

New approaches to semi-invisible τ and B decays

Chan Beom Park

Chonnam National University

Workshop on Higgs and Cosmology connection:
Yonsei-APCTP-France-Korea Star collaboration project

13 December 2022

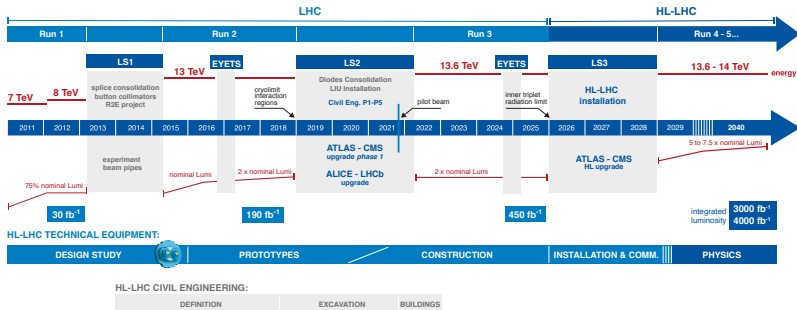
Based on

D. Guadagnoli, CBP, F. Tenchini, [2106.16236](#), PLB 822 (2021) 136701
G. de Marino, D. Guadagnoli, CBP, K. Trabelsi, [2209.03387](#)

Large Hadron Collider

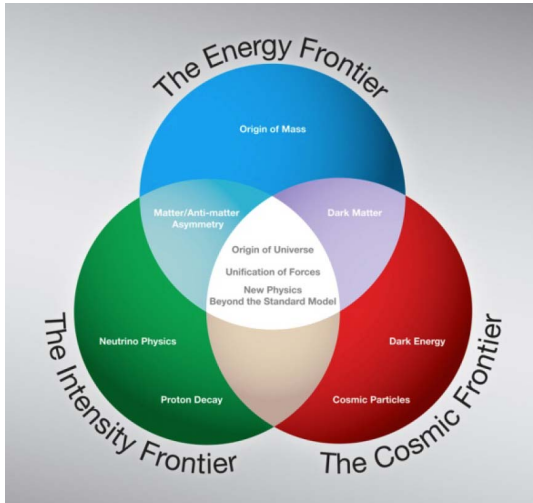


LHC / HL-LHC Plan



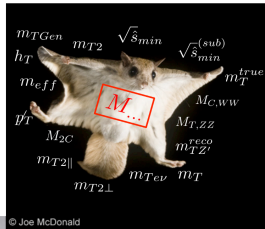
<https://hilumilhc.web.cern.ch/content/hl-lhc-project>

- The third run (Run 3) of the LHC has started this year (2022) with upgraded collision energy.

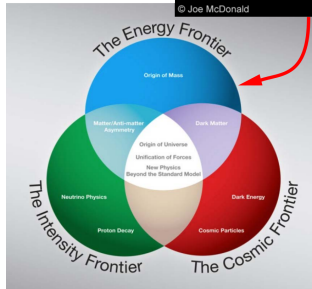


■ The Energy Frontier (to produce new *heavy* particles):

LHC, Future Colliders (CEPC, FCC-*ee*, FCC-*hh*, ILC, Muon Collider, ...)



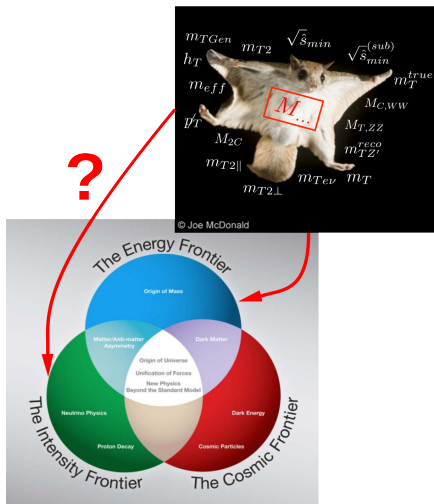
© Joe McDonald



Upper image taken from Barr *et al.*, 1105.2977 (PRD 2011)

■ How to probe new heavy particles at high-energy colliders?

— via **Kinematic Variables**



■ Applications to the Intensity Frontier (to search for *rare* new physics process)?

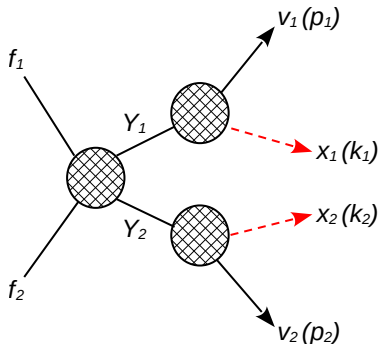
- ▶ Belle/Belle II, LHCb, ... (aka B- and τ -factories)
- ▶ **Kinematic variables:** Event topology \longrightarrow observable

Outline

1. The M_{T2} and M_2 variables
2. Searching for a new invisible particle: $\tau \rightarrow \ell + \phi$
3. Search for rare B decays: $B \rightarrow K\tau\mu$
4. Conclusions

Pair production, two invisible particles

- Pair production of heavy resonances: $Y_1 Y_2 \rightarrow v_1 \chi_1 + v_2 \chi_2$

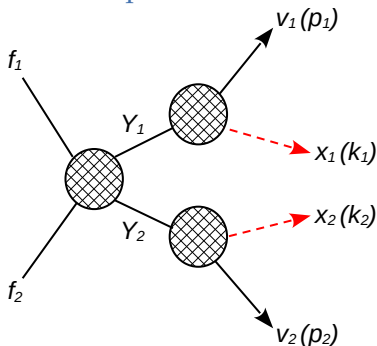


- ▶ v : (collections of) visible particles (jets, charged leptons, ...)
- ▶ χ : (stable or long-lived) **invisible** particles (neutrinos, dark matter, ...)

- A common decay topology arising in many physics models:

$$\begin{aligned} \tilde{q}\tilde{q} &\rightarrow q\tilde{\chi}_1^0 + q\tilde{\chi}_1^0, \quad \tilde{\ell}\tilde{\ell} \rightarrow \ell\tilde{\chi}_1^0 + \ell\tilde{\chi}_1^0, \quad \tilde{g}\tilde{g} \rightarrow q\tilde{q}\tilde{\chi}_1^0 + q\tilde{q}\tilