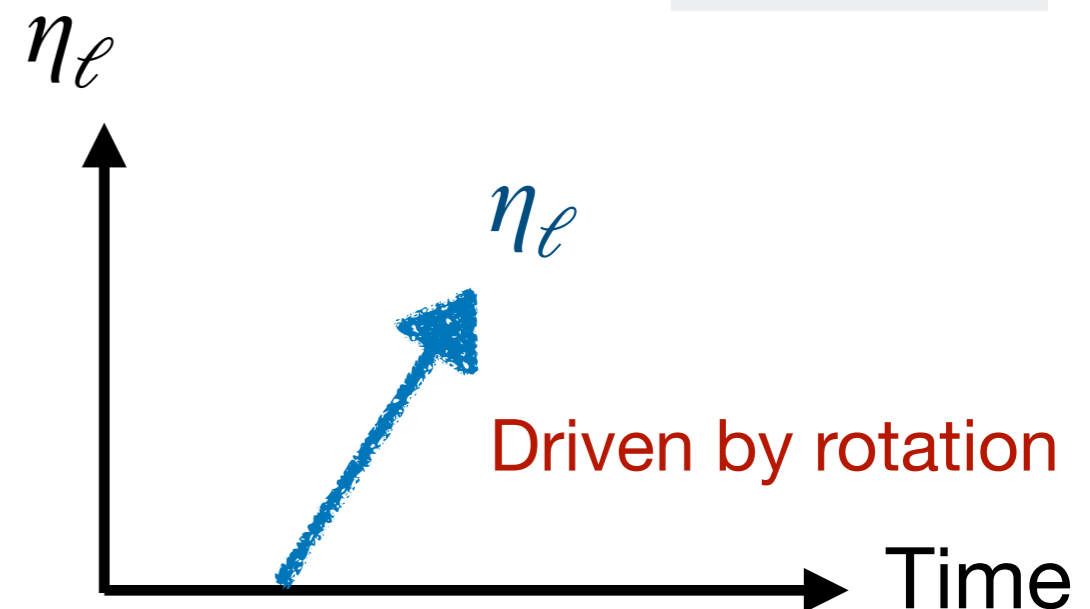
At later times

$$\eta_\ell = 0$$

Urca processes are too slow.

➔ Deviation from β equilibrium

➔ η_ℓ increases!



Rotochemical heating

R. Fernandez and A. Reisenegger, *Astrophys. J.* **625**, 291 (2005);
C. Petrovich, A. Reisenegger, *Astron. Astrophys.* **521**, A77 (2010).

Once η_ℓ exceeds a **threshold** Δ_{th} determined by nucleon gaps,

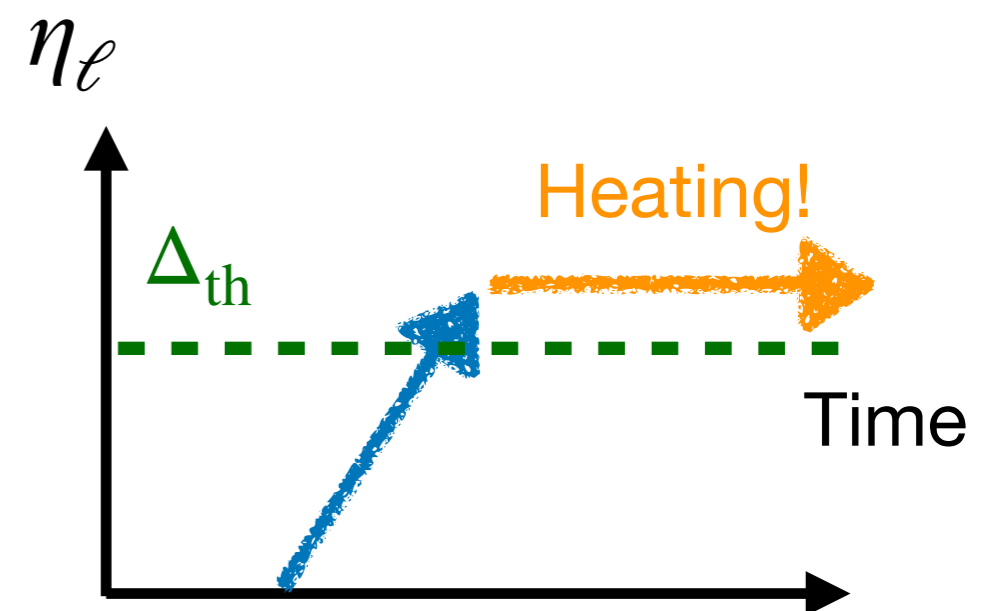
$$\Delta_{\text{th}} = \min \{3\Delta_n + \Delta_p, \Delta_n + 3\Delta_p\}$$

- ▶ Urca processes are **enhanced**.
- ▶ Generation of **heat**

Called the **rotochemical heating**.

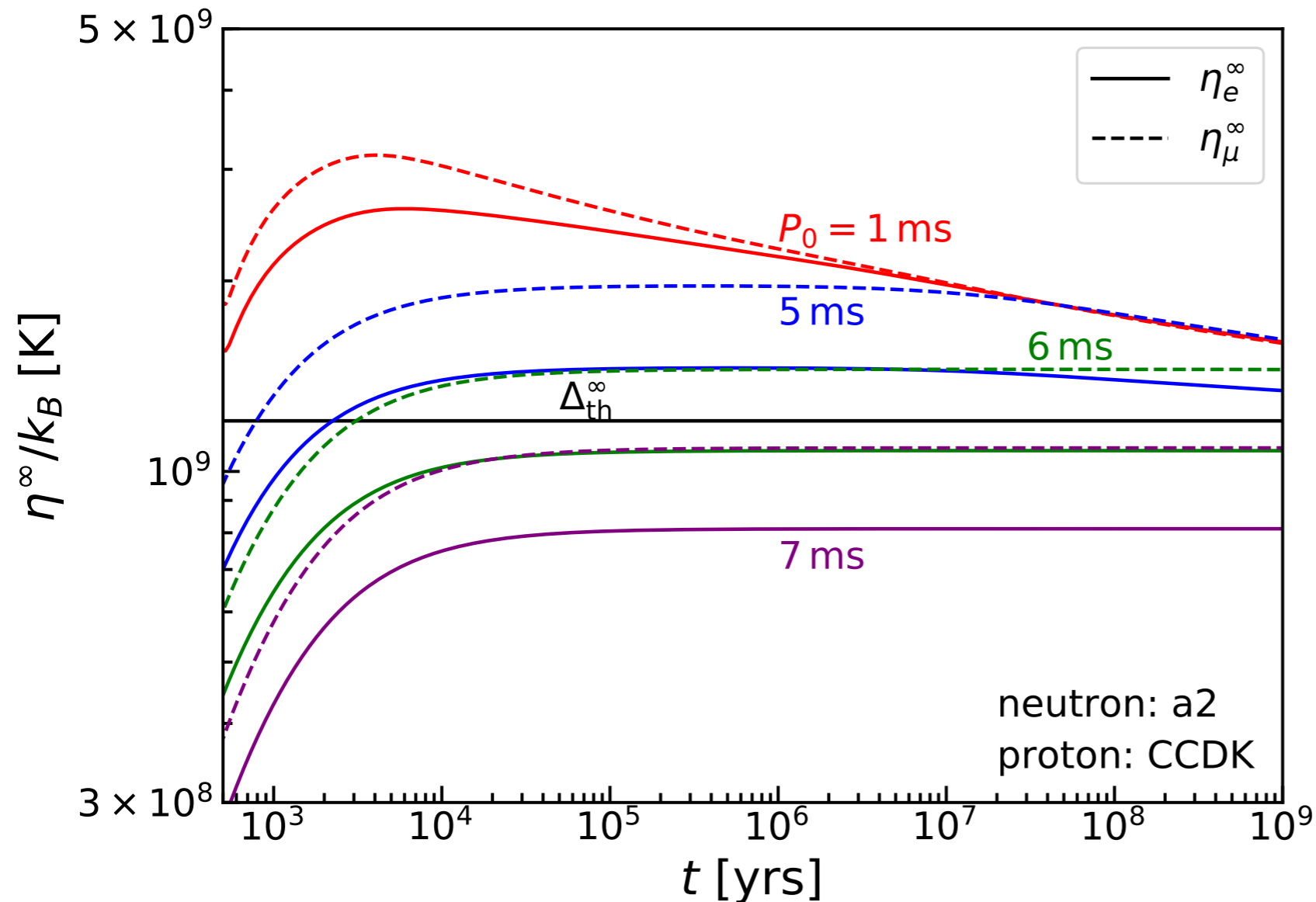
It occurs in the **same setup** as the standard cooling.

- No exotic physics needed.
- This effect should have been included from the beginning...



Evolution of chemical imbalance

Since the deviation from equilibrium is driven by rotation, it strongly depends on the value of **initial period**.



$$M = 1.4M_{\odot}$$

$$P = 1 \text{ s}$$

$$\dot{P} = 10^{-15}$$

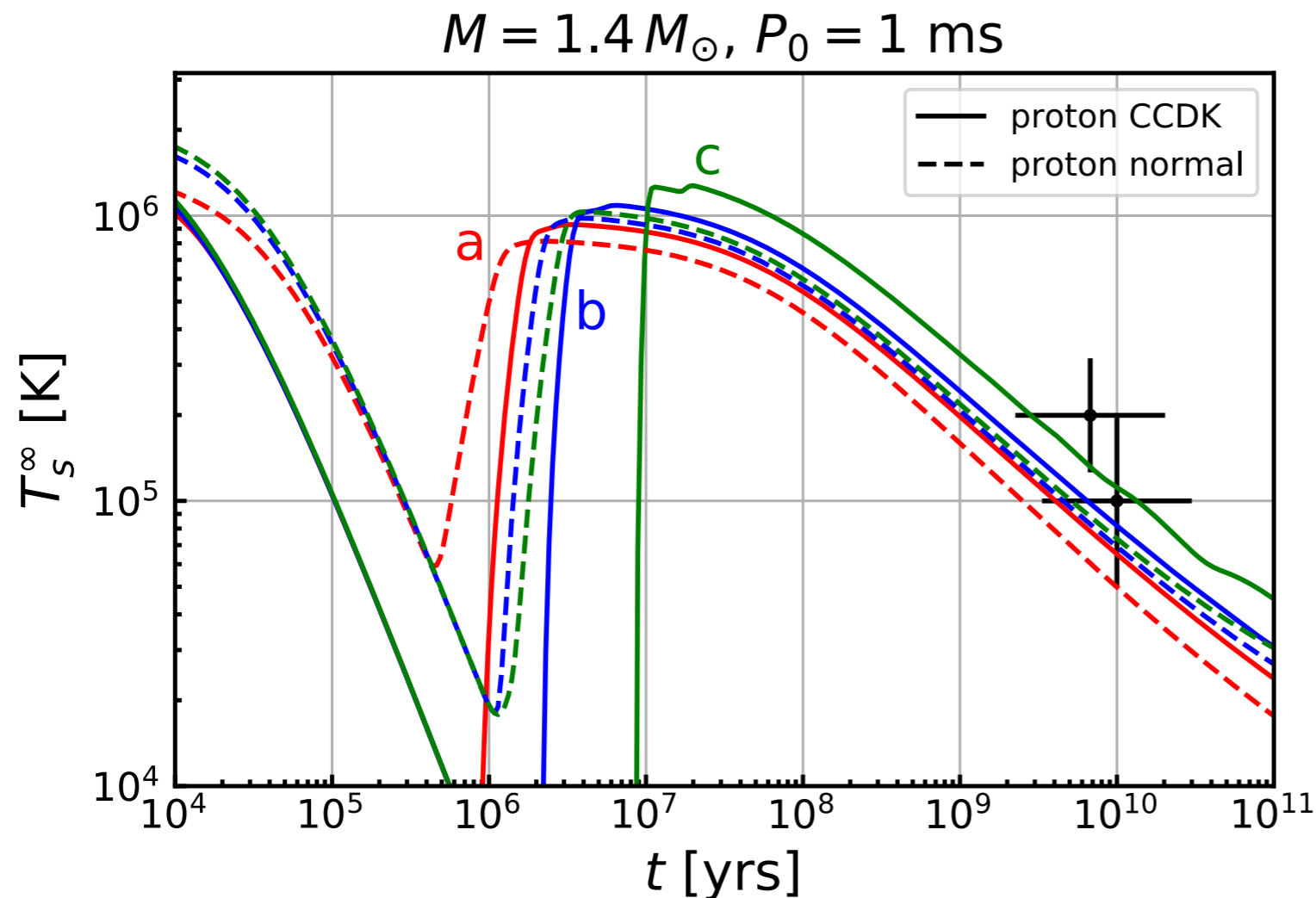
Magnetic dipole radiation

$$\dot{\Omega} = -k\Omega^3$$

Rotochemical heating occurs if the initial period P_0 is small enough.

Millisecond pulsars

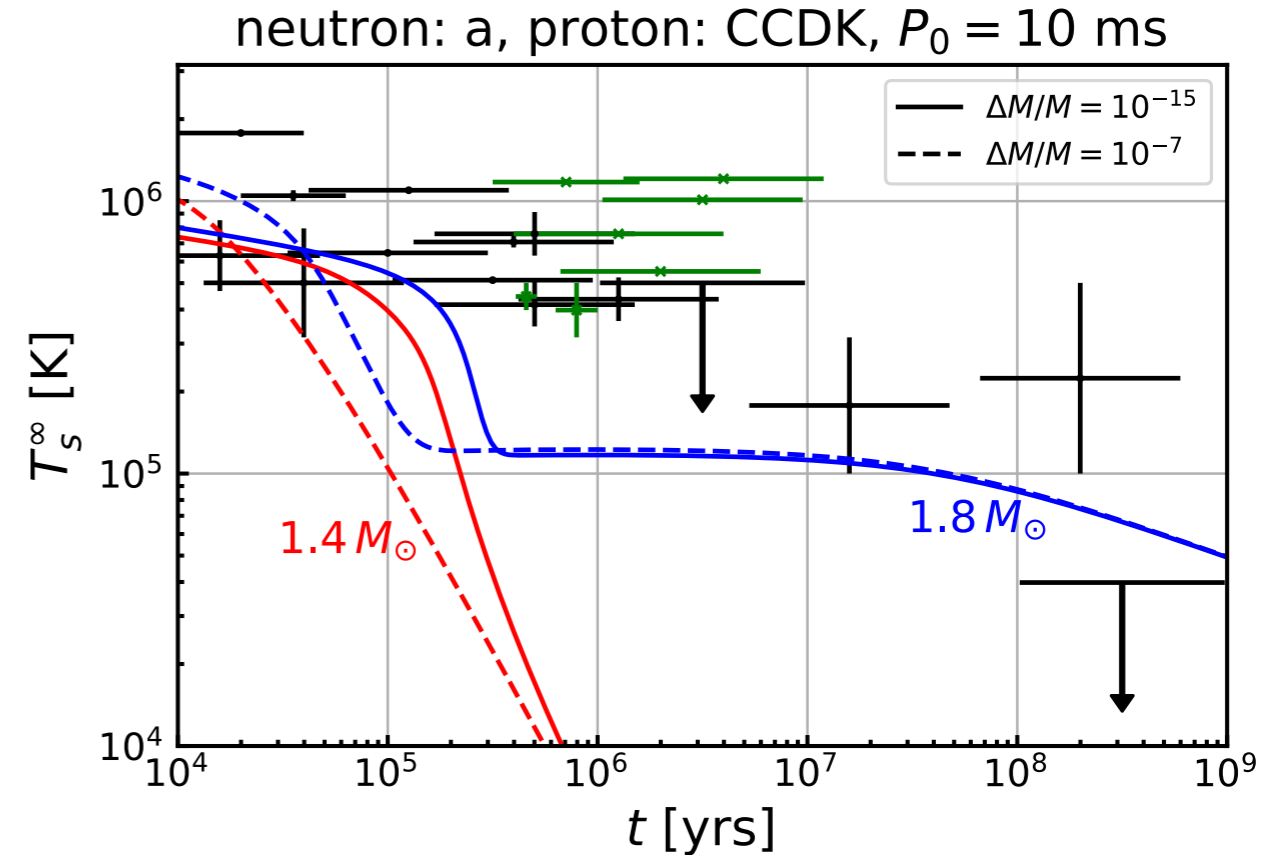
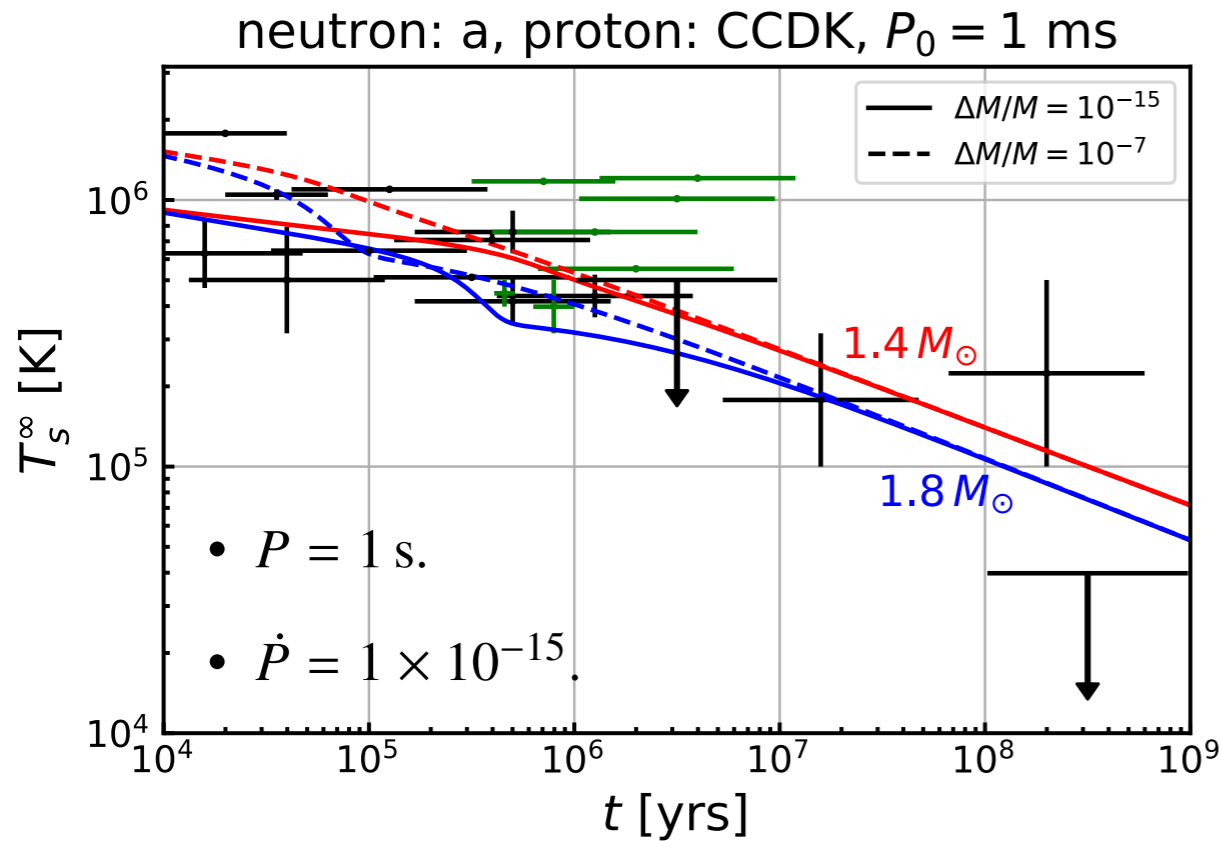
We take account of the effect of **non-equilibrium β processes**.



- $M = 1.4 M_{\odot}$.
- $P = 5.8 \text{ ms}$.
- $\dot{P} = 5.7 \times 10^{-20}$.

- Rotochemical heating always occurs in MSPs.
- We can explain the observations.

Ordinary pulsars

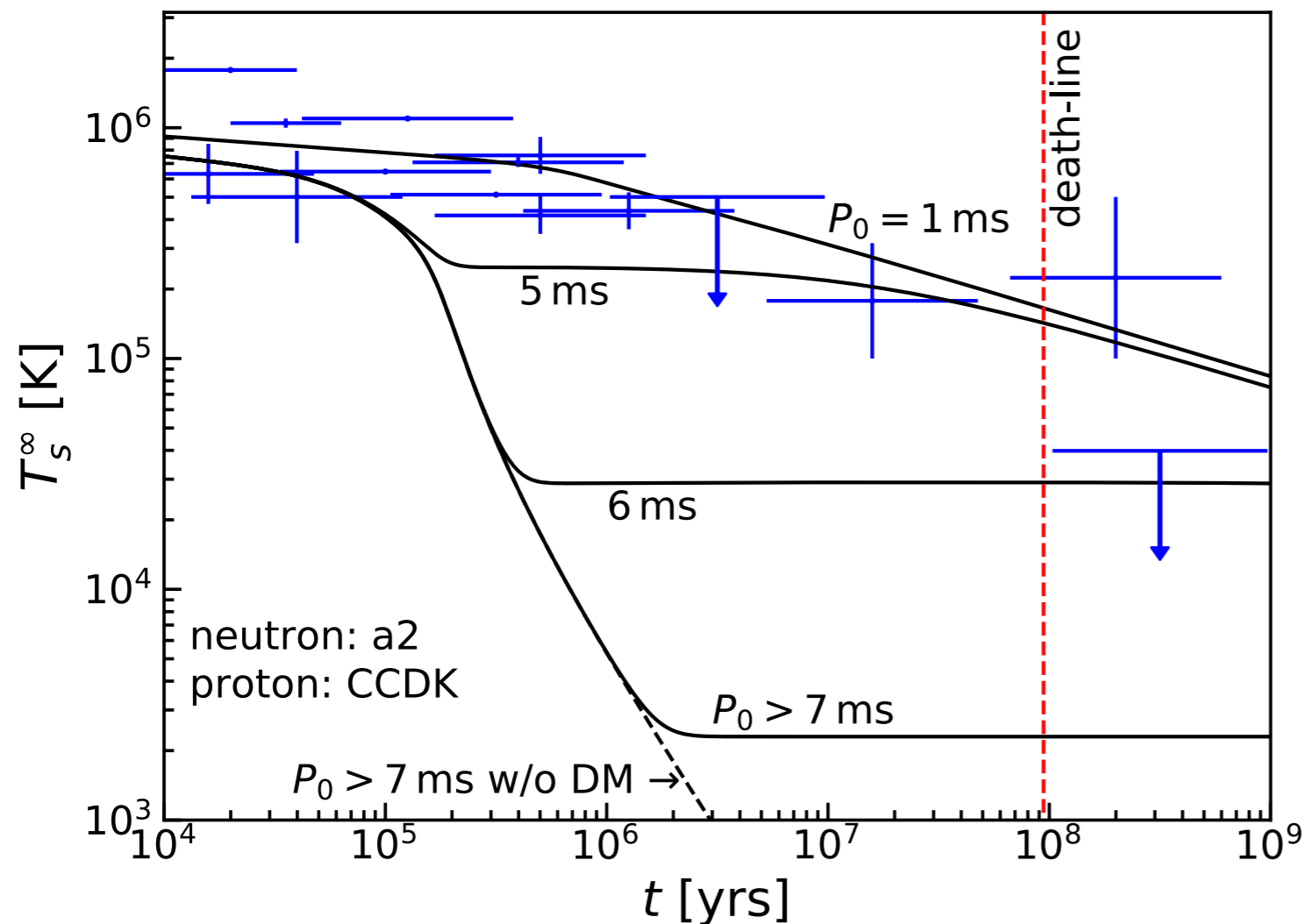


- The temperature evolution highly depends on the **initial period P_0** of pulsars.
- We can explain all of the observations.
 - ▶ Cool star: large initial period \rightarrow no rotochemical heating.
 - ▶ Warm star: small initial period \rightarrow rotochemical heating effective.

Rotochemical heating vs DM heating

Rotochemical heating vs DM heating

Now we include both the **DM** and **rotochemical** heating effects.



Simulations show that P_0 can be as large as $O(100)$ ms.

See, e.g., 1811.05483.

- If P_0 is large enough, DM heating effect can be observed.
- It is always concealed in millisecond pulsars.

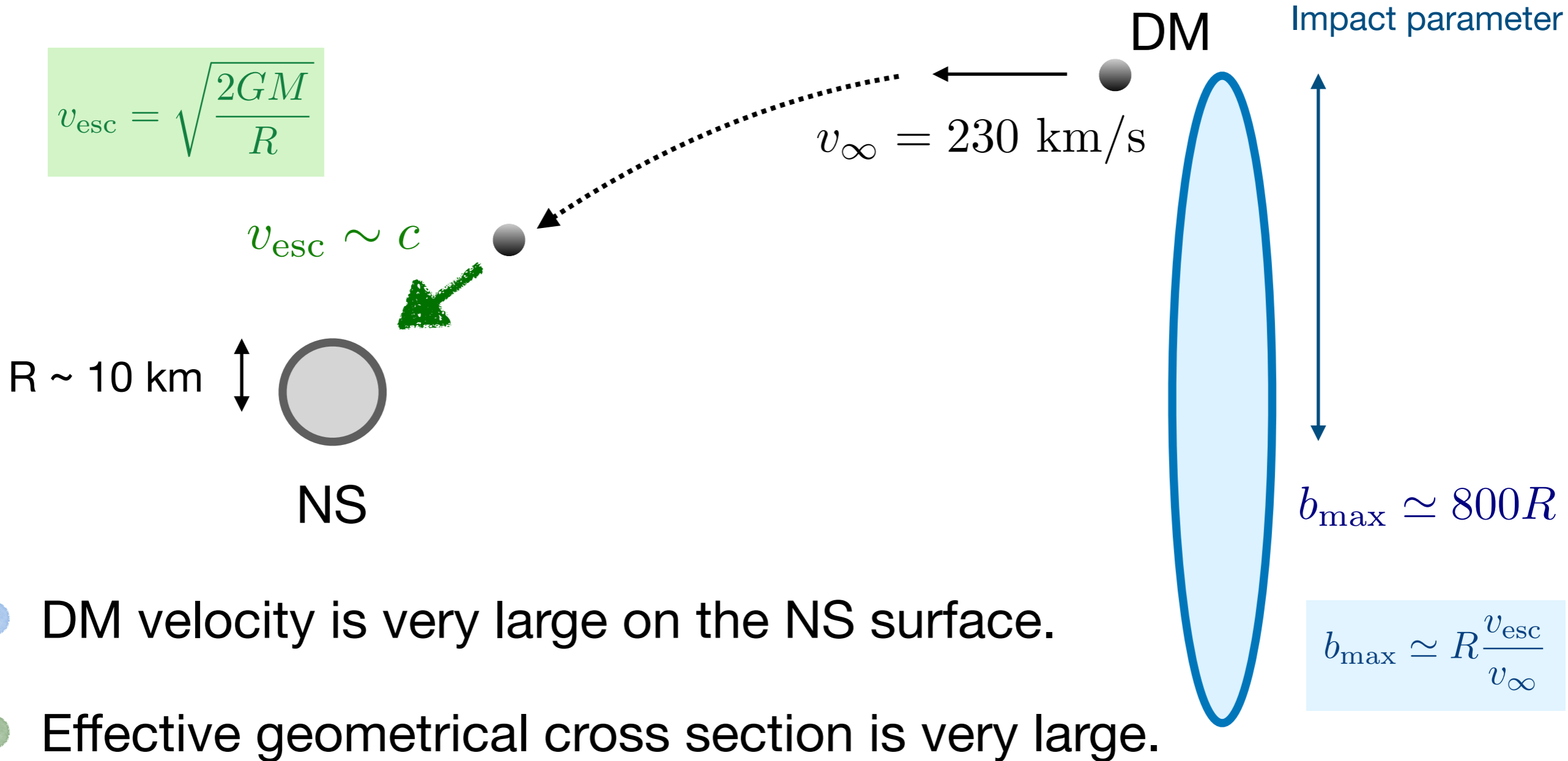
Conclusion

Conclusion

- We studied the NS temperature evolution including both the **rotochemical** and **DM heating** effects.
- For **ordinary pulsars**, DM heating effect can be observed if their initial period is relatively large.
- For **millisecond pulsars**, DM heating effect is always hidden by the rotochemical heating.
- In any case, an observation of a NS with $T_s^\infty \lesssim 10^3$ K can give a stringent constraint on WIMP DM.

Backup

Dark matter accretion in NS



DM accretion rate is

$$\dot{N} \simeq \pi b_{\text{max}}^2 v_{\infty} \cdot \frac{\rho_{\text{DM}}}{m_{\text{DM}}}$$

DM number density

Dark matter accretion in NS

It is found that

- One scattering is enough for WIMPs to be captured.

Energy transfer $\sim 100 \text{ MeV} - 1 \text{ GeV}$.

- At least one scattering occurs if $\sigma_N \gtrsim 10^{-45} \text{ cm}^2$.

For old NSs, we have

Accretion rate

=

Annihilation rate

equilibrium

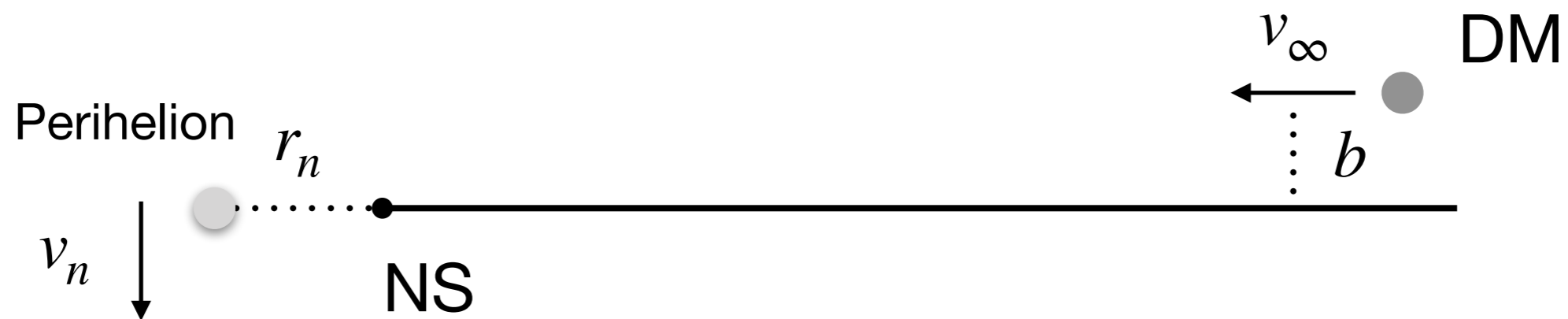


$$L_H \simeq m_{\text{DM}} \dot{N} \simeq 2\pi G M R \rho_{\text{DM}} / v_\infty$$

Independent of DM mass.

Dark matter accretion in NS

Consider a WIMP with mass m_{DM} , incoming from infinity with speed v_∞ and impact parameter b .



Energy

$$\frac{m_{\text{DM}}v_\infty^2}{2} = \frac{m_{\text{DM}}v_n^2}{2} - \frac{Gm_{\text{DM}}M}{r_n}$$

Angular momentum

$$m_{\text{DM}}v_\infty b = m_{\text{DM}}v_n r_n$$



$$r_n = \frac{GM}{v_\infty^2} \left[\sqrt{1 + \frac{v_\infty^4 b^2}{G^2 M^2}} - 1 \right]$$

Dark matter accretion in NS

For a WIMP to be captured by a NS, $r_n \leq R$ is required.

→ $b \leq R \left[1 + \frac{v_{\text{esc}}^2}{v_{\infty}^2} \right]^{\frac{1}{2}}$ $v_{\infty} \simeq 230 \text{ km/s}$

Escape velocity

$$v_{\text{esc}} = \sqrt{\frac{2GM}{R}} \simeq 2 \times 10^8 \times \left(\frac{M}{1.4M_{\odot}} \right)^{1/2} \left(\frac{R}{10 \text{ km}} \right)^{-1/2} \text{ m/s}$$

Close to the speed of light!

Maximum impact parameter

$$b_{\text{max}} \simeq R \frac{v_{\text{esc}}}{v_{\infty}} \simeq 0.8 \times 10^7 \times \left(\frac{M}{1.4M_{\odot}} \right)^{1/2} \left(\frac{R}{10 \text{ km}} \right)^{1/2} \text{ m}$$

Much larger than the NS radius.

Recoil energy

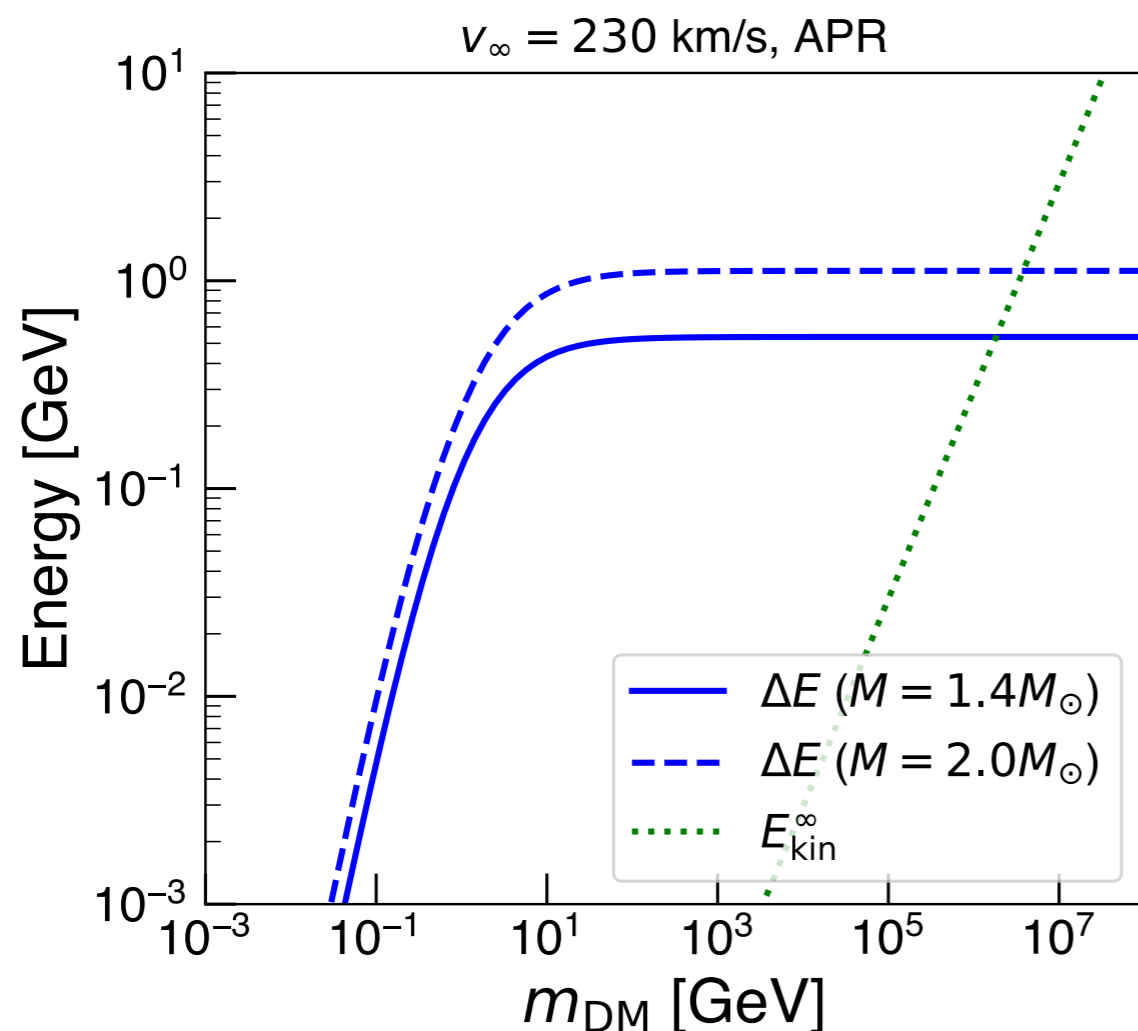
For each DM-nucleon scattering, WIMPs lose energy by

$$\Delta E = \frac{m_N m_{\text{DM}}^2 \gamma_{\text{esc}}^2 v_{\text{esc}}^2}{m_N^2 + m_{\text{DM}}^2 + 2\gamma_{\text{esc}} m_{\text{DM}} m_N} (1 - \cos \theta_c)$$

θ_c : scattering angle
in the CM frame.

$$\gamma_{\text{esc}} \equiv (1 - v_{\text{esc}}^2)^{-1/2}$$

Let us compare this with the **initial kinetic energy**: $E_{\text{kin}}^\infty = m_{\text{DM}} v_\infty^2 / 2$



- **One scattering** is sufficient for WIMPs to lose the initial kinetic energy.
- Energy transfer can be as large as **O(100) MeV**.

One scattering in NS

WIMP-nucleon scattering occurs **at least once** if

$$\text{Mean Free Path} \sim (\sigma_N n)^{-1} \sim \frac{m_N R^3}{M \sigma_N} \lesssim R \quad \Rightarrow \quad \sigma_N \gtrsim 10^{-45} \text{ cm}^2$$

σ_N : DM-nucleon scattering cross section

If this is satisfied, then **all of the accreted WIMPs are captured**.

If not, capture rate is **suppressed by $\sigma_N / \sigma_{\text{th}}$** .

Captured WIMPs eventually **annihilate** inside the NS core.

For old NSs, we have

Accretion rate

=

Annihilation rate

equilibrium

NS temperature with DM heating

At later times, the **DM heating** balances with the **cooling** by photon emission.

$$L_H = L_\gamma$$

$$L_H \simeq m_{\text{DM}} \dot{N} \simeq 2\pi G M R \rho_{\text{DM}} / v_\infty$$

Independent of DM mass.



$$2\pi G M R \rho_{\text{DM}} / v_\infty \simeq 4\pi R^2 \sigma_{\text{SB}} T_s^4$$

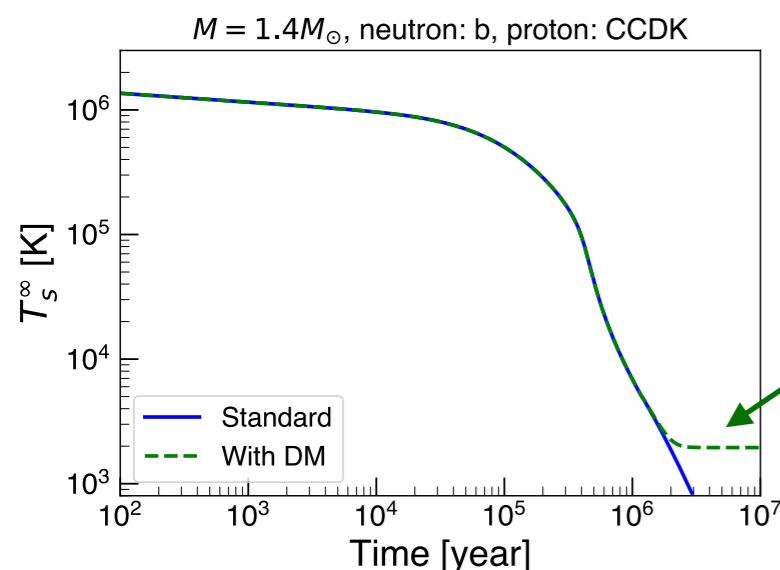
(for $\sigma > \sigma_{\text{th}}$)



$$T_s \simeq 2500 \text{ K}$$

Robust, smoking-gun prediction of DM heating.

Can we observe this??



NASA unveils first images from James Webb Space Telescope



By [Joel Achenbach](#)

Updated July 12, 2022 at 4:41 p.m. EDT | Published July 11, 2022 at 4:28 p.m. EDT

<https://www.washingtonpost.com/science/2022/07/11/nasa-james-webb-space-telescope-images/>

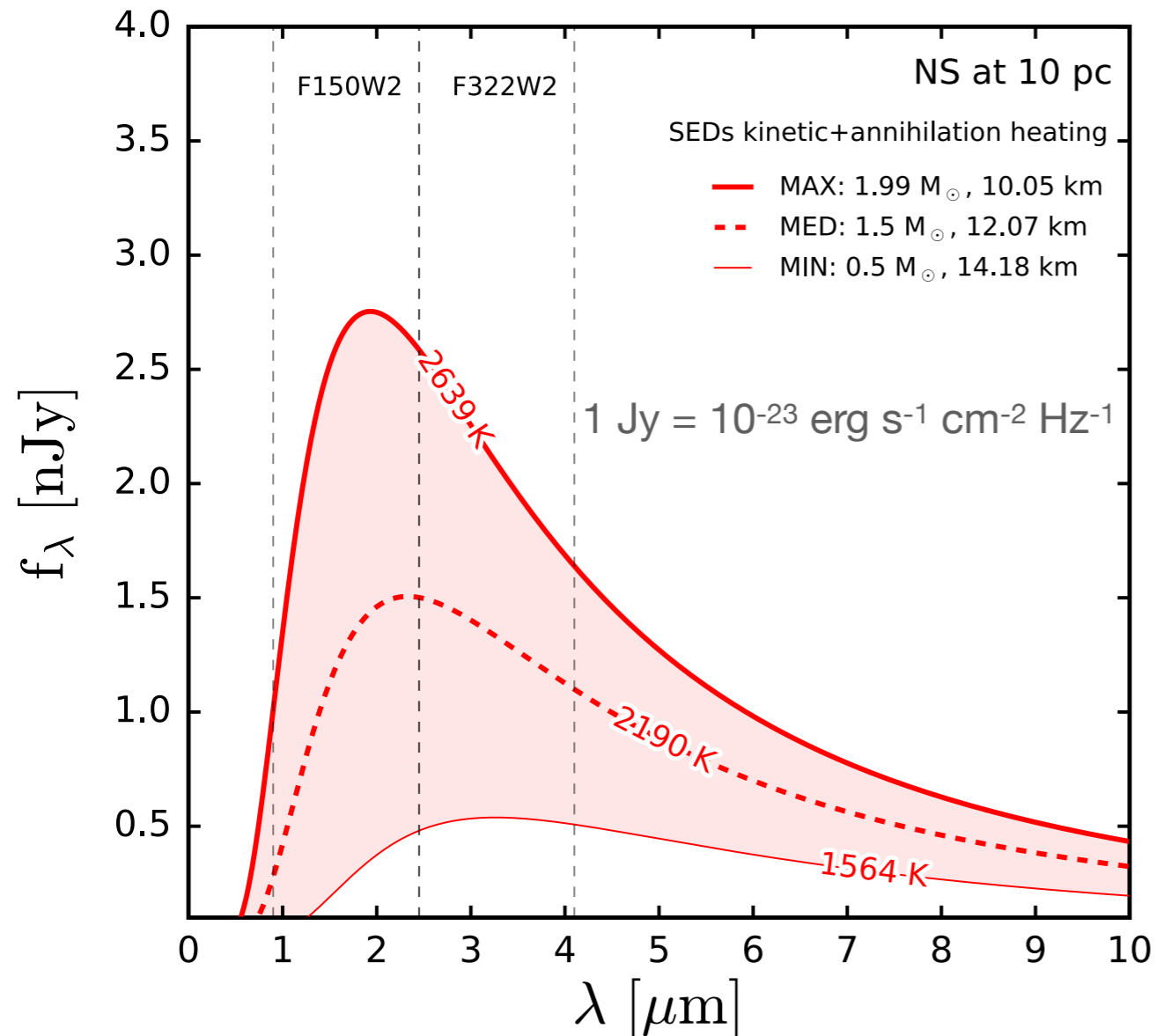


- ▶ Infrared space telescope.
- ▶ Succeed the Hubble Space Telescope.

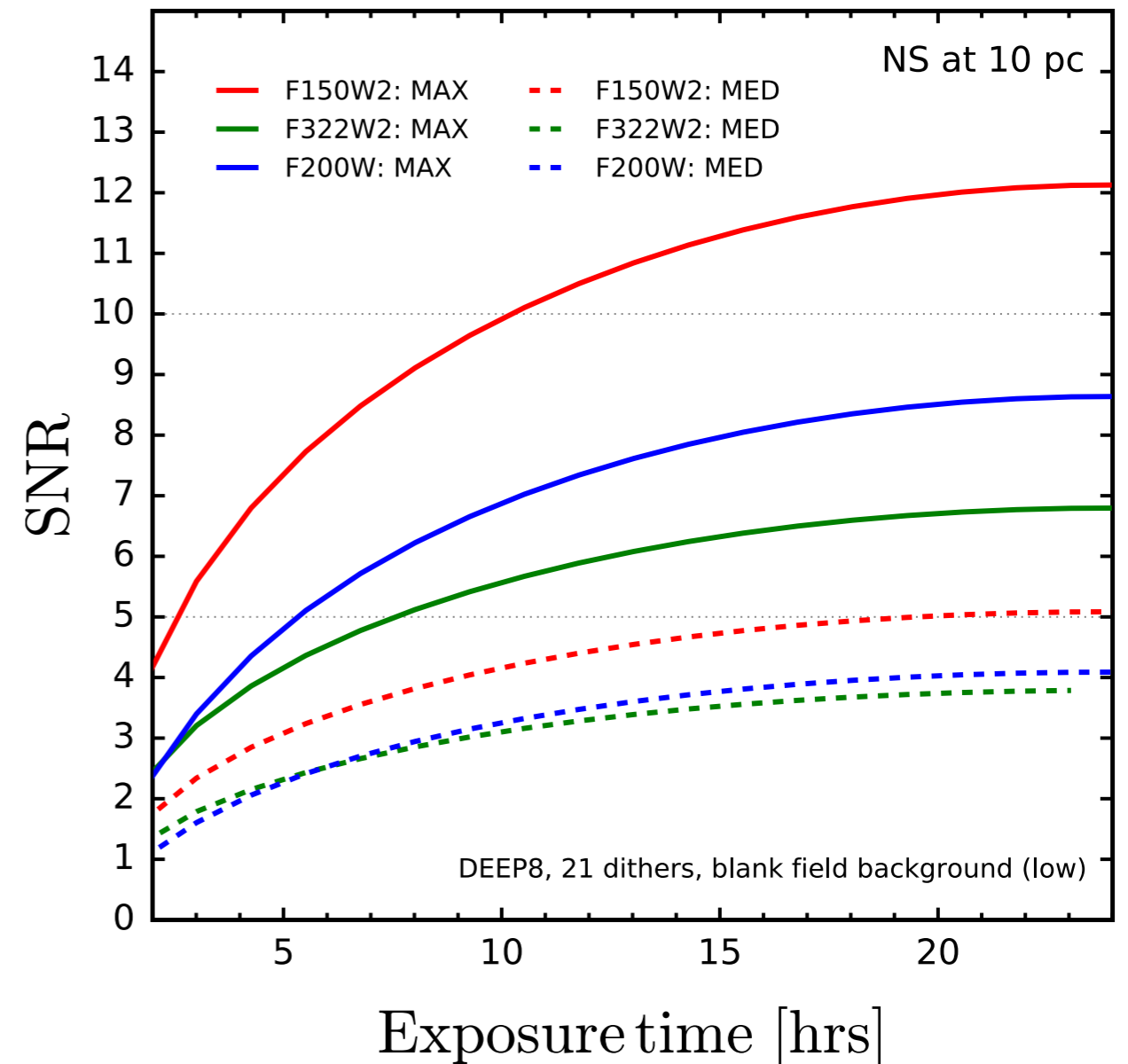
Spectrum, flux, and SNR

arXiv:2205.05048

Spectral distributions



Signal-to-noise ratio



- $\lambda \sim 2 \mu\text{m}$ \rightarrow Near-Infrared Camera (NIRCam) on JWST
- With the F150W2 filter, SNR $\gtrsim 5$ is obtained for 24 hours.

FAST

Many pulsars are expected to be discovered by

Five-hundred-meter Aperture Spherical radio Telescope (FAST)

(五百米口径球面射电望远镜)

in China in the near future.



- About 5000 (4000 new) pulsars are expected to be discovered.

arXiv: 1105.3794

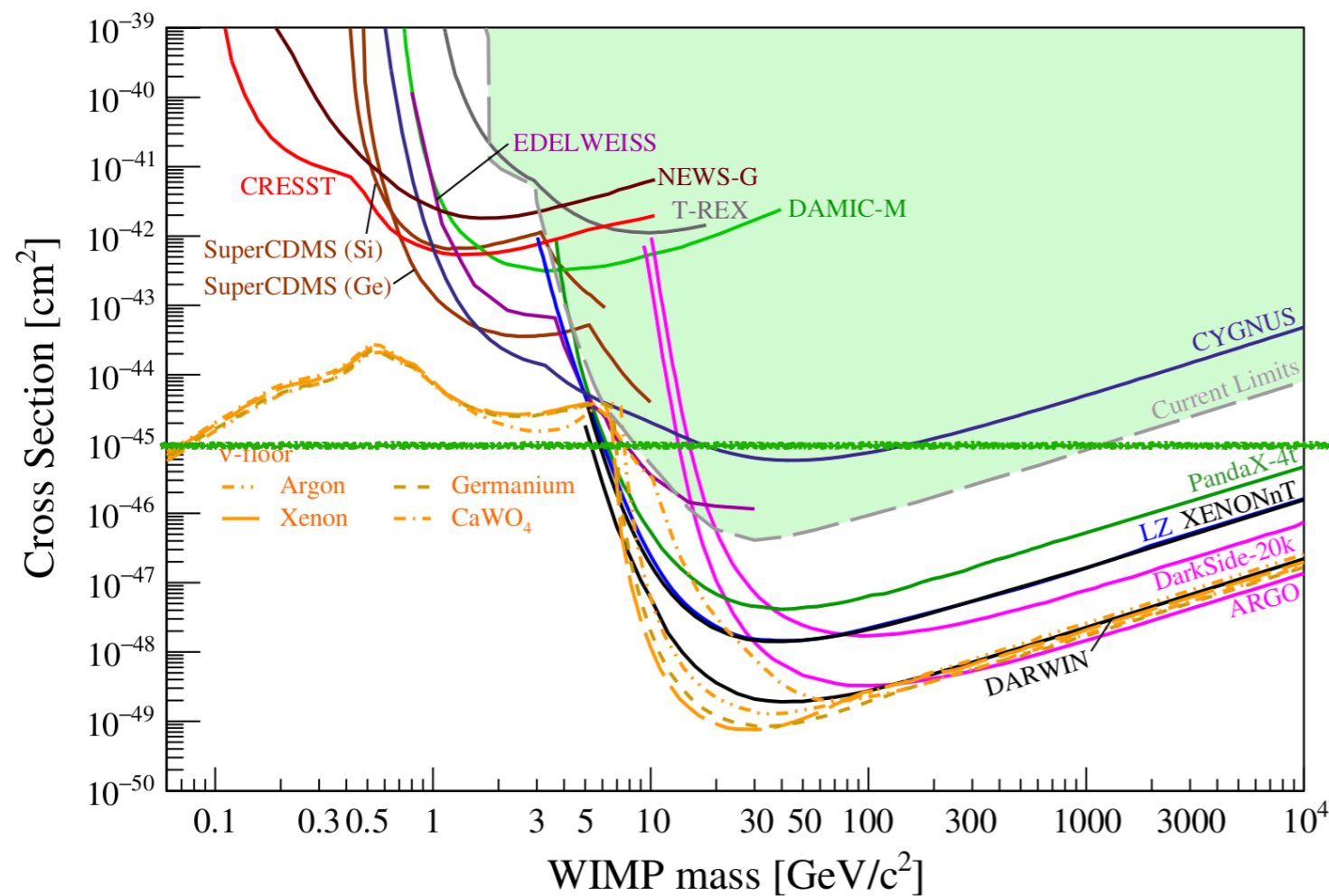
- A lot of pulsars have already been discovered.

See J. L. Han *et al.*, arXiv:2105.08460

DM heating vs direct detection

In any case, an observation of a NS with $T_s \lesssim 2 \times 10^3$ K disfavors WIMPs which have $\sigma_N \gtrsim 10^{-45} \text{ cm}^2$.

Prospects for direct detection experiments



$$\sigma_N = 10^{-45} \text{ cm}^2$$

APPEC Committee Report, [arXiv:2104.07634](https://arxiv.org/abs/2104.07634).

Such a large scattering cross section can be probed in **direct detection experiments**. Why we should care about DM heating??

Advantage of DM heating in NSs

Bound from NS temperature may surpass those from DM direct searches in the following cases:

- **Inelastic scattering** occurs for $\Delta M \lesssim \mathcal{O}(100)$ MeV.
- Dark matter interacts only with **leptons**.
- Heavy/light dark matter
- WIMP-nucleon scattering is velocity-suppressed.
- Spin-dependent scattering

Electroweak multiplet DM

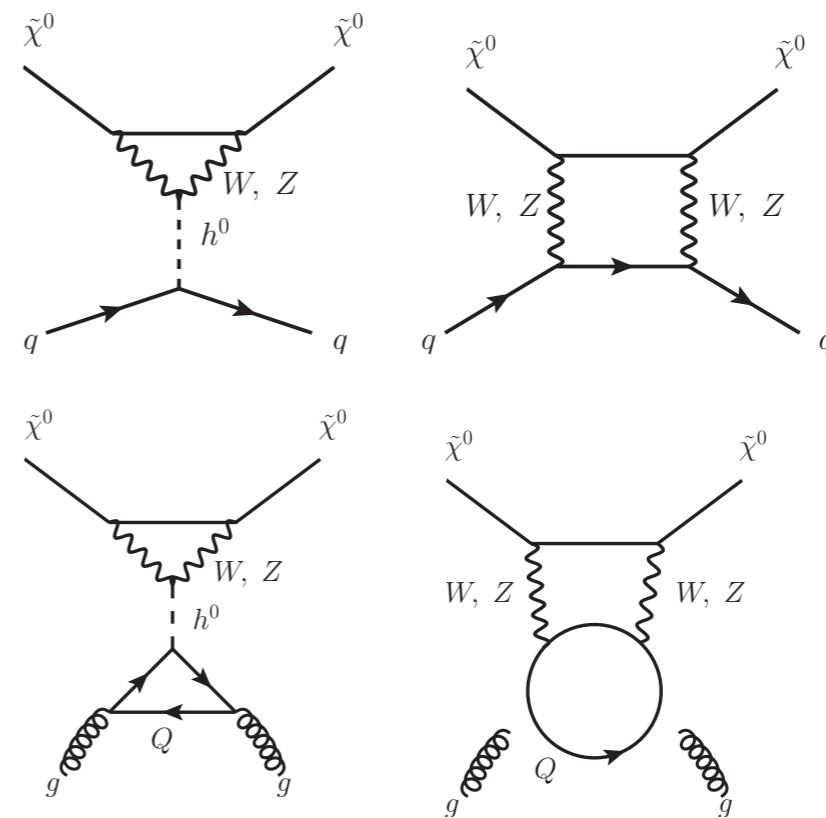
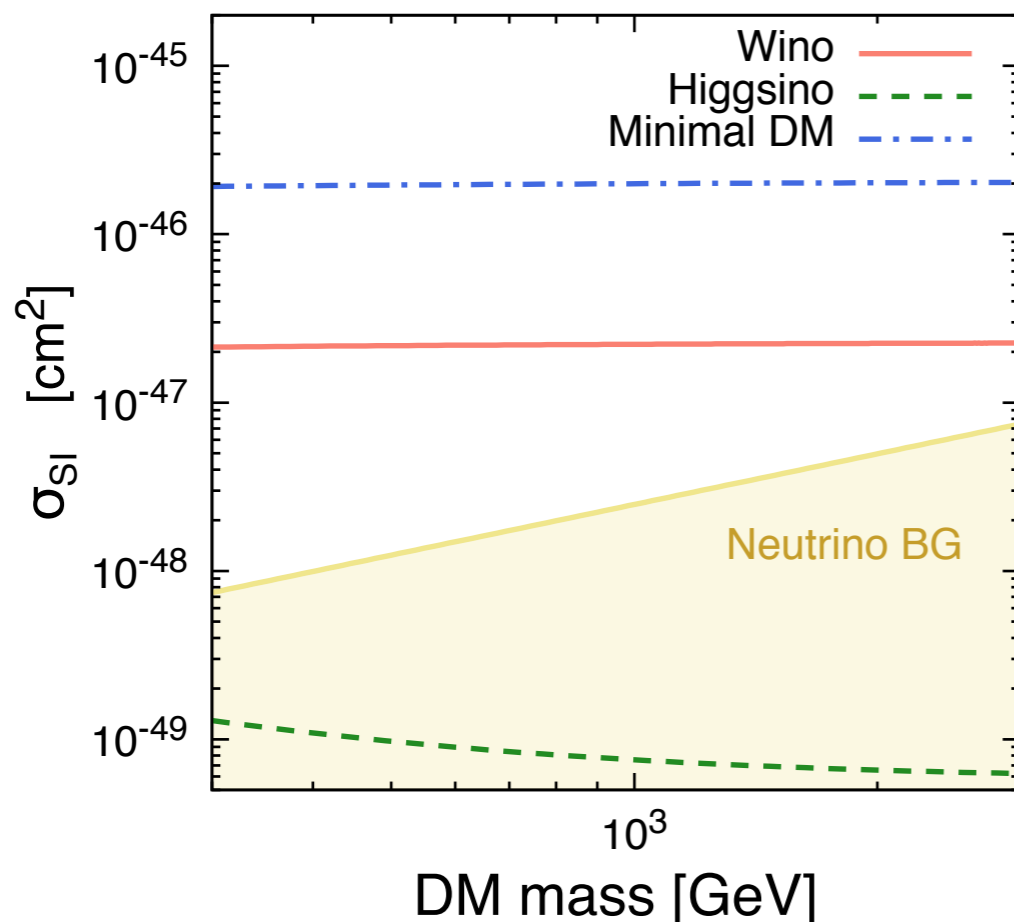
DM is **electrically neutral**. But, this does not fully determine its electroweak charges.



$$SU(2)_L \otimes U(1)_Y : (1,0), (2, \pm 1/2), (3,0), (3, \pm 1), \dots$$

Electroweak multiplet DM

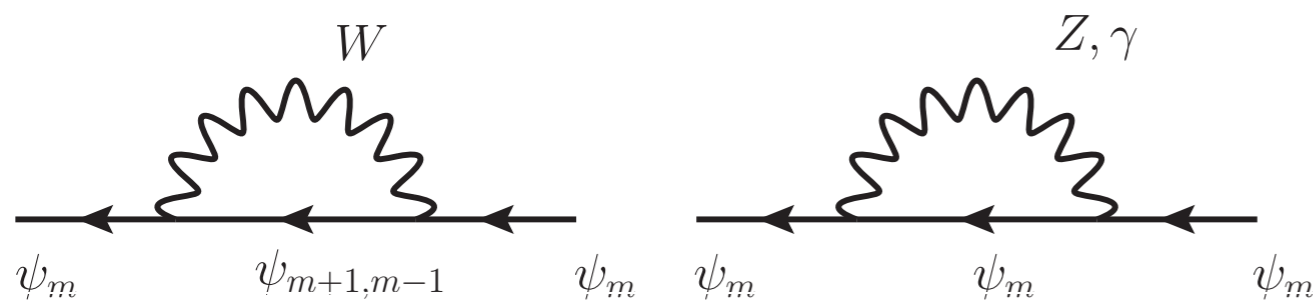
This class of DM has small DM-nucleon scattering cross section.



Electroweak multiplet DM

Electroweak multiplet DM is accompanied by **charged particles**, which are **degenerate in mass**.

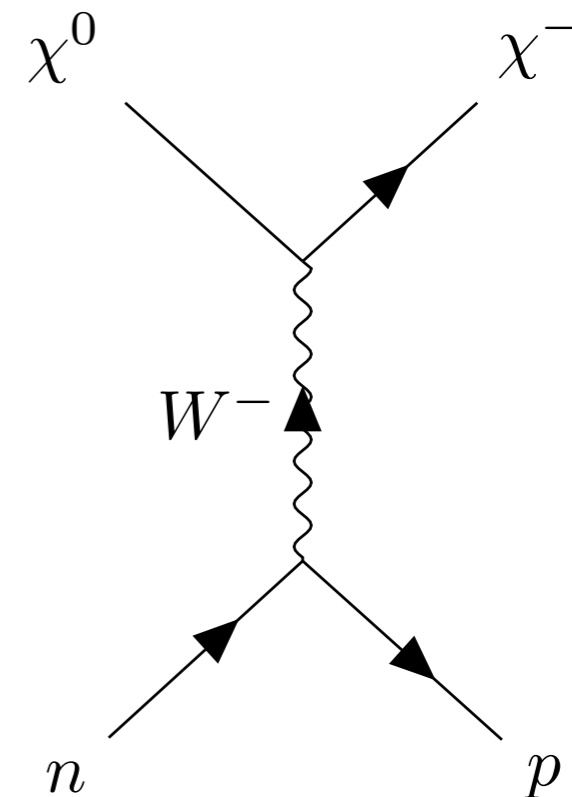
Mass splitting



$$\Delta M \simeq \alpha_2 m_W \sin^2 \frac{\theta_W}{2} + \alpha_2 Y m_W \left(\frac{1}{\cos \theta_W} - 1 \right)$$

O(100) MeV

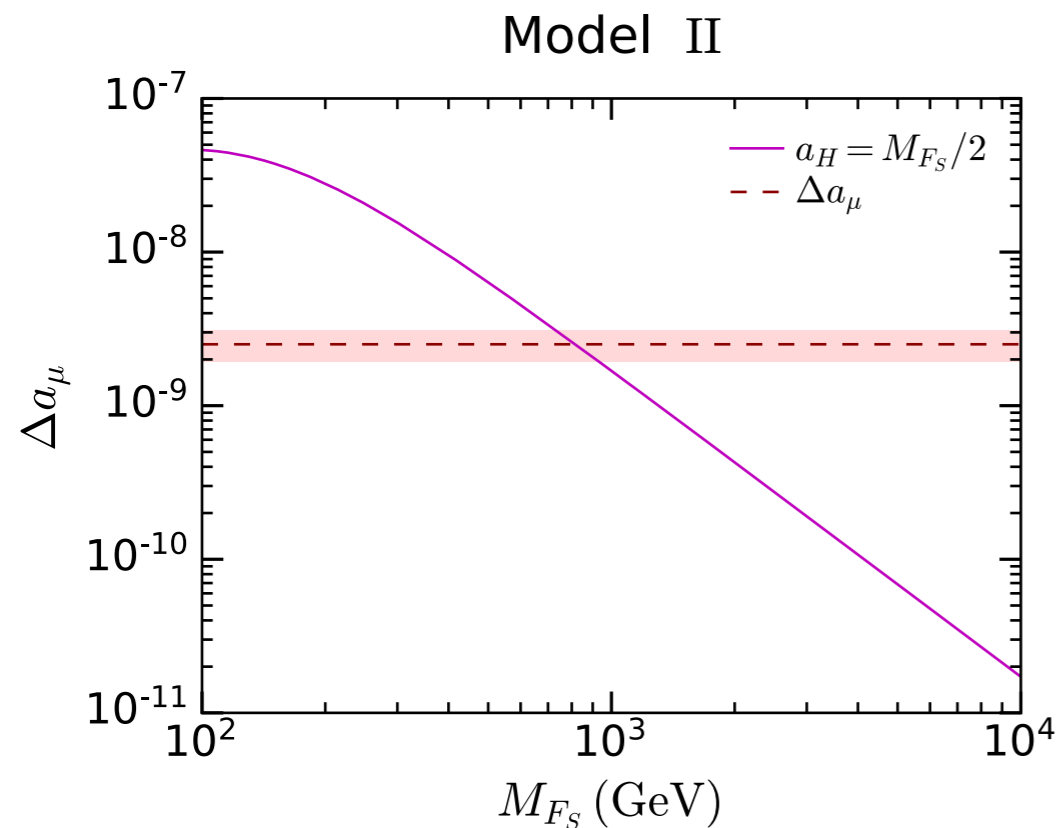
- **Inelastic scattering** can occur.
- Cross section is large enough for such a DM to be captured in NS.
- NS can be a promising probe for this class of DM candidates.



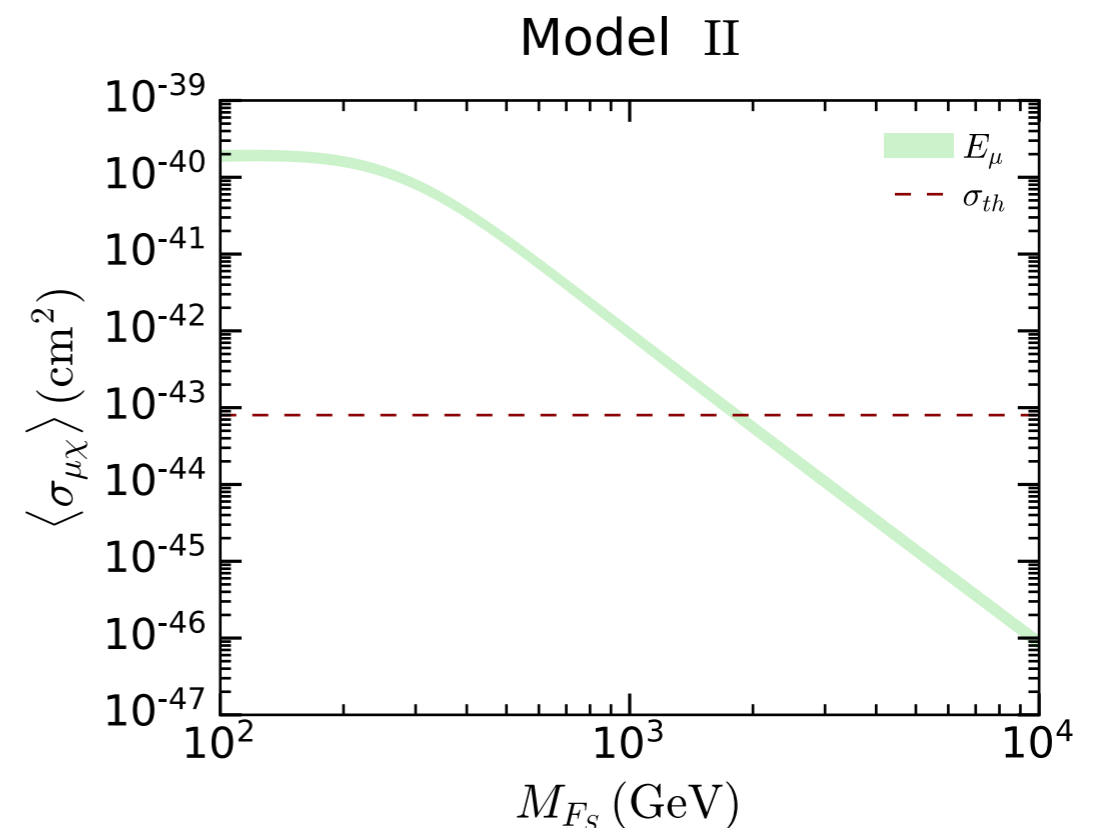
Muon $g-2$ and DM

NS heating can occur for DM models that couple only to leptons.

Muon $g-2$

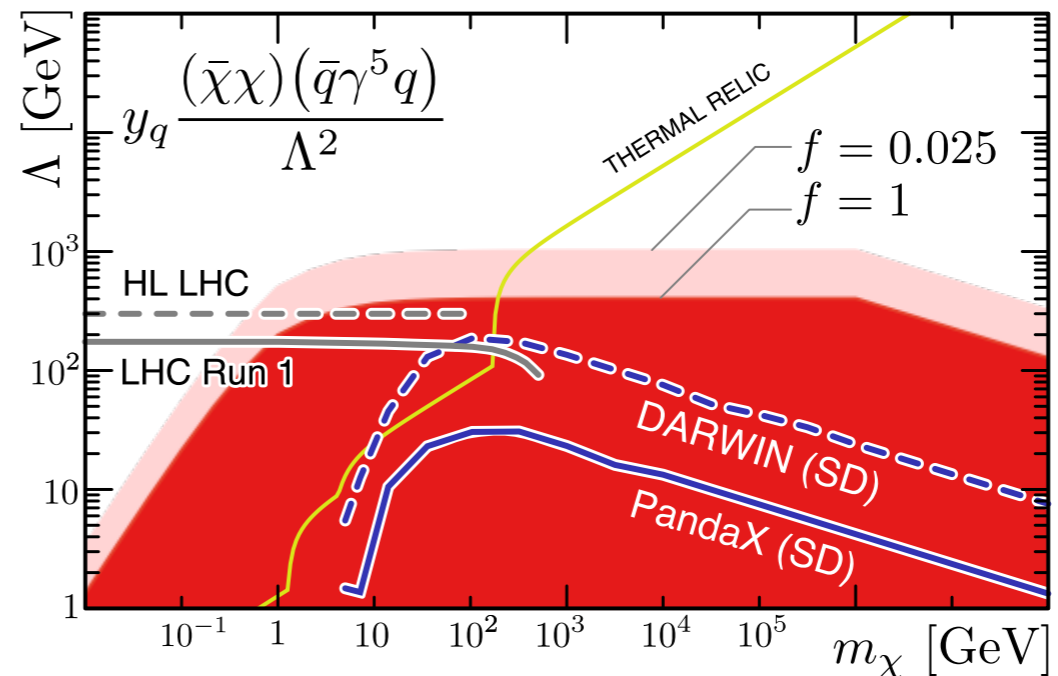
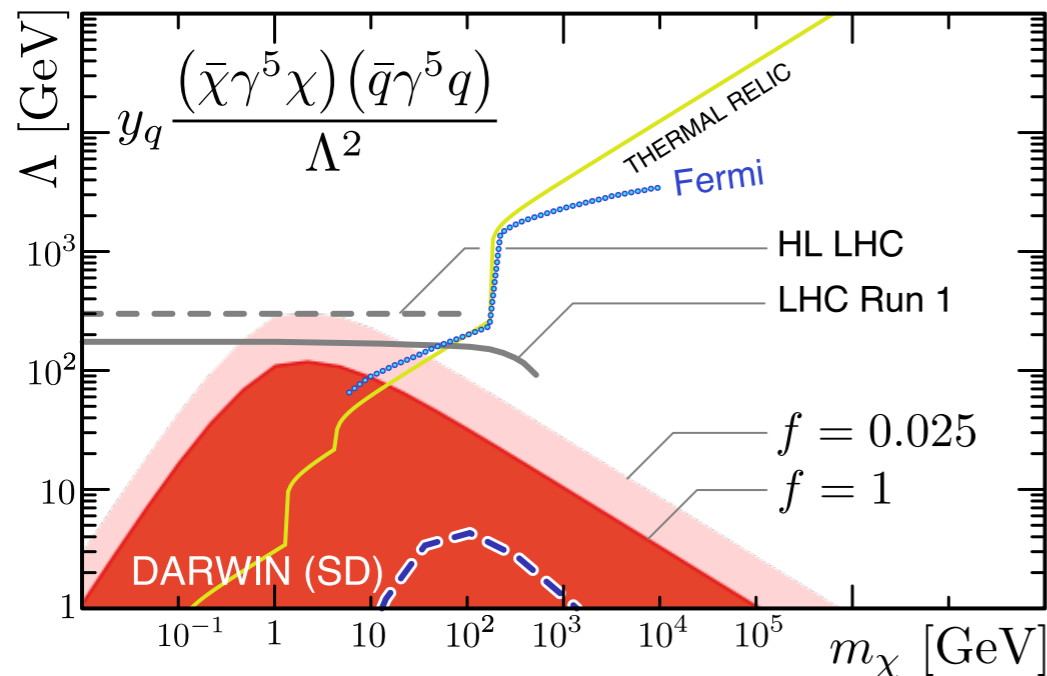
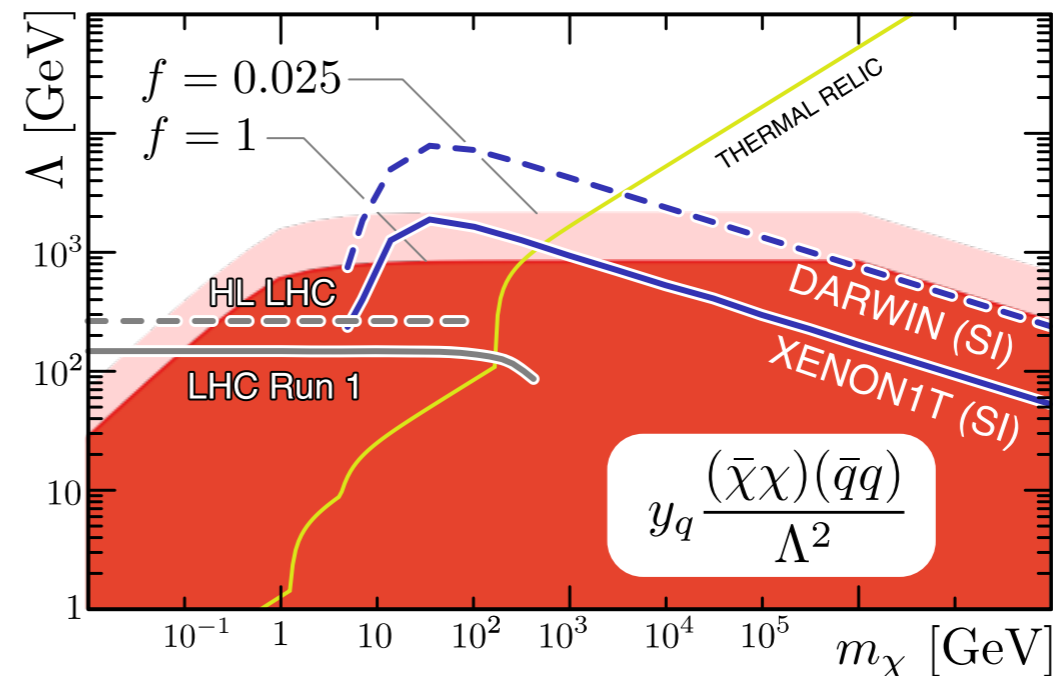
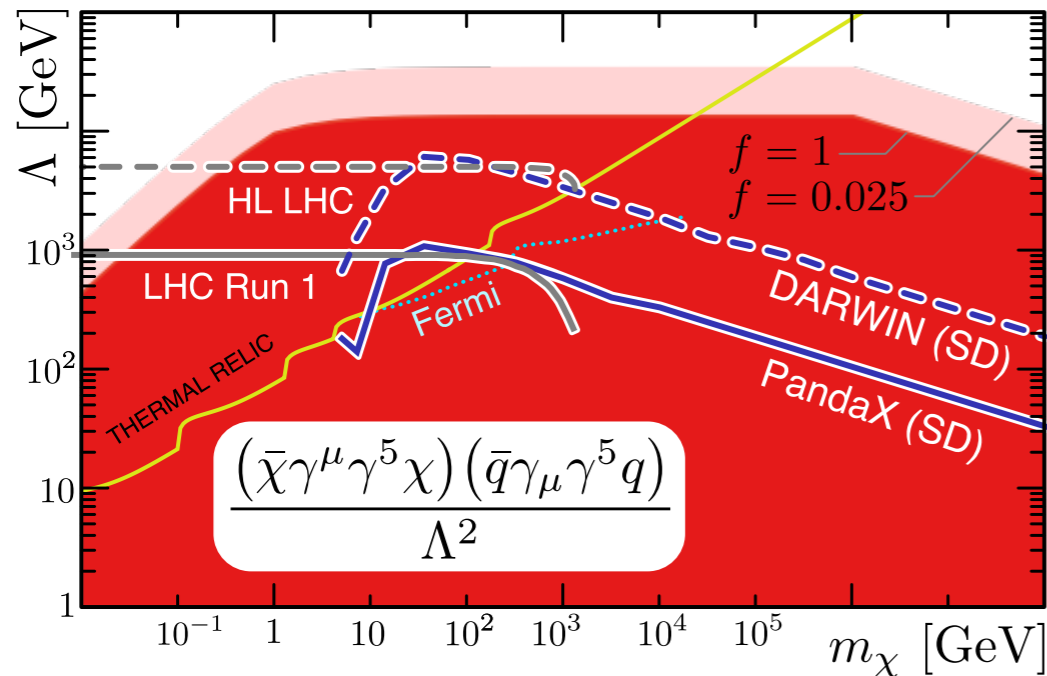


DM-muon scattering cross section

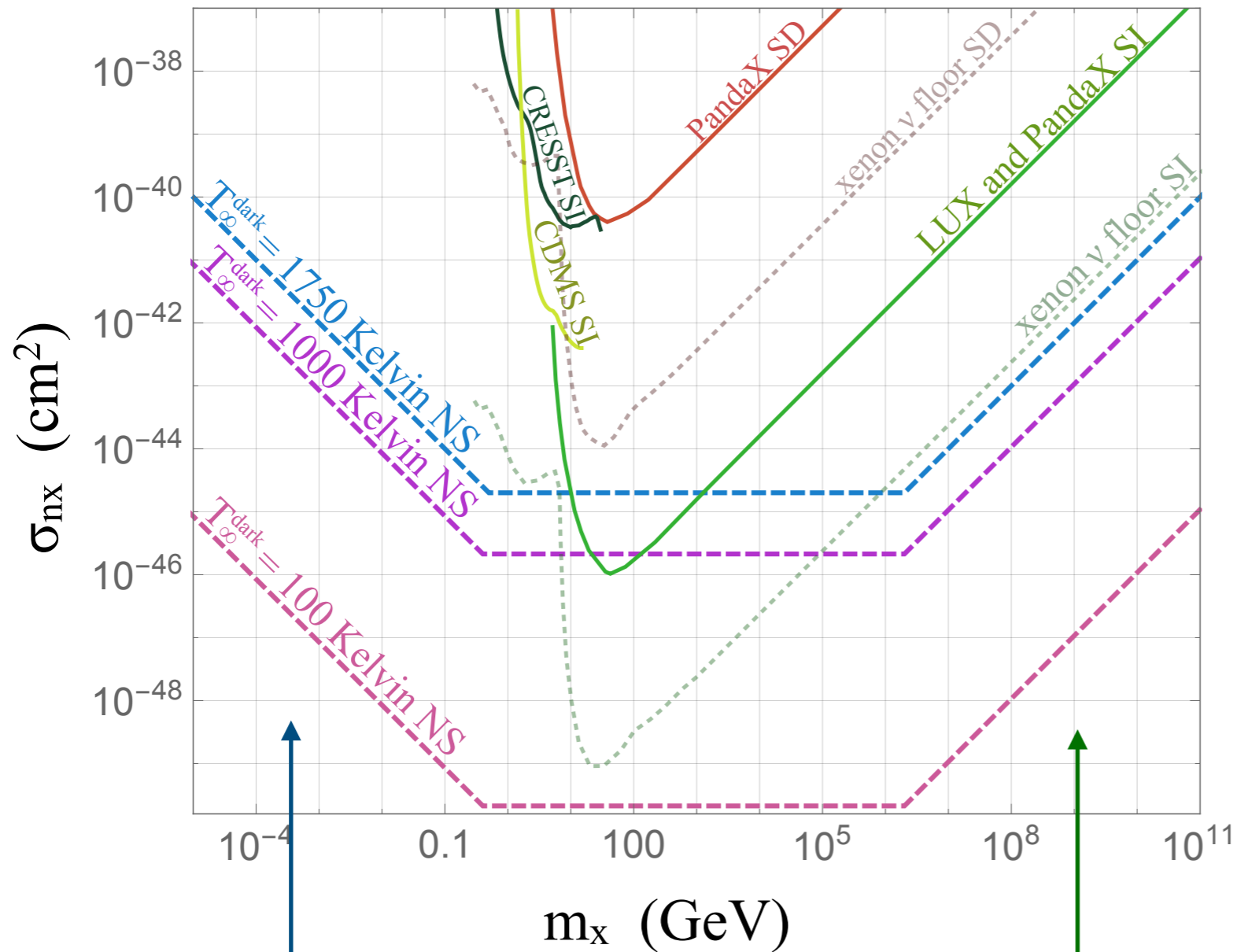


In the parameter regions where the **muon $g-2$ anomaly** is explained, DM-muon scattering is sufficiently large.

Effective operator analysis



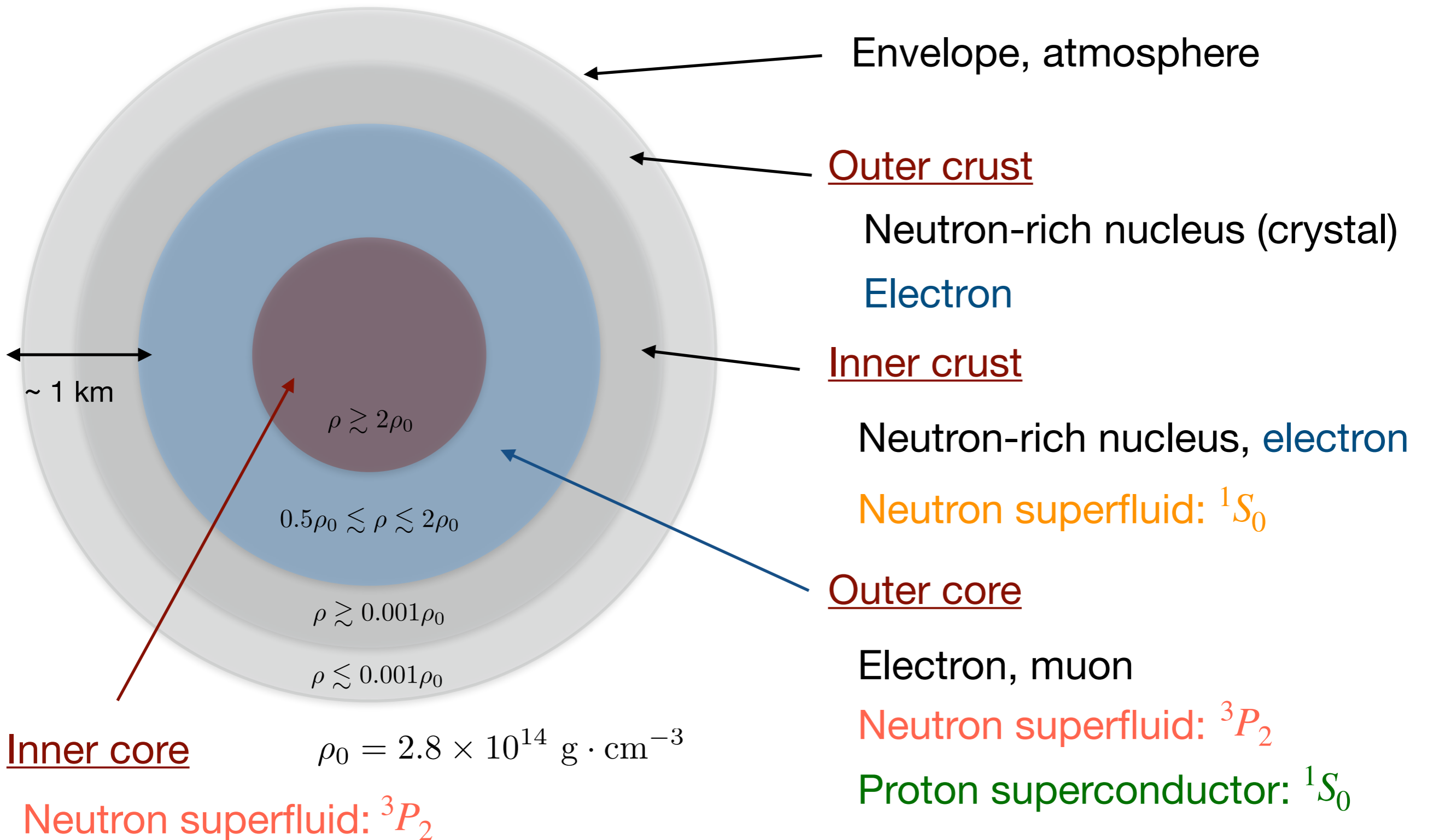
Dark kinetic heating



Effect of Pauli blocking

Multiple scattering required

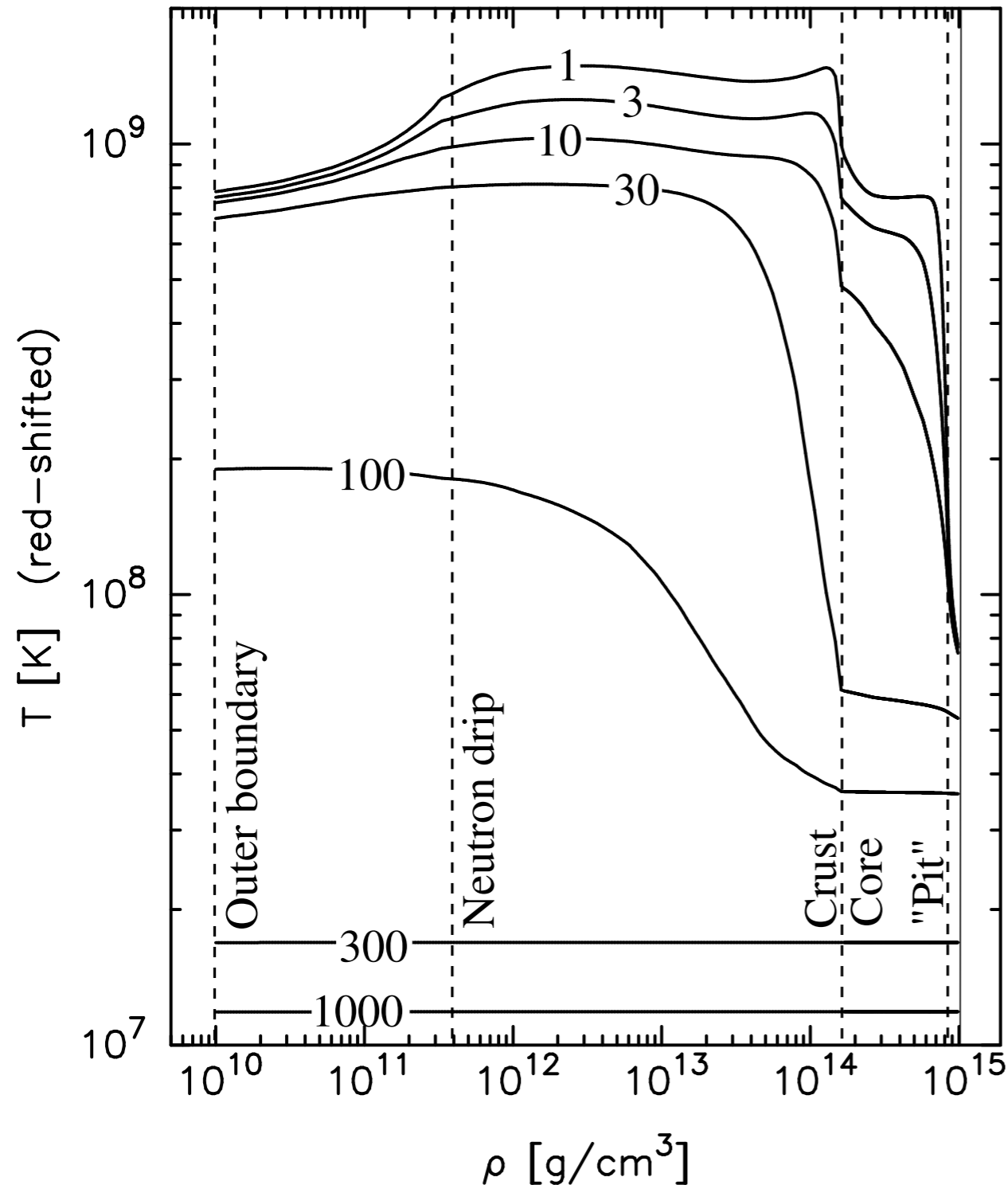
Neutron star structure



~~Hyperons, π /K condensation, quarks (?)~~

We do not consider them in this talk.

Temperature distribution



Relaxation in the Core
done in ~ 100 years.

Name: Urca

APRIL 1, 1941

PHYSICAL REVIEW

VOLUME 59

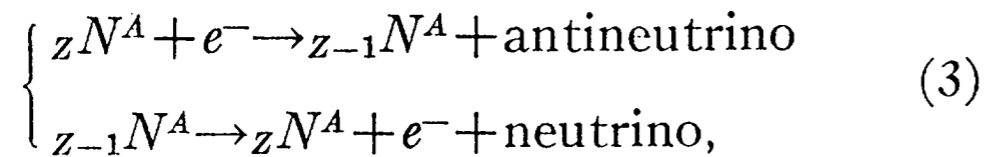
Neutrino Theory of Stellar Collapse

G. GAMOW, *George Washington University, Washington, D. C.*

M. SCHOENBERG,* *University of São Paulo, São Paulo, Brazil*

(Received February 6, 1941)

of β -particles. In fact, when the temperature and density in the interior of a contracting star reach certain values depending on the kind of nuclei involved, we should expect processes of the type



which we shall call, for brevity, “urca-processes.”

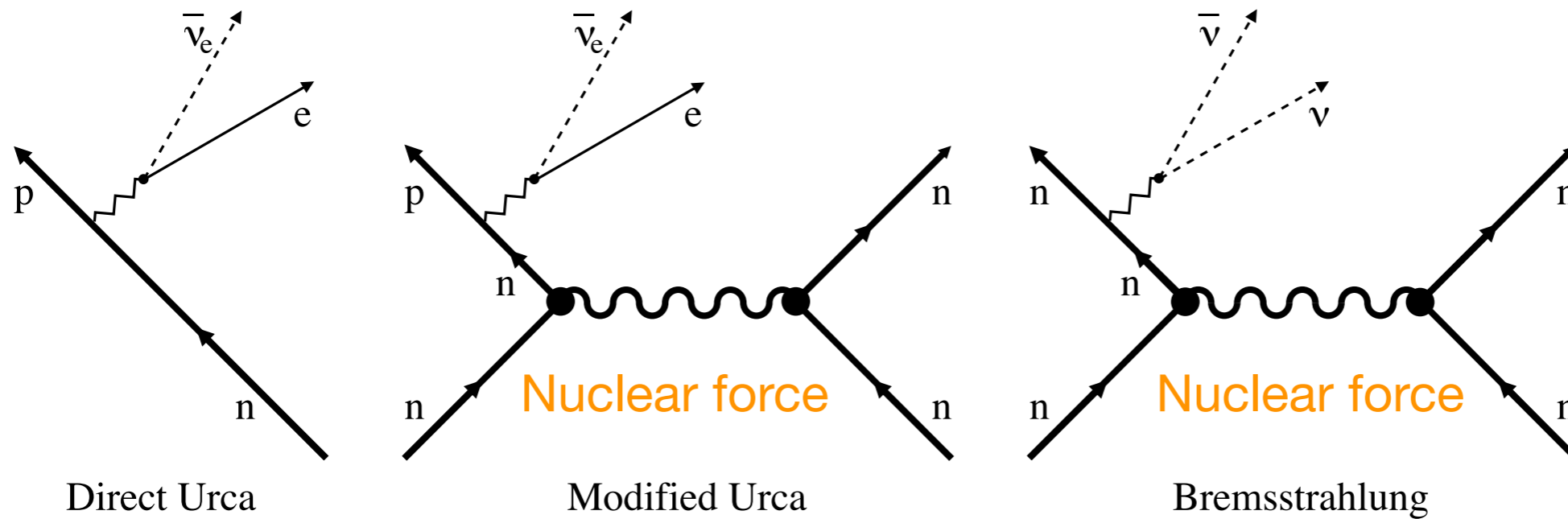
Named after a casino in
Rio de Janeiro:

Cassino da Urca

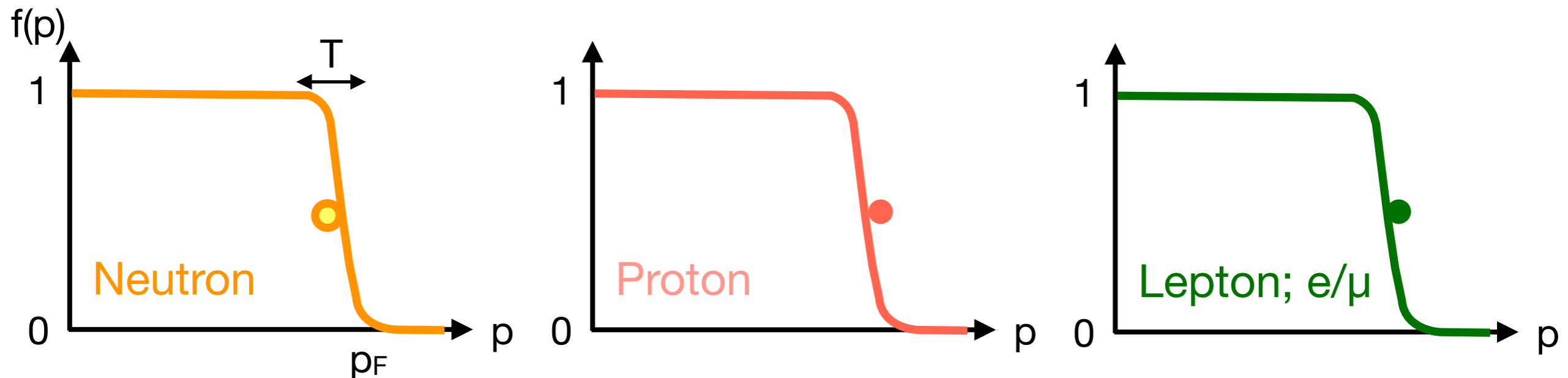
- ▶ To commemorate the casino where they first met.
- ▶ Rapid disappearance of energy (money) of a star (gambler).
- ▶ **UnRecordable Cooling Agent.**
- ▶ “Urca” means “thief” in Russian.

Neutrino emission

First we consider the processes that occur without superfluidity.



These processes occur only near the **Fermi surface**.



β equilibrium

Inside neutron stars, β equilibrium is achieved via the direct/modified Urca reactions

Chemical equilibrium

$$\mu_e + \mu_p = \mu_n$$

Chemical potential of neutrino is zero since it can escape from neutron star.

Charge neutrality

$$n_p = n_e$$

Muons also appear in the region where $\mu_e > m_\mu$.

Chemical equilibrium

$$\mu_e = \mu_\mu \quad (\mu_\mu + \mu_p = \mu_n)$$

Charge neutrality

$$n_p = n_e + n_\mu$$

Direct Urca

Emissivity \equiv energy loss per volume per time.

of the direct Urca process is given by

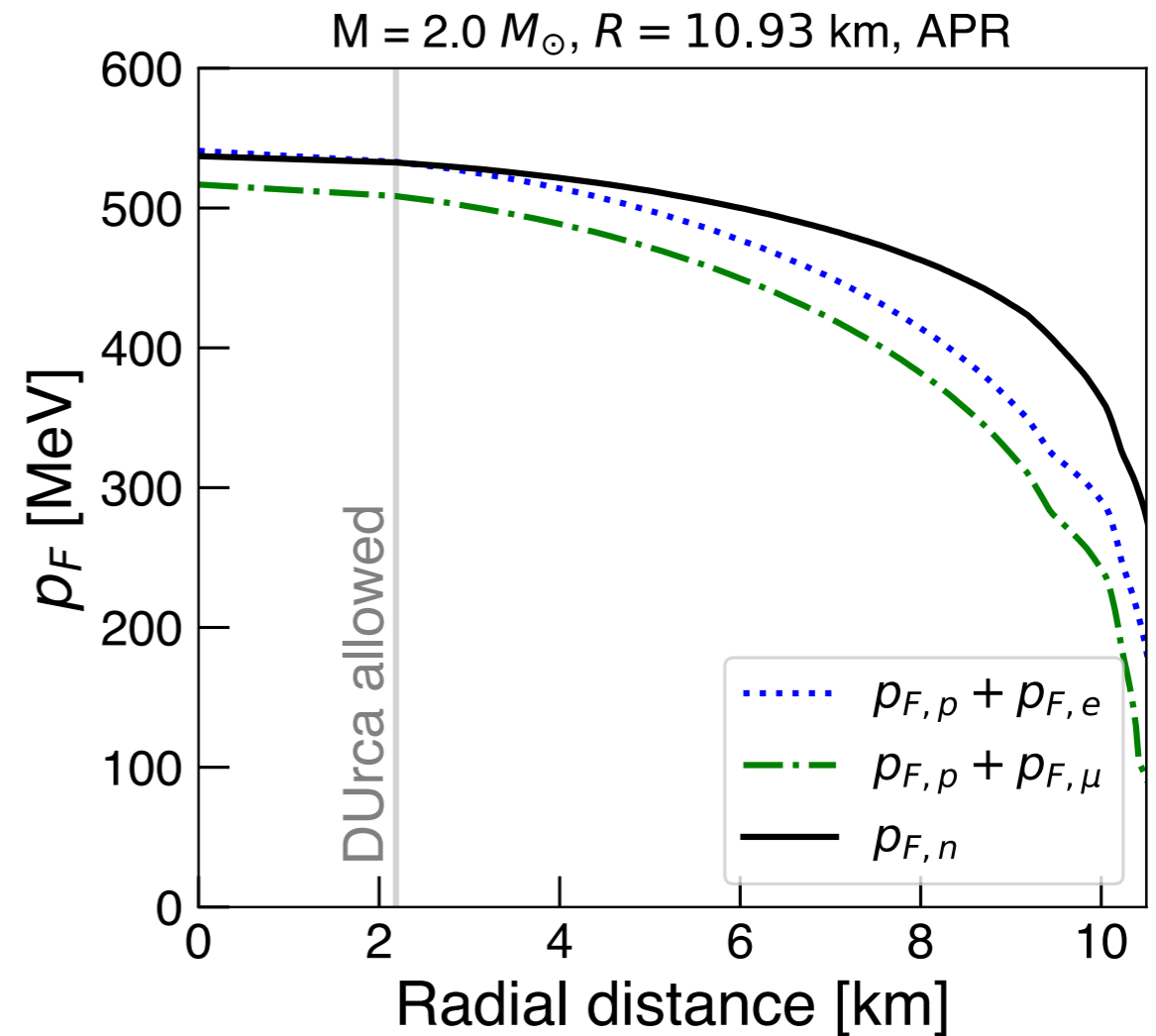
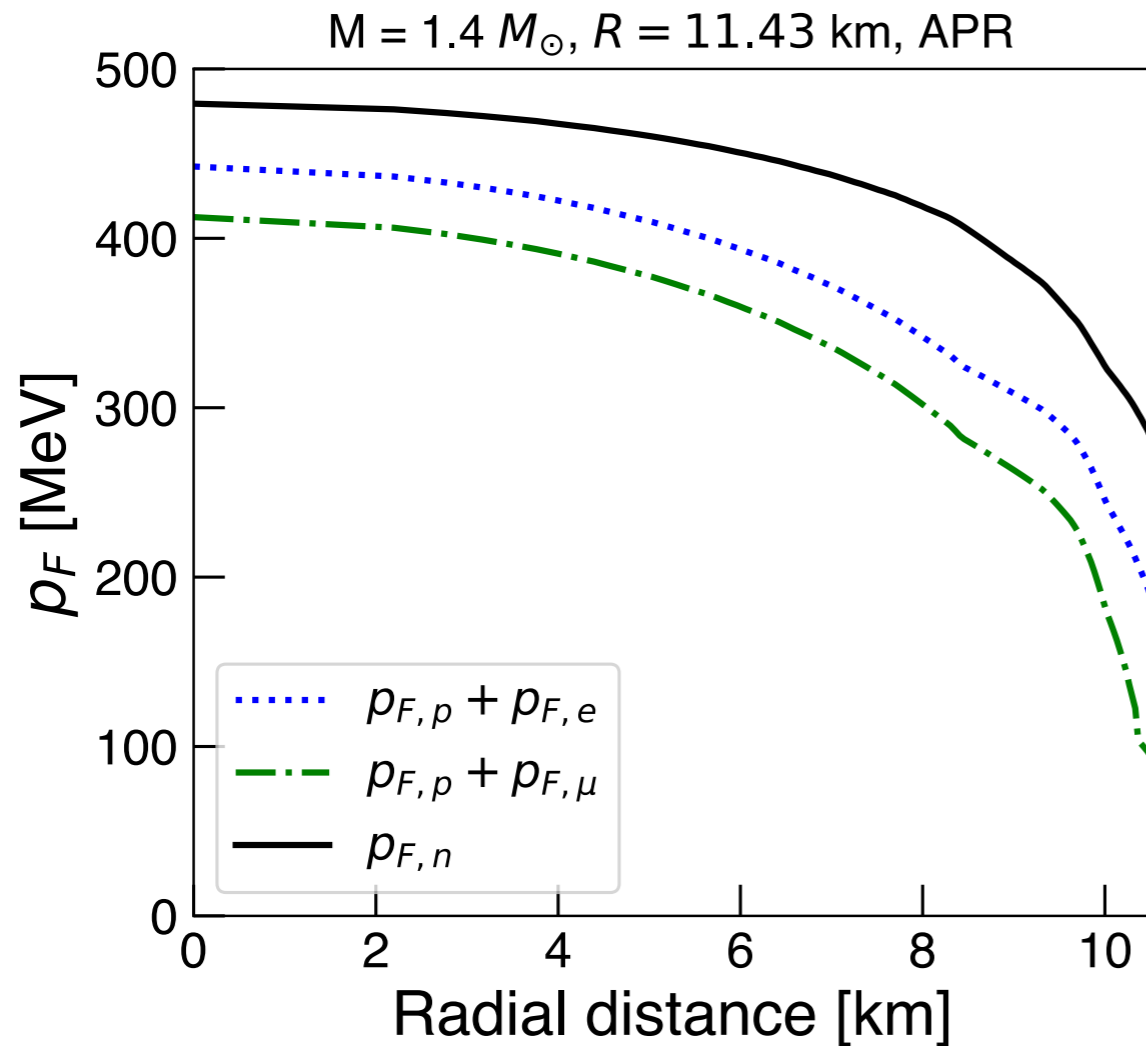
$$Q_D = \frac{457\pi}{10080} G_F^2 V_{ud}^2 (1 + 3g_A^2) m_{*,n} m_{*,p} m_{*,e} T^6 \Theta(p_{F,p} + p_{F,e} - p_{F,n})$$
$$\simeq 4 \times 10^{27} \times \left(\frac{T}{10^9 \text{ K}} \right)^6 \Theta(p_{F,p} + p_{F,e} - p_{F,n}) \text{ erg} \cdot \text{cm}^{-3} \cdot \text{s}^{-1}$$

- The step function comes from the **momentum conservation**.

$$p_{F,p} + p_{F,e} > p_{F,n}$$

- Direct Urca is the dominant process, **if it occurs**.

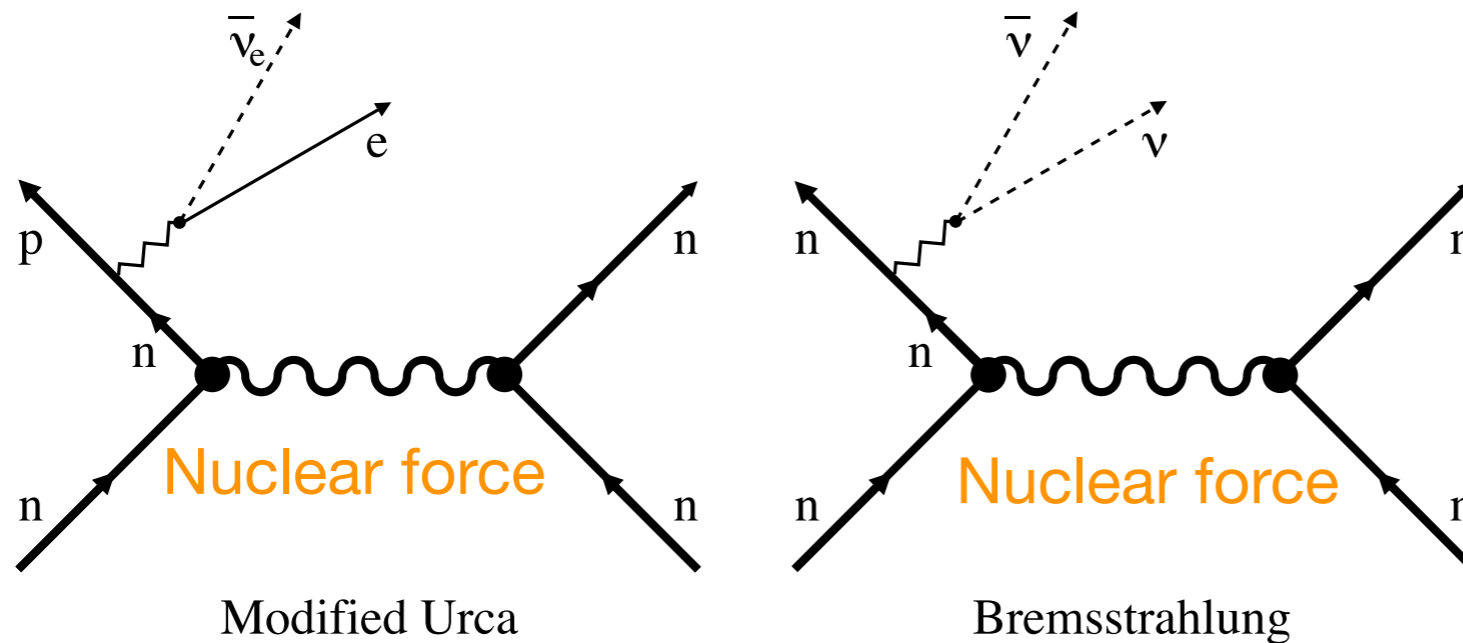
Direct Urca condition



- Direct Urca can occur only in the **high density region**.
- It can occur only in relatively heavy stars.

For the APR equation of state, $M \gtrsim 1.97 M_{\odot}$

Modified Urca/bremsstrahlung



If Direct Urca does not operate, **Modified Urca/bremsstrahlung processes** become dominant.

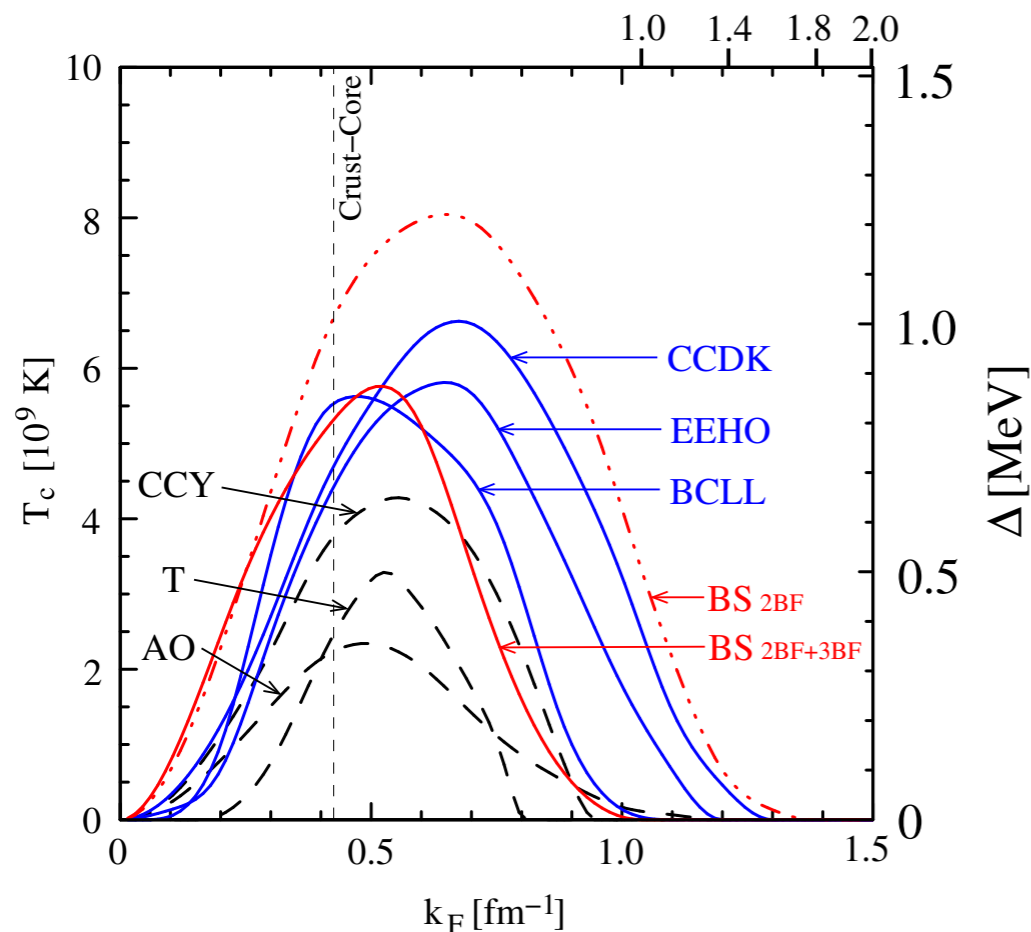
Momentum exchange with a spectator allows these processes to satisfy the momentum conservation.

Nucleon pairing

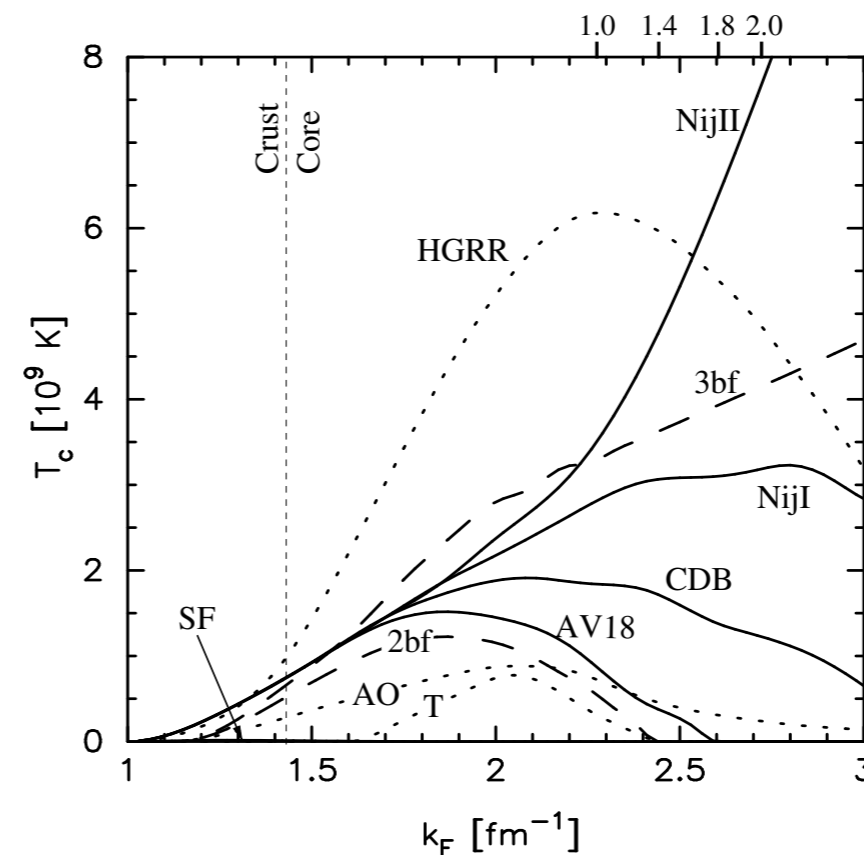
Nucleons in a NS form pairings below their critical temperatures:

- ▶ Neutron singlet 1S_0 ← Only in the crust. Less important.
- ▶ Proton singlet 1S_0 } ← Form in the core. Important.
- ▶ Neutron triplet 3P_2 }

Proton singlet pairing gap



Neutron triplet pairing gap



Effects of nucleon pairings

Nucleons in a NS form **Cooper pairings**.

Energy spectrum

$$\epsilon_N(\mathbf{p}) \simeq \sqrt{\Delta_N^2 + v_{F,N}^2 (p - p_{F,N})^2}$$

Δ_N : pairing gap

The **pairing gap** introduces a suppression factor to

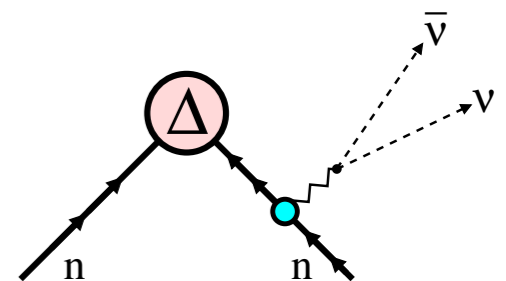
▶ **Neutrino emission processes**

▶ **Heat capacity**

$$\propto e^{-\frac{\Delta_N}{T}}$$

In addition, a new neutrino emission process is turned on:

▶ **Pair-breaking and formation (PBF) process**



PBF process

Thermal disturbance induces the **breaking** of nucleon pairs.

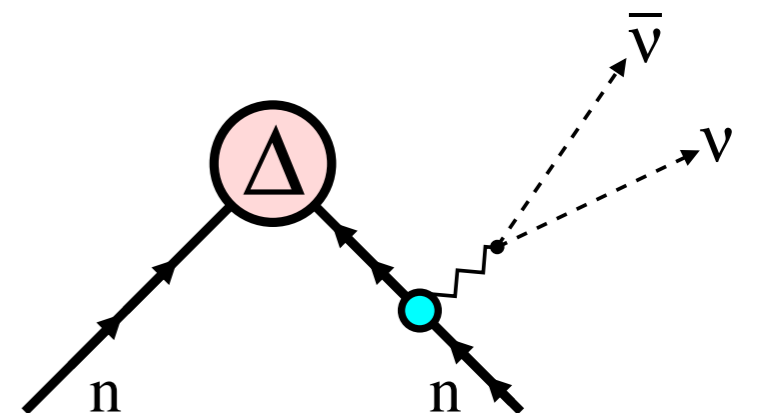


During the **reformation** of cooper pairs, the **gap energy** is released via **neutrino emission**.

This process significantly **enhances** the neutrino emission only when

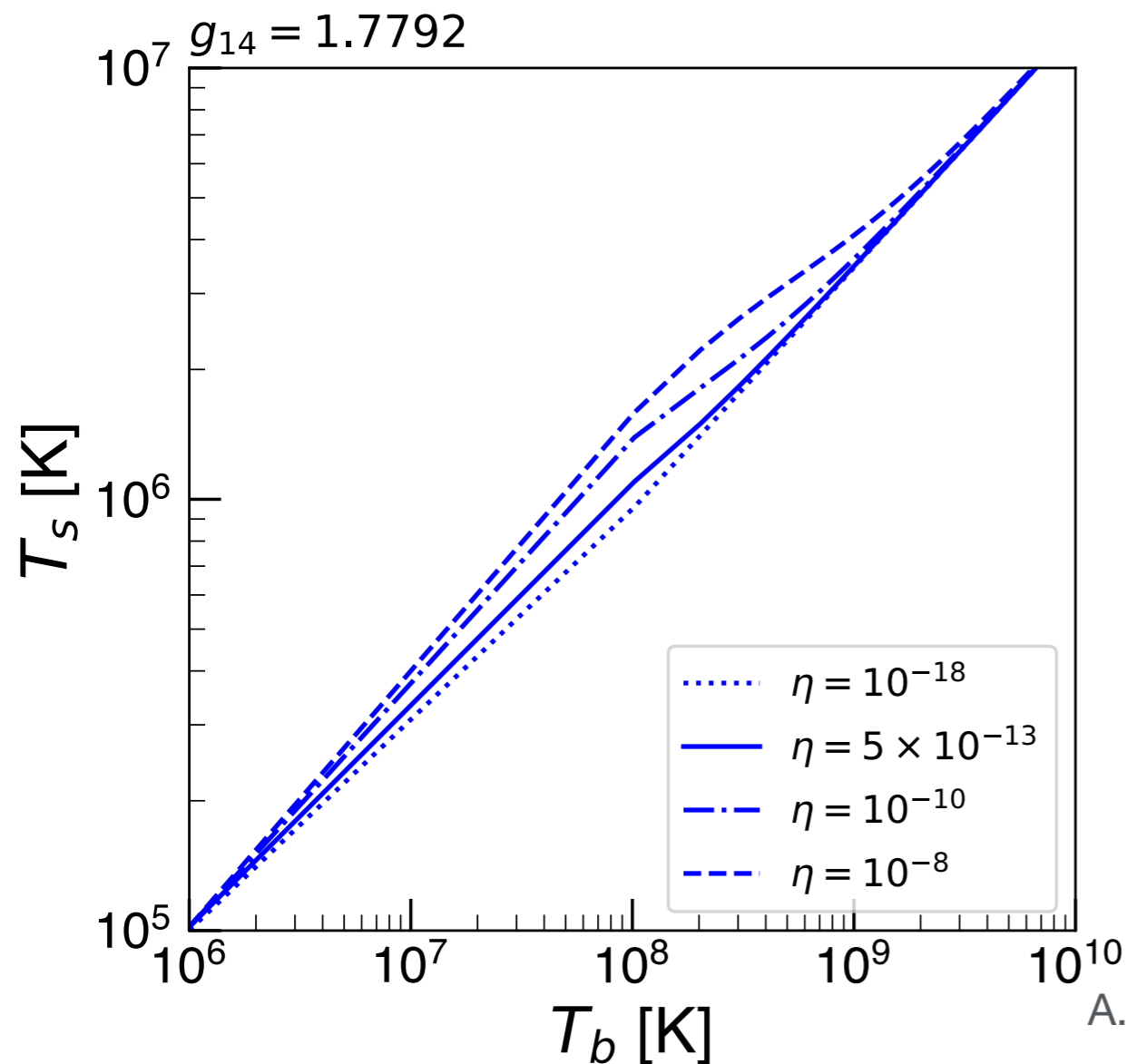
$$T \lesssim T_C$$

- If $T > T_C$, this process does not occur.
- If $T \ll T_C$, pair breaking rarely occurs.



Surface temperature

It is the **surface temperature** that we observe, so we need to relate it to the **internal temperature**.



This relation depends on the amount of **light elements** in the envelope.

$$\eta \equiv g_{14}^2 \Delta M / M$$

g_{14} : surface gravity in units of $10^{14} \text{ cm s}^{-2}$.
 ΔM : mass of light elements.

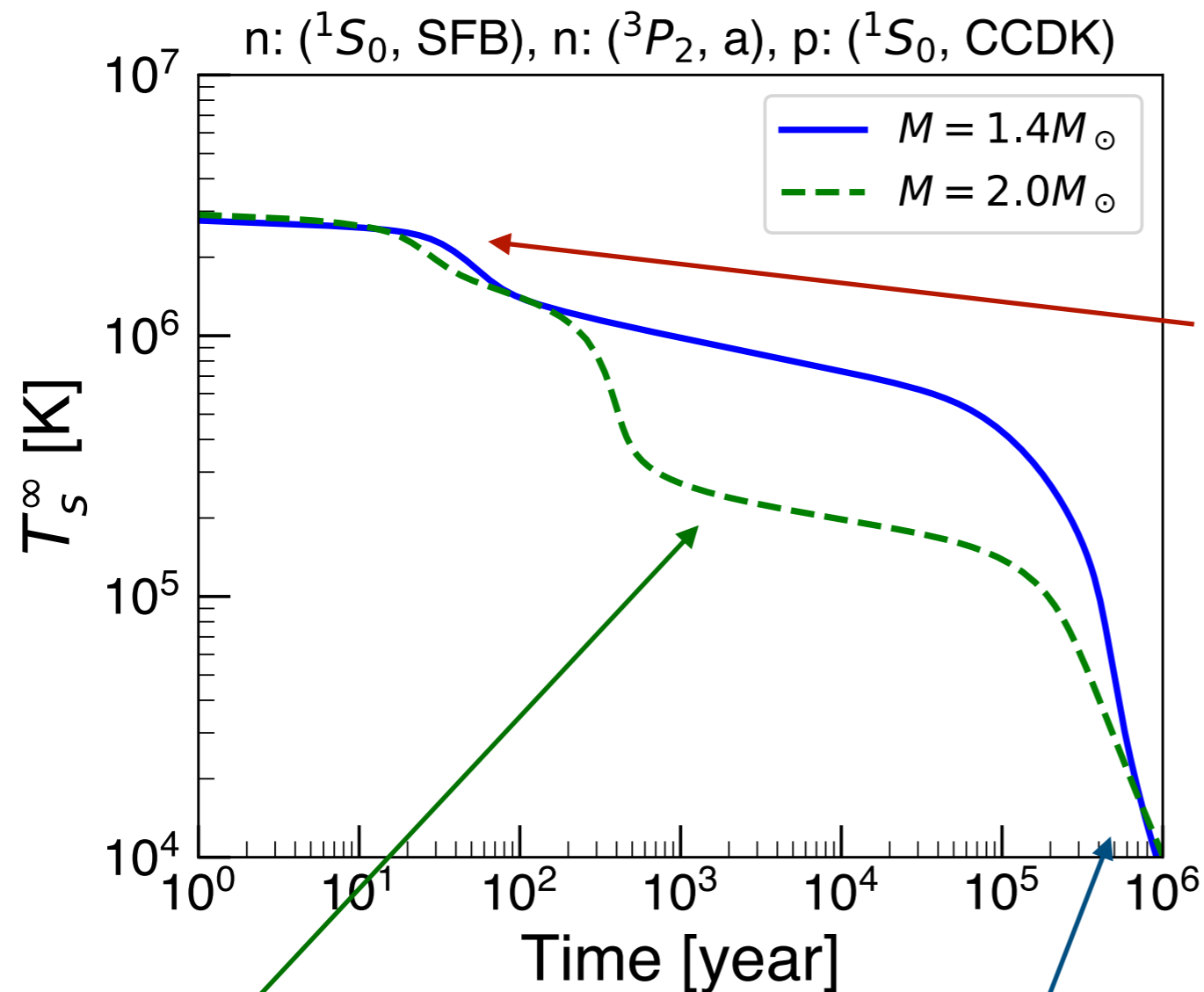
A. Y. Potekhin, G. Chabrier, and D. G. Yakovlev, A&A **323**, 415 (1997).

As the amount of light elements gets increased, the surface temperature becomes larger.

Light elements have large thermal conductivities.

Temperature evolution

We can now solve the equation for temperature evolution:



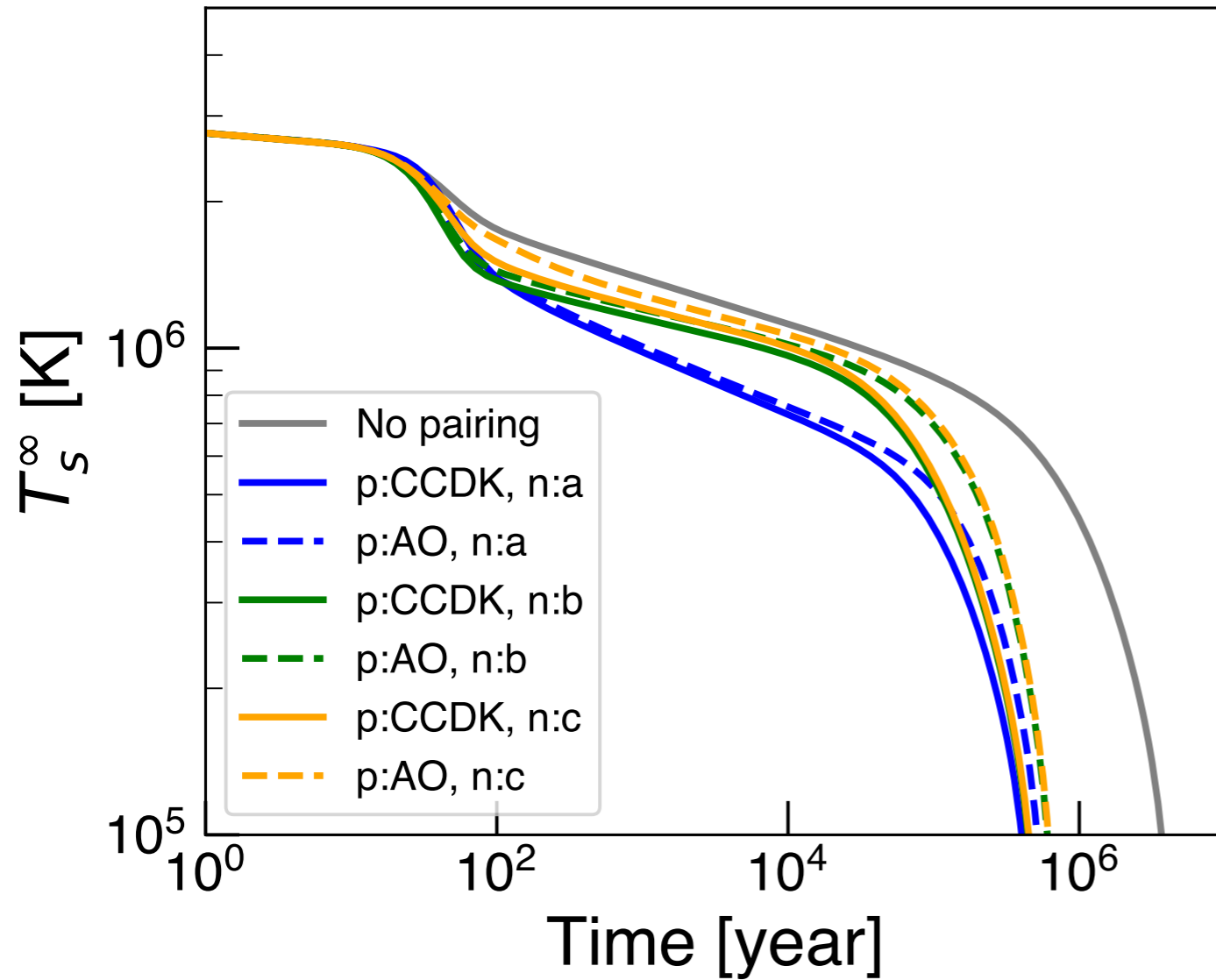
Before the thermal relaxation completed, the surface temperature does not follow the internal temperature.

If **Direct Urca occurs**, the neutron star cools down rapidly.

Temperature of NSs (older than **10^6 years**) is very low.

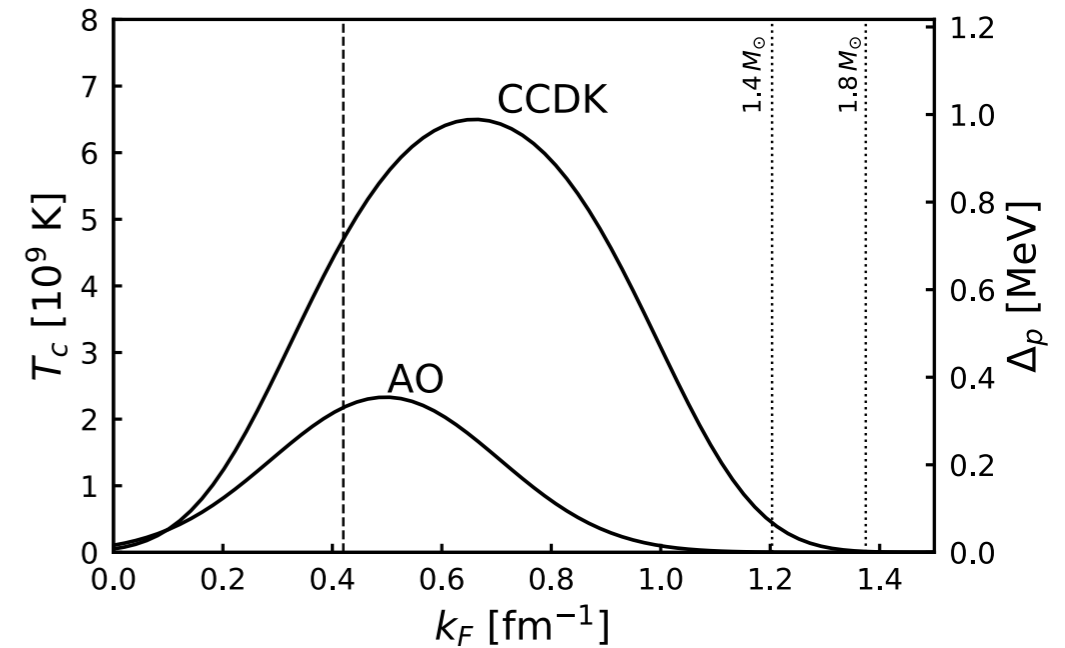
Temperature evolution (gap dependence)

$M = 1.4M_{\odot}$

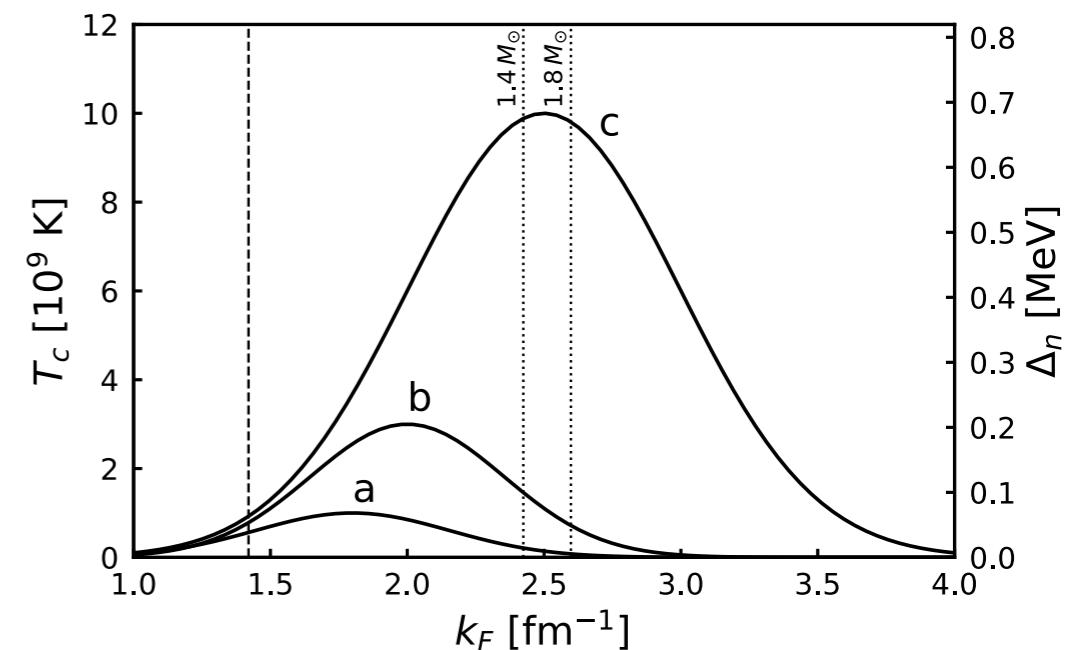


Uncertainty in nucleon gap models lead to the theoretical errors in the cooling calculation.

Proton singlet gap



Neutron triplet gap



Challenge for standard cooling

On the other hand, there is an example of **old cool neutron star**.

▶ J2144-3933: $t_{\text{sd}} = 3.33 \times 10^8$ years, $T_s^\infty < 4.2 \times 10^4$ K

S. Guillot, *et al.*, *Astrophys. J.* **874**, 175 (2019).

Is there any theory that can explain these observations on the equal footing??

Out of β equilibrium

The excess of energy is dissipated by

► Increase of **neutrino emission**

► Generation of **heat**

P. Haensel, *Astron. Astrophys.* **262**, 131 (1992);
A. Reisenegger, *Astrophys. J.* **442**, 749 (1995).

Deviation from β equilibrium is quantified by

$$\eta_\ell \equiv \mu_n - \mu_p - \mu_\ell \quad (\ell = e, \mu)$$

Heating luminosity

$$L_H = \sum_{\ell=e,\mu} \sum_{N=n,p} \int dV \eta_\ell \cdot \Delta\Gamma_{M,N\ell}$$

where

$$\Delta\Gamma_{M,N\ell} \equiv \Gamma(n + N \rightarrow p + N + \ell + \bar{\nu}_\ell) - \Gamma(p + N + \ell \rightarrow n + N + \nu_\ell)$$

Evolution of chemical imbalance

The time evolution of η_ℓ is determined by

$$\frac{d\eta_e}{dt} = - \sum_{N=n,p} \int dV (Z_{npe} \Delta\Gamma_{M,Ne} + Z_{np} \Delta\Gamma_{M,N\mu}) + 2W_{npe} \Omega \dot{\Omega}$$

Bring the system back to equilibrium.

Drive the system out of equilibrium.

$W < 0, Z > 0$: coefficients which depend on NS structure.

R. Fernandez and A. Reisenegger, *Astrophys. J.* **625**, 291 (2005).

Once the second term wins, the imbalance increases.

Magnetic dipole radiation

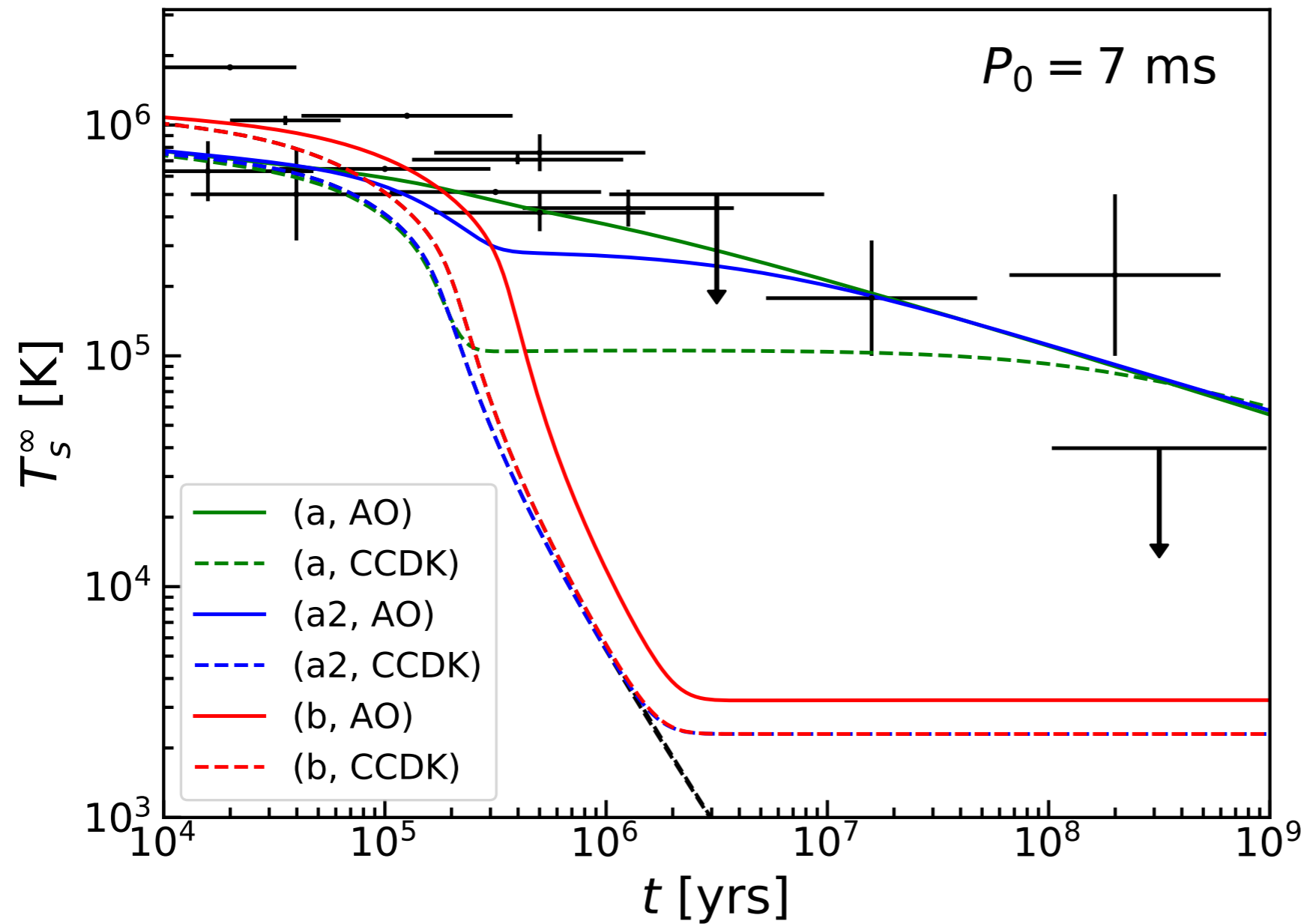
$$\dot{\Omega} = -k\Omega^3$$



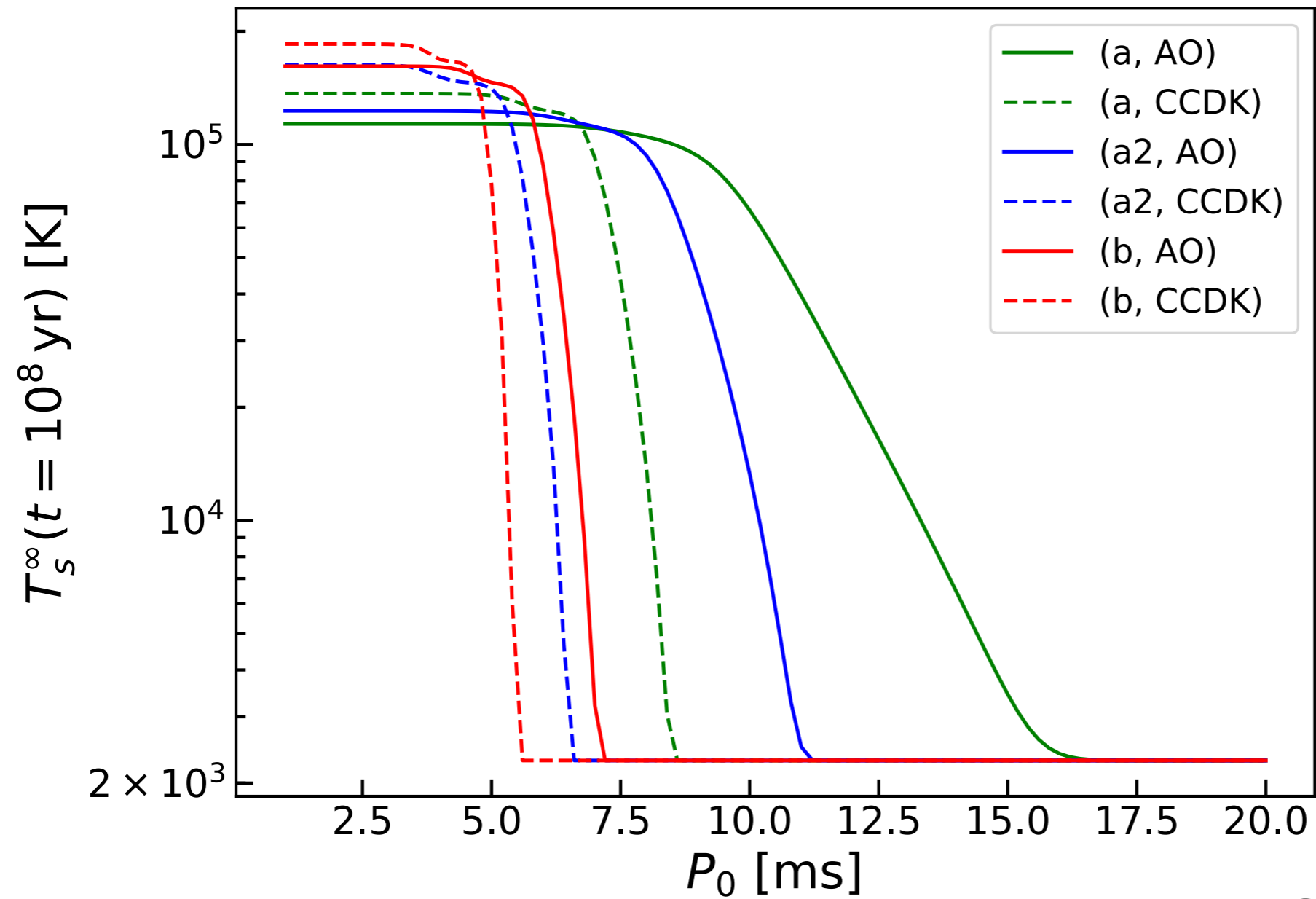
$$\Omega \dot{\Omega} = - \frac{4\pi^2 P_{\text{now}} \dot{P}_{\text{now}}}{(P_0^2 + 2P_{\text{now}} \dot{P}_{\text{now}} t)^2}$$

(P_0 : initial period)

Gap dependence



Gap dependence



Courtesy of K. Yanagi.