

# Solar neutrinos and future experiments

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## Reference

- P. Bakhti and A. Y. Smirnov, “Oscillation tomography of the Earth with solar neutrinos and future experiments,” arXiv:2001.08030 [hep-ph], Phys. Rev. D **101** (2020) no.12, 123031.
- P. Bakhti and M. Rajaei, “Sensitivities of future solar neutrino observatories to nonstandard neutrino interactions,” Phys. Rev. D **102** (2020) no.3, 035024 [arXiv:2003.12984 [hep-ph]].

# Overview

- 1 Solar Neutrino production and detection
- 2 Neutrino Oscillation
- 3 Current status of solar neutrino oscillation and future experiments
- 4 Day-night asymmetry and Earth tomography
- 5 NSI and Solar Neutrinos
- 6 Summary and Conclusion

# Solar Neutrino production

- $4p \rightarrow {}^4\text{He} + 2e^+ + 2\nu_e + Q$
- $Q = 26.73 \text{ MeV}$
- pp chain reactions provides 98.4% of the energy generation in the Sun
- 1.6% of energy is produced in the CNO cycle
- $\beta^+$  decay of proton in the presence of another proton
- $p + p \rightarrow d + e^+ + \nu_e$
- $Q_{pp} = 2M_p - M_d - m_e = 0.420 \text{ MeV}$ ,  $\bar{E}_\nu = 0.24 \text{ MeV}$  and energy peak at 0.31 MeV
- According to SSM, the pp neutrinos compose the majority (92%) of solar flux and therefore the average energy of all neutrinos is close to  $\bar{E}_{pp}$
- The reaction is a weak interaction and has the Coulomb suppression
- It is one of the slowest processes of the chain ( $t_{pp} \sim 10^{10}$  years)

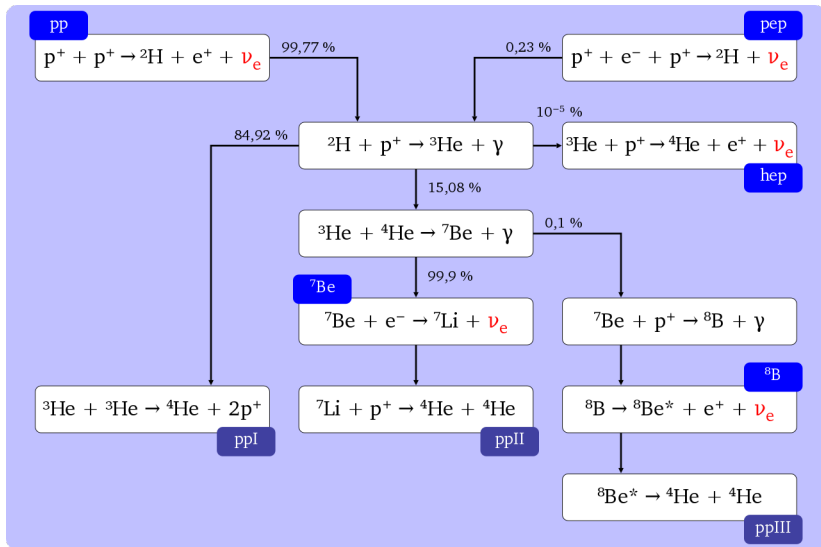
# Solar Neutrino production

- Other reactions of the chain are faster (except pep)
- pep reaction is  $p + e^- + p \rightarrow d + \nu_e$
- The rate is two orders of magnitudes smaller than pp reaction. Three body reaction.
- $t_{pep} \sim 10^{12}$  years
- $E_{pep} = 1.441$  MeV, monochromatic, width of 2 keV.  $T_c = 10^7$  K
- $d + p \rightarrow {}^3\text{He} + \gamma$  is very fast ( $t \sim 10^8$  years) and precise rate is not important
- The time of diffusion of photons from the center of the Sun to its surface is  $10^5$  years
- Neutrinos freely escape from the Sun without affecting dynamics of the Sun's evolution

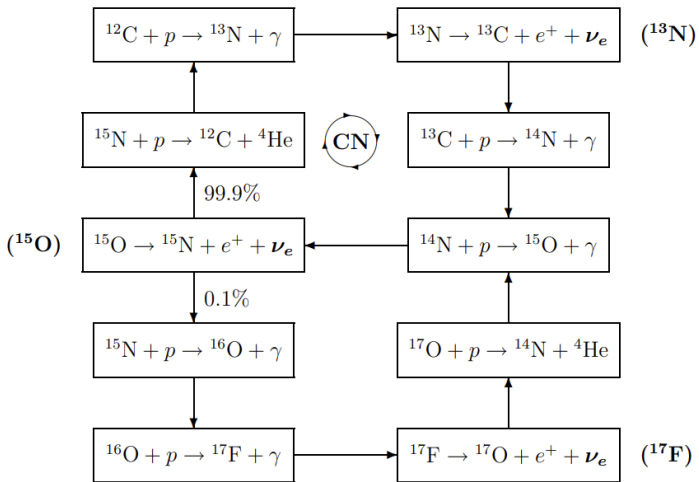
## Solar Neutrino production

- ${}^3\text{He}$  has two comparable branching fractions and a rare one
- ${}^3\text{He} + {}^3\text{He} \rightarrow {}^4\text{He} + 2p$  with branching fraction of 84.6% ( $t \sim 10^5$  years)
- ${}^3\text{He} + {}^4\text{He} \rightarrow {}^7\text{Be} + \gamma$  with branching fraction of 15.4% ( $t \sim 10^6$  years)
- The branching fractions depend on ratio of  ${}^3\text{He}/{}^4\text{He}$  densities
- The reactions depend on temperature
- ${}^3\text{He} + p \rightarrow {}^4\text{He} + e^+ + \nu_e$  has branching fraction of  $2.5 \times 10^{-5}\%$
- $Q = m_{3\text{He}} + m_p - m_{4\text{He}} - m_e = 19.8 \text{ MeV}$
- peak of energy is 9.5 MeV
- $10^{-7}$  of pp neutrino flux, three orders of magnitude smaller than Boron neutrino flux

# Solar Neutrino production

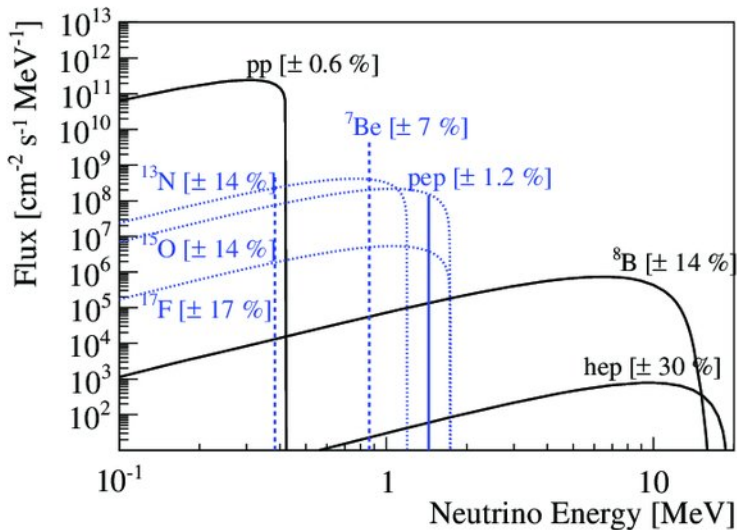


# Solar Neutrino production



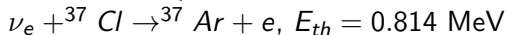


# Solar Neutrino production



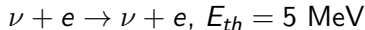
# Solar Neutrino detection

- Homestake experiment:



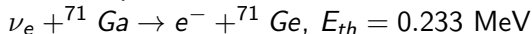
$$R_{Ar} = \frac{Q_{Ar}^{exp}}{Q_{Ar}^{SSM}} = 0.32 \pm 0.05$$

- Kamiokande, SK



$$R_{\nu e} = \frac{\phi_B^{exp}}{\phi_B^{SSM}} = 0.49 - 0.64(K) = 0.43 \pm 0.06(SK)$$

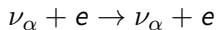
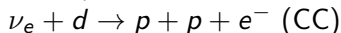
- Ga-Ge experiments



$$R_{Ar} = \frac{Q_{Ge}^{exp}}{Q_{Ge}^{SSM}} = 0.52 \pm 0.03$$

# Solar Neutrino detection

- SNO (The Sudbury Neutrino Observatory)



$$R = \frac{\phi_{CC}}{\phi_{NC}} = \frac{\phi_e}{\phi_{tot}} = 0.34 \pm 0.04(K)$$

- Borexino: 1 kt scintillation detector,  $\nu_e$  scattering, recoil electrons is measured down to 0.2 MeV, with the fiducial mass of 0.1 kt high energy resolution

# Neutrino Oscillation

There is a mixing between mass and flavor states

$$|\nu_\alpha\rangle = \sum_i U_{\alpha i}^* |\nu_i\rangle, \quad \alpha = e, \mu, \tau, \quad i = 1, 2, 3 \quad (1)$$

PMNS mixing matrix

$$U = \begin{bmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{bmatrix} \quad (2)$$

Neutrino oscillation in vacuum

$$P_{\nu_\alpha \rightarrow \nu_\beta} = \sum_{k,j} U_{\alpha k}^* U_{\beta k} U_{\alpha j} U_{\beta j}^* e^{-i \frac{\Delta m_{kj}^2 L}{2E}} \quad (3)$$

## Neutrino Oscillation in Vacuum

$$H |\nu_k\rangle = E_k |\nu_k\rangle \quad (4)$$

$$i \frac{d}{dt} |\nu_k(t)\rangle = H |\nu_k(t)\rangle \quad (5)$$

$$|\nu_k(t)\rangle = e^{-iE_k t} |\nu_k\rangle \quad (6)$$

$$|\nu_\alpha(t)\rangle = \sum_k U_{\alpha k}^* e^{-iE_k t} |\nu_k\rangle \quad (7)$$

$$|\nu_\alpha(t)\rangle = \sum_\beta \sum_k U_{\alpha k}^* e^{-iE_k t} U_{\beta k} |\nu_\beta\rangle \quad (8)$$

$$P_{\nu_\alpha \rightarrow \nu_\beta} = \sum_{k,j} U_{\alpha k}^* U_{\beta k} U_{\alpha j} U_{\beta j}^* e^{-i(E_k - E_j)t} \quad (9)$$

## Neutrino Oscillation in Vacuum

$$E_k \simeq E + \frac{m_k^2}{2E} \quad (10)$$

$$E_k - E_j \simeq \frac{\Delta m_{kj}^2}{2E} \equiv \frac{m_k^2 - m_j^2}{2E} \quad (11)$$

$$P_{\nu_\alpha \rightarrow \nu_\beta} = \sum_{k,j} U_{\alpha k}^* U_{\beta k} U_{\alpha j} U_{\beta j}^* e^{-i \frac{\Delta m_{kj}^2 L}{2E}} \quad (12)$$

# Neutrino Oscillation in Matter

- Forward elastic scattering processes affect neutrino oscillation

$$\mathcal{H}_f = \mathcal{H}_{vac} + \mathcal{H}_{mat} \quad (13)$$

$$\mathcal{H}_{mat} = \sqrt{2}G_F N_e \text{diag}(1, 0, 0) \quad (14)$$

$$\mathcal{H}_{vac} = U_{PMNS} \cdot \text{Diag}(0, \Delta m_{21}^2, \Delta m_{31}^2) \cdot U_{PMNS}^\dagger \quad (15)$$

- Considering  $2\nu$  Oscillation

$$i \frac{d}{dx} \psi_\alpha = \mathcal{H}_f \psi_\alpha \quad (16)$$

$$\mathcal{H}_F = \begin{bmatrix} -\Delta m^2 \cos 2\theta + A_{CC} & \Delta m^2 \sin 2\theta \\ \Delta m^2 \sin 2\theta & \Delta m^2 \cos 2\theta - A_{CC} \end{bmatrix} \quad (17)$$

# Neutrino Oscillation in Matter

$$\psi^T = (\psi_{ee}, \psi_{e\mu}) \quad (18)$$

$$A_{CC} = 2\sqrt{2}EG_F N_e = 2V_{CC}E \quad (19)$$

$$\mathcal{H}_M = U_M \mathcal{H}_F U_M \quad (20)$$

$$U_M = \begin{bmatrix} \cos 2\theta_M & \sin \theta_M \\ -\sin \theta_M & \cos 2\theta_M \end{bmatrix} \quad (21)$$

$$\mathcal{H}_M = \text{diag}(-\Delta m_M^2, \Delta m_M^2) \quad (22)$$



# Neutrino Oscillation in Matter

$$\Delta m_M^2 = \sqrt{(\Delta m^2 \cos 2\theta - A_{CC})^2 + (\Delta m^2 \sin 2\theta)^2} \quad (23)$$

$$\tan 2\theta_M = \frac{\tan 2\theta}{1 - \frac{A_{CC}}{\Delta m^2 \cos 2\theta}} \quad (24)$$

$$A_{CC}^R = \Delta m^2 \cos 2\theta \quad (25)$$

$$N_e^R = \frac{\Delta m^2 \cos 2\theta}{2\sqrt{2}EG_F} \quad (26)$$

In the case of anti-neutrino  $V_{CC} \rightarrow -V_{CC}$  ( $A_{CC} = 2EV_{CC}$ )

- For  $\Delta m_{21}^2 > 0$  the resonance condition is fulfilled in the neutrino channel with  $V > 0$  only. For antineutrinos  $V < 0$ .

## Neutrino Oscillation in the Sun

$$P_{ee} = \sum_k |U_{ek}^m(n_i) U_{ek}^{m\dagger}(n_f) e^{-i\phi_k}|^2 = \sum_k |U_{ek}^m(n_e^0)|^2 P_{ek}^E \quad (27)$$

$$|U_{e1}^m| = \cos \theta_{13}^m \cos \theta_{12}^m, \quad |U_{e2}^m| = \cos \theta_{13}^m \sin \theta_{12}^m, \quad |U_{e3}^m| = \sin \theta_{13}^m$$

$$P_{3e} \approx s_{13}^2, \quad P_{1e} + P_{2e} = 1 - s_{13}^2$$

$$P_D(E) = \frac{1}{2} c_{13}^4 [1 + \cos 2\theta_{12} \cos 2\bar{\theta}_{12}^m(E)] + s_{13}^4 \quad (28)$$

$$\cos 2\bar{\theta}_{12}^m \approx \frac{\cos 2\theta_{12} - c_{13}^2 \bar{\epsilon}_\odot}{\sqrt{(\cos 2\theta_{12} - c_{13}^2 \bar{\epsilon}_\odot)^2 + \sin^2 2\theta_{12}}}. \quad (29)$$

$$\bar{\epsilon}_\odot \equiv \frac{2\bar{V}_\odot E}{\Delta m_{21}^2}, \quad V(x) = \sqrt{2} G_F n_e(x)$$

# Day-Night Asymmetry

- Due to loss of the propagation coherence, the solar neutrinos arrive at the surface of the Earth as independent fluxes of the mass eigenstates
- Inside the Earth, the mass states oscillate in a multilayer medium with smoothly changing density within layers

$$f_{reg} = |U_{e1}|^2 - P_{1e}^E = \frac{1}{2} c_{13}^4 \sin^2 2\theta_{12} \int_0^L dx V(x) \sin \phi^m \quad (30)$$

$$\Delta P(E) = \kappa(E) \left[ \int_0^L dx V(x) \sin \phi^m(L-x, E) + I_2 \right] \quad (31)$$

$$\kappa(E) \equiv -\frac{1}{2} c_{13}^6 \cos 2\bar{\theta}_{12}^{\odot}(E) \sin^2 2\theta_{12} \approx 0.5$$

## Day-Night Asymmetry

$$I_2 \equiv \frac{1}{2} \cos 2\theta_{12} \left[ \int_0^L dx V(x) \cos \phi^m(L-x) \right]^2 \quad (32)$$

$$\phi^m(L-x, E) \equiv \int_x^L dx \Delta_{21}^m(x). \quad (33)$$

$$\begin{aligned} \Delta_{21}^m &= \Delta_{21} \sqrt{(\cos 2\theta_{21} - c_{13}^2 \epsilon)^2 + \sin^2 2\theta_{21}} \\ &\approx \Delta_{21} (1 - c_{13}^2 \cos 2\theta_{12} \epsilon) = \frac{\Delta m_{21}^2}{2E} (1 - c_{13}^2 \cos 2\theta_{12} \epsilon). \end{aligned} \quad (34)$$

$$\phi^m(L-x, E) = \Delta_{21} \left[ (L-x) - c_{13}^2 \cos 2\theta_{12} \int_x^L dx \epsilon(x) \right]. \quad (35)$$

# Day-Night Asymmetry

$$A_{ND}(\eta, \Delta E) \equiv \frac{\Delta N(\eta, \Delta E)}{N_D(\Delta E)} \quad \Delta N \equiv N_N - N_D \quad (36)$$

$$\Delta N(E^r) = D \int dE G_\nu(E^r, E) \Delta P(E) \quad (37)$$

$$G_\nu(E^r, E) \propto g_\nu(E^r, E) \sigma(E) f_B(E) \quad (38)$$

$$\Delta N(E^r) = D \int_0^L dx V(x) \int_0^{E^{\max}} dE G_\nu(E^r, E) \sin \phi^m(L - x, E) \quad (39)$$

# Attenuation Effect

$$\int dE G_\nu(E^r, E) \sin \phi^m(L-x, E) = F(L-x) \sin \phi^m(L-x, E^r) \quad (40)$$

$$\Delta N(E^r) = D \int dx V(x) F(L-x) \sin \phi^m(L-x, E^r). \quad (41)$$

For the Gaussian form of  $G_\nu(E^r, E)$

$$F(L-x) \simeq e^{-2\left(\frac{L-x}{\lambda_{att}}\right)^2} \quad (42)$$

$$\lambda_{att} \equiv l_\nu \frac{E}{\pi \sigma_E} \quad l_\nu = \frac{4\pi E}{\Delta m_{21}^2}$$

For  $L-x \gg \lambda_{att}$  the attenuation factor  $F(L-x) \approx 0$ , a detector with the energy resolution  $\Delta E$  is not sensitive to remote structures

# Day-Night Asymmetry

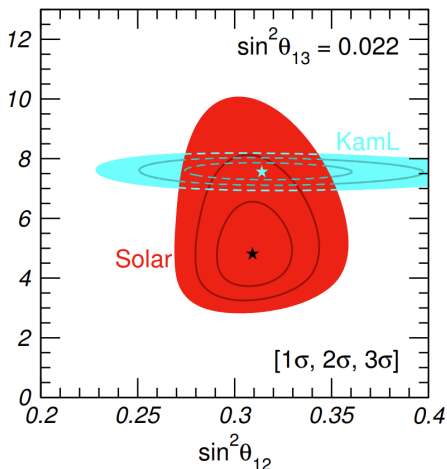
Neutrino-nuclei scattering

$$N_D(\Delta E_e^r) = Dz \int_{E^{min}}^{E^{max}} dE^r \sigma(E^r) f_B(E^r) P_D(E^r). \quad (43)$$

Neutrino-electron scattering

$$N_D(E_e^r) = \int_0^{E^{max}} dE f_B(E) g_\nu(E_e^r, E) \left[ P_D(E) \sigma^e(E, E_e^{th}) + (1 - P_D(E)) \sigma^\mu(E, E_e^{th}) \right]. \quad (44)$$

# Global analysis of solar neutrino oscillation



M. Maltoni and A. Y. Smirnov, "Solar neutrinos and neutrino physics,"  
 Eur. Phys. J. A **52** (2016) no.4, 87 [arXiv:1507.05287 [hep-ph]]



# LMA MSW solution and beyond

- The sign of  $\Delta m_{21}^2$  determines the resonance of  $\nu_e$  solar neutrinos
- About  $2\sigma$  tension between KamLAND and solar neutrino data
- Increase of the ratio of the measured spectrum to the SSM one toward low energies (discrepancy)
- Discrepancy between measured and predicted day-night asymmetry
- Non-Standard neutrino Interaction
- Sterile neutrino, etc

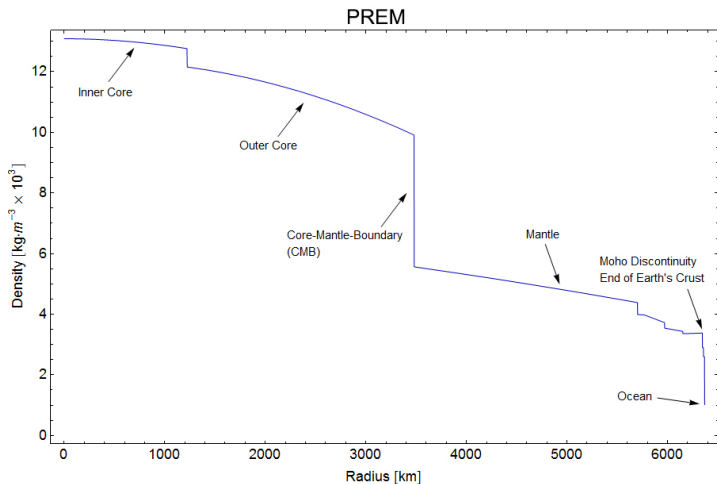
## Future studies of solar neutrinos

- JUNO and RENO-50, determination of  $\Delta m_{21}^2$  and  $\theta_{12}$  with sub percent precision. With a good energy resolution, these experiments will detect  ${}^8B, {}^7Be$  and *pep* neutrinos
- Precision (at sub-percent level) measurements of neutrino fluxes with future solar neutrino observatories
- SNO+, 780 t of liquid scintillator fiducial mass of 390 t, energy threshold of 3 MeV, the threshold of the upgraded version decreased
- Jinping, 4 (2) kton liquid scintillator, detect low energy neutrinos with a good precision
- Yemilab solar neutrino detector, 2 kton liquid scintillator
- DUNE, 40 kton liquid argon, 10 MeV energy threshold
- Hyper-Kamiokande (KNO), energy threshold of 6.5 MeV, several 100 kt detectors
- THEIA, water-based liquid scintillator, 1% doping by  ${}^7Li$

# Earth Structure

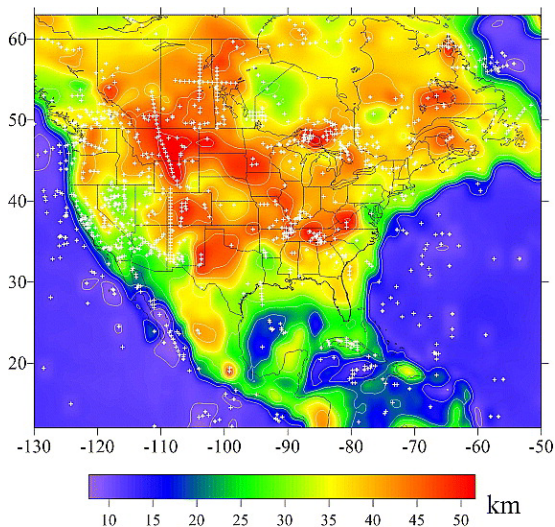
- P. Bakhti and A. Y. Smirnov, "Oscillation tomography of the Earth with solar neutrinos and future experiments," Phys. Rev. D **101** (2020) no.12, 123031 [arXiv:2001.08030 [hep-ph]].
- Due to the attenuation effect,  $A_{ND}$  mainly depends on shallow density structures: crust, upper mantle, and crust-mantle border called Moho, or Mohorovicic discontinuity.
- There are two types of crust: the oceanic crust (5 - 10) km and the continental crust (20 - 90) km
- Shen-Ritzwoller model: crust and uppermost mantle beneath North America, in the area with latitudes ( $20^\circ - 50^\circ$ ) and longitudes ( $235^\circ - 295^\circ$ ), from the sea level surface down to the depth of 150 km
- FWEA18, the Full Waveform Inversion of East Asia model: latitudes  $10^\circ - 60^\circ$  and longitudes  $90^\circ - 150^\circ$ , from the surface down to 800 km
- SAW642AN: global model, from the depth of Moho, down to 2900 km
- CRUST1: global model, from Earth's surface down to the Moho

## PREM

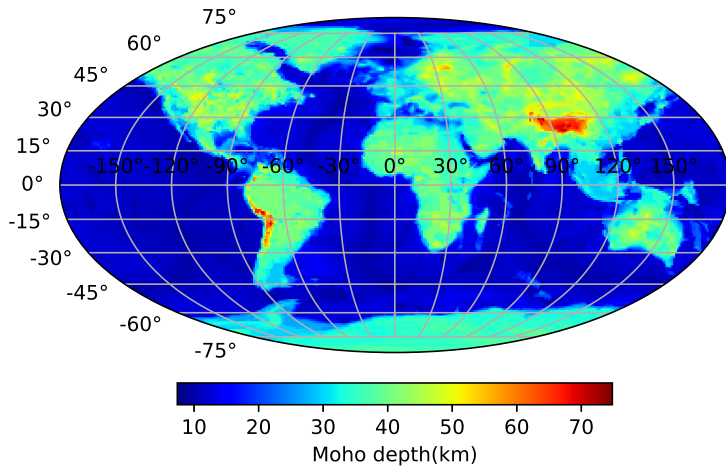


## Preliminary Reference Earth Model (PREM)

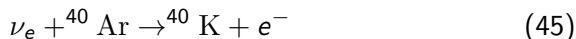
# Shen-Ritzwoller Moho depth



# CRUST1 Moho depth



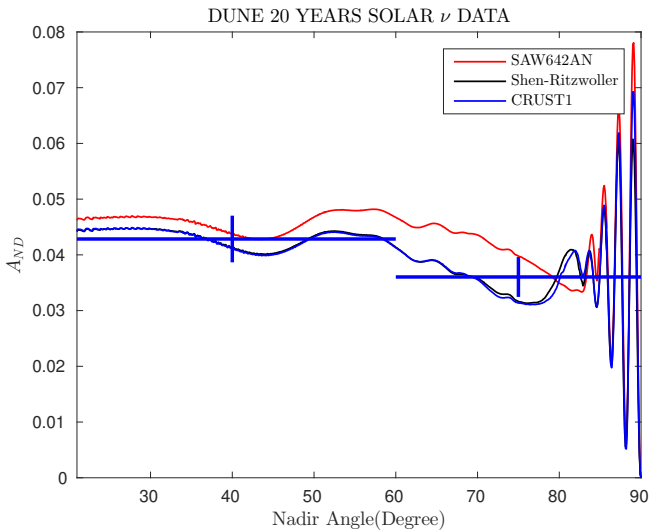
## DUNE



$$\sigma_{CC}(E) = A\rho_e E_e \quad (46)$$

$$E_e = E_\nu - \Delta M, \quad \Delta M = 5.8 \text{ MeV}$$

- With  $\sigma_E/E = 7\%$ ,  $\lambda_{att} = 1800 \text{ km}$  for  $E = 12 \text{ MeV}$
- $L > \lambda_{att}$  is  $\eta_{att} = 82^\circ$
- 27000  $\nu_e$  events detected annually with  $E_\nu > 11 \text{ MeV}$  in the 40 kt fiducial volume
- $\bar{A}_{ND} = 0.040, 0.040$  and  $0.043$ , for CRUST1, S-R, and SAW642AN models, respectively
- precision of measurement of  $\bar{A}_{ND}$  will be 0.002

$A_{ND}(\eta)$  at DUNE



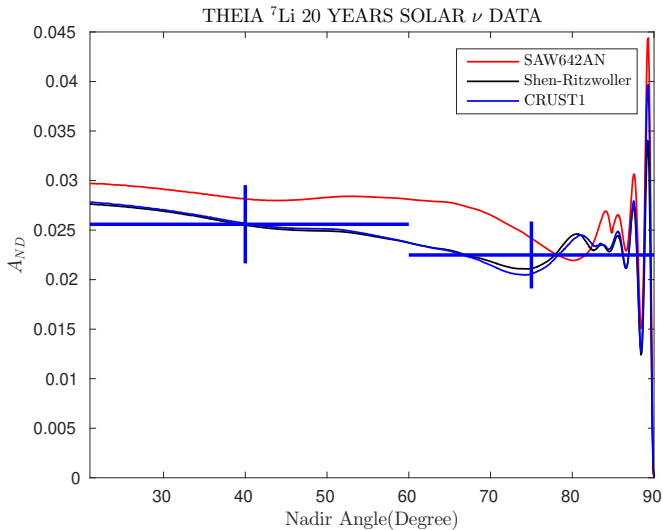
## THEIA

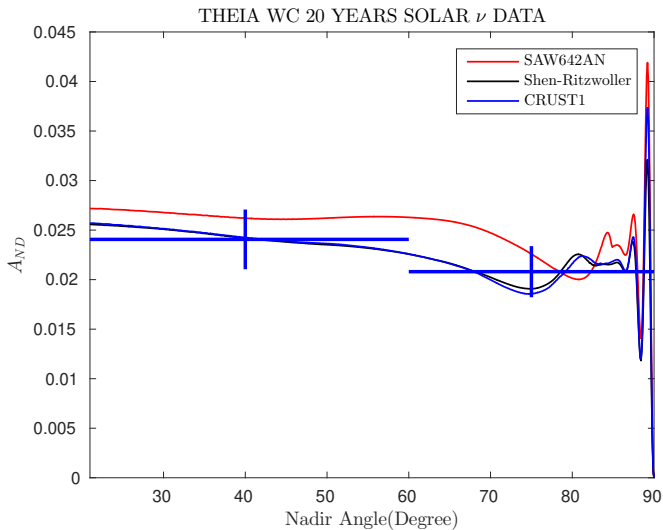
- 100 kT water-based liquid scintillator detector loaded with 1%  ${}^7\text{Li}$

- 



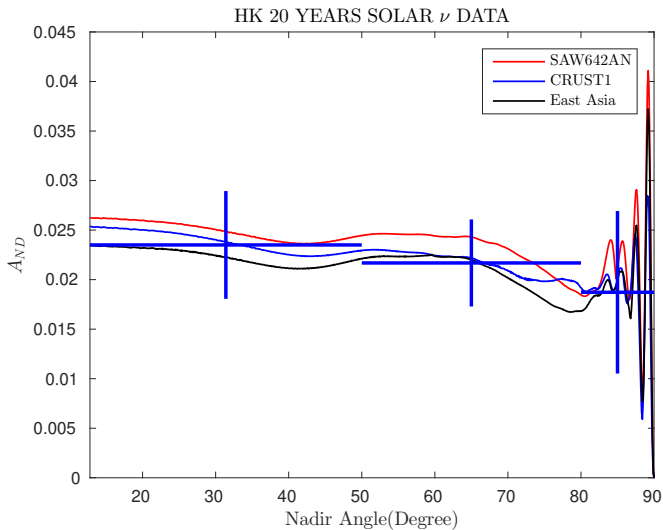
- The cross-section of this process is known with high precision.
- $\nu - e$  elastic scattering with 6.5 MeV threshold
- 17000  ${}^7\text{Li}$  and 15000  $\nu - e$  elastic scattering events are expected annually with  $E_\nu > 5$  MeV
- $\sigma_E/E = 12\%$  for  ${}^7\text{Li}$  and  $\sigma_E/E = 15\%$  for  $\nu - e$  elastic scattering
- $\bar{A}_{ND} = 0.024$  (CRUST1 and S-R) and 0.027 (SAW642AN) for  ${}^7\text{Li}$ , and  $\bar{A}_{ND} = 0.022$  (CRUST1 and S-R) and 0.025 (SAW642AN) for elastic scattering events
- precision of measurement of  $\bar{A}_{ND}$  will be 0.005

$A_{ND}(\eta)$  at THEIA

$A_{ND}(\eta)$  at THEIA

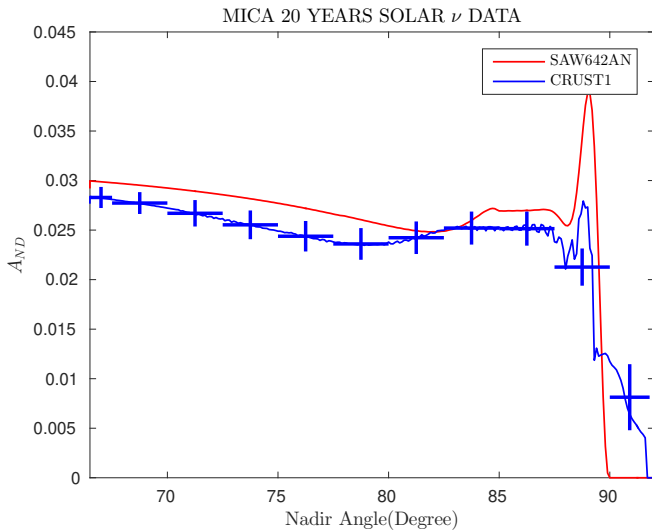
## HK

- $\nu - e$  elastic scattering with 6.5 MeV threshold
- $\sigma_E/E = 15\%$
- $\lambda_{att} = 700$  km for  $E = 10$  MeV
- 80 events are expected per day
- $\bar{A}_{ND} = 0.020$  (FWEA18), 0.022 (CRUST1) and 0.024 (SAW642AN)
- precision of measurement of  $\bar{A}_{ND}$  will be 0.002
- Smaller  $\bar{A}_{ND}$  than DUNE: damping due to contribution from NC scattering, which is 0.76, and difference of averaged energies  $E_{HK}/E_{DUNE} = 0.75$
- HK will distinguish between EA and SAW642AN, with  $1.5\sigma$ , CRUST1 is recognizable from EA and SAW642 with  $0.7\sigma$  and  $1.2\sigma$  respectively

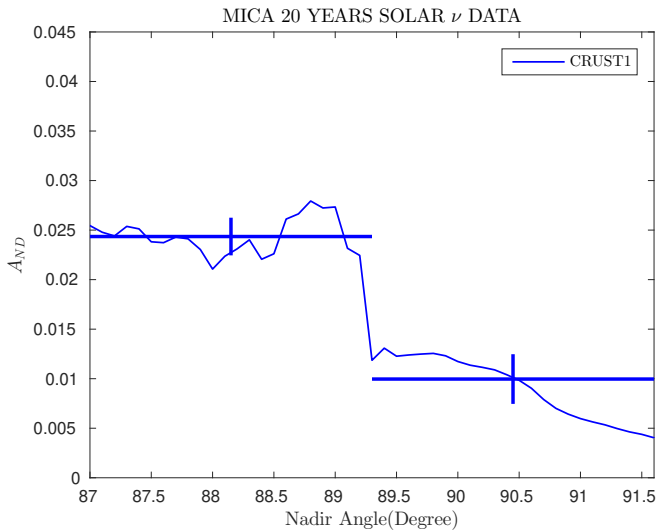
$A_{ND}(\eta)$  at HK

# MICA

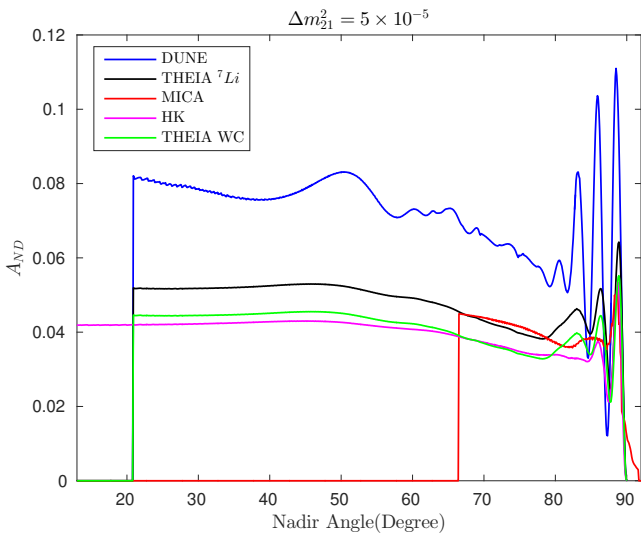
- $\nu - e$  elastic scattering with 10 MeV threshold
- 10 Mton fiducial mass
- $\sigma_E/E = 15\%$
- $5 \times 10^5$  solar  $\nu e$ - scattering events are expected per year
- MICA detector at a depth of 2.25 km below the icecap (as the Deep Core). The height of icecap at the location of MICA is 2.7 km above the sea level.
- $\bar{A}_{ND} = 0.026$  (CRUST1)
- precision of measurement of  $\bar{A}_{ND}$  will be 0.00045

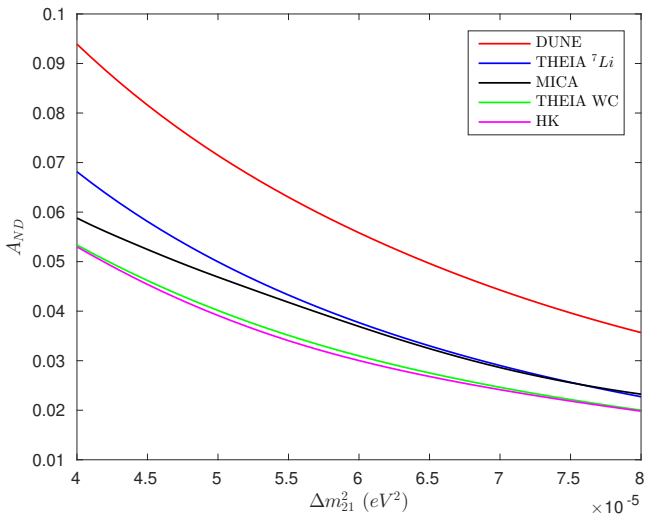
$A_{ND}(\eta)$  at MICA

# $A_{ND}(\eta)$ at MICA and Ice-Soil borderline





$A_{ND}(\eta)$  with  $\Delta m_{21}^2 = 5 \times 10^{-5}$ 


$\bar{A}_{ND}$ 

# NSI for Solar Neutrinos

P. Bakhti and M. Rajaei, "Sensitivities of future solar neutrino observatories to nonstandard neutrino interactions," Phys. Rev. D **102** (2020) no.3, 035024 [arXiv:2003.12984 [hep-ph]].

$$\mathcal{L}_{\text{NSI}}^{\text{NC}} = -2\sqrt{2}G_F \varepsilon_{\alpha\beta}^{fC} (\bar{\nu}_\alpha \gamma^\mu P_L \nu_\beta) (\bar{f} \gamma_\mu P_C f) \quad (48)$$

Since  $\frac{\Delta m_{31}^2}{E_\nu} \gg G_F N_e$  for solar neutrinos, it is possible to work on one mass dominate approximation, using  $2 \times 2$  effective Hamiltonian as following

$$H_{\text{vac}}^{\text{eff}} = \frac{\Delta m_{21}^2}{4E_\nu} \begin{pmatrix} -\cos 2\theta_{12} & \sin 2\theta_{12} \\ \sin 2\theta_{12} & \cos 2\theta_{12} \end{pmatrix}, \quad (49)$$

$$H_{\text{mat}}^{\text{eff}} = \sqrt{2}G_F N_e(r) \begin{pmatrix} c_{13}^2 & 0 \\ 0 & 0 \end{pmatrix} + \sqrt{2}G_F \sum_f N_f(r) \begin{pmatrix} -\epsilon_D^f & \epsilon_N^f \\ \epsilon_N^{f*} & \epsilon_D^f \end{pmatrix}. \quad (50)$$

## NSI for Solar Neutrinos

$$\begin{aligned} \epsilon_D^f &= -\frac{c_{13}^2}{2} (\epsilon_{ee}^f - \epsilon_{\mu\mu}^f) + \frac{s_{23}^2 - s_{13}^2 c_{23}^2}{2} (\epsilon_{\tau\tau}^f - \epsilon_{\mu\mu}^f) \\ &+ \text{Re} \left[ c_{13} s_{13} e^{i\delta} (s_{23} \epsilon_{e\mu}^f + c_{23} \epsilon_{e\tau}^f) - (1 + s_{13}^2) c_{23} s_{23} \epsilon_{\mu\tau}^f \right] \end{aligned} \quad (51)$$

$$\epsilon_N^f = c_{13} (c_{23} \epsilon_{e\mu}^f - s_{23} \epsilon_{e\tau}^f) + s_{13} e^{-i\delta} \left[ s_{23} \epsilon_{\mu\tau}^f - c_{23}^2 \epsilon_{\mu\tau}^{f*} + c_{23} s_{23} (\epsilon_{\tau\tau}^f - \epsilon_{\mu\mu}^f) \right]$$

$$U' = \begin{pmatrix} \cos \tilde{\theta}_{12} & \sin \tilde{\theta}_{12} e^{-i\phi} \\ -\sin \tilde{\theta}_{12} e^{i\phi} & \cos \tilde{\theta}_{12} \end{pmatrix} \quad (52)$$

$$\tan 2\tilde{\theta}_{12} = \frac{|\sin 2\theta_{12} + 2\hat{A}_E \epsilon_N|}{\cos 2\theta_{12} - \hat{A}_E (c_{13}^2 - 2\epsilon_D)} \quad (53)$$

$$\phi = -\text{Arg} \left( \sin 2\theta_{12} + 2\hat{A}_E \epsilon_N \right). \quad (54)$$

# Day-Night Asymmetry and NSI

$$P_D(E) = \frac{1}{2} c_{13}^4 \left[ 1 + \cos 2\theta_{12} \cos 2\tilde{\theta}_{12}(E) \right] + s_{13}^4 \quad (55)$$

$$N_{D(N)} = A \int dE g_\nu(E^r, E) \sigma(E) f_B(E) P(E)_{D(N)} \quad (56)$$

$$\Delta P(E, \eta) = P_N - P_D = \kappa(E) \left[ \int_0^L dx V(x) \sin \phi^m(L-x, E) \right] \quad (57)$$

$$\kappa(E) \equiv -\frac{1}{2} c_{13}^4 \cos 2\tilde{\theta}_{12}^s \sin 2\theta_{12} (\sin 2\theta_{12} (c_{13}^2 - 2\epsilon_D^E) + 2 \cos 2\theta_{12} \epsilon_N^E) \quad (58)$$

$$\phi^m(L-x, E) \equiv \int_x^L dx \Delta_{21}^m(x) \approx \int_x^L dx \Delta_{21} (1 - c_{13}^2 \cos 2\theta_{12} a_{CC}^E) \quad (59)$$

# Neutral Current NSI Effect on Electron Neutrino Scattering

$$\frac{d\sigma}{dT}(E_\nu, T_e) = \frac{2G_F^2 m_e}{\pi} \left[ (g_1)^2 + (g_2)^2 \left(1 - \frac{T_e}{E_\nu}\right)^2 - g_1 g_2 \frac{m_e T_e}{E_\nu^2} \right] \quad (60)$$

within the standard model

$$g_1^{\nu_e} = g_2^{\bar{\nu}_e} = \frac{1}{2} + \sin^2 \theta_W = 0.73 \quad (61)$$

$$g_2^{\nu_e} = g_1^{\bar{\nu}_e} = g_2^{\nu_\mu} = g_1^{\bar{\nu}_\mu} = \sin^2 \theta_W = 0.23 \quad (62)$$

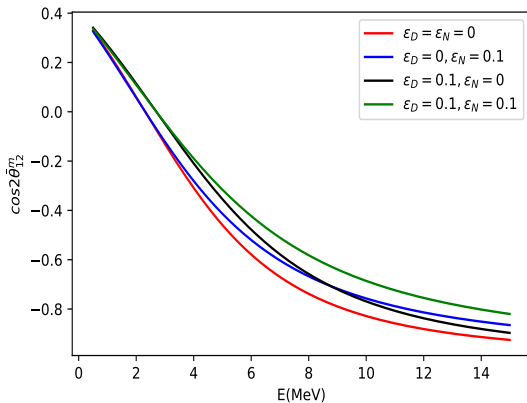
$$g_1^{\nu_\mu} = g_2^{\bar{\nu}_\mu} = -\frac{1}{2} + \sin^2 \theta_W = -0.27 \quad (63)$$

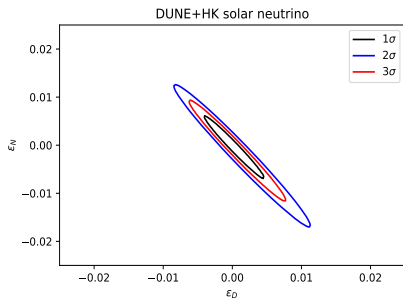
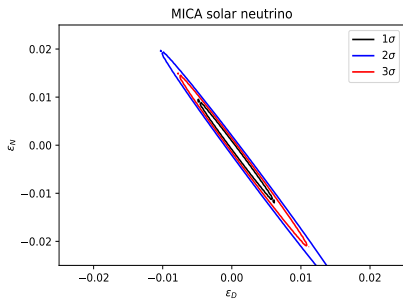
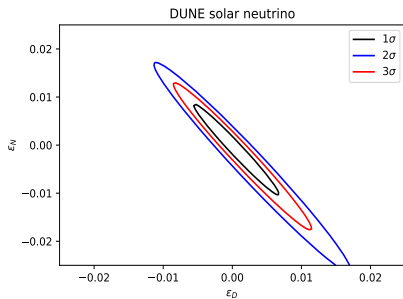
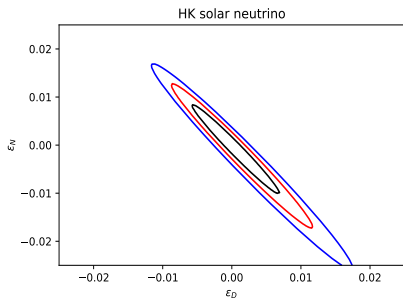
Considering the neutral current NSI

$$g_1^{e \text{ NSI}} = g_1^e + \epsilon_{ee}^{eL} \quad (64)$$

$$g_2^{e \text{ NSI}} = g_2^e + \epsilon_{ee}^{eR} \quad (65)$$

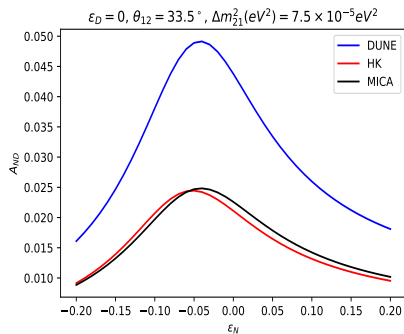
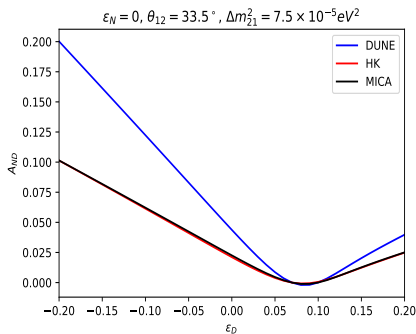
## Solar Neutrino NSI



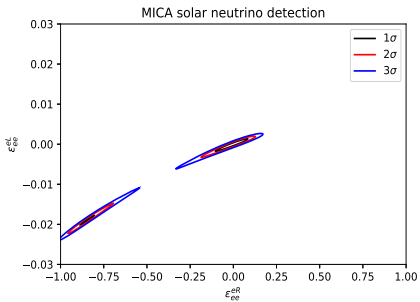
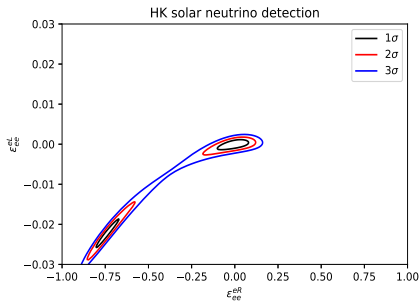
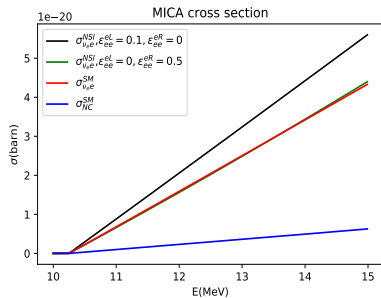
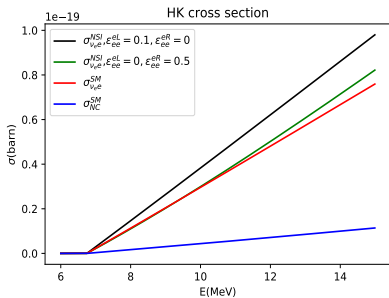


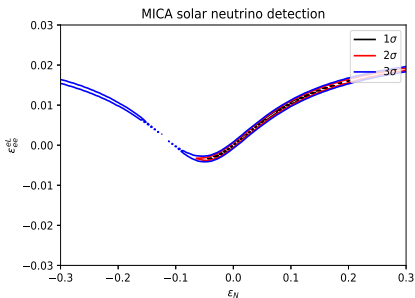
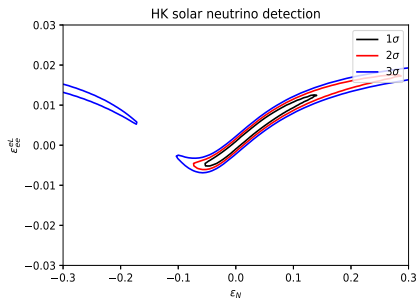
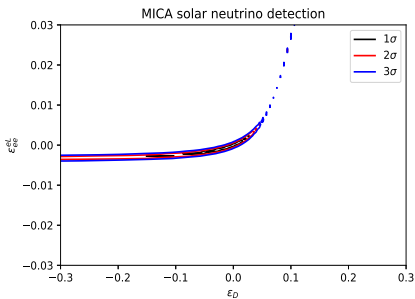
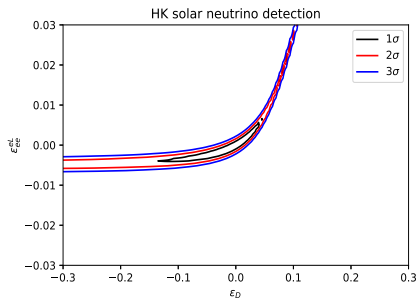


# Day-Night Asymmetry



- constraints on  $\epsilon_N$  will be 0.014, 0.014, and 0.007 respectively by DUNE, HK, and MICA
- constraints on  $\epsilon_D$  will be 0.004, 0.004, and 0.002 respectively by DUNE, HK, and MICA





# Summary

- JUNO and RENO-50 determines solar neutrino oscillation parameters with the sub-percent precision
- We will be sensitive to the shallow structure of the Earth, especially the crust and upper mantle from Day-Night asymmetry due to the attenuation effect
- Solar neutrino observatories combined with JUNO and RENO-50 will be sensitive to new physics such as NSI
- Future precision measurements of all the components of the solar neutrino spectrum will bring us to a new level of checks of solar models, physics of neutrino propagation, and transformations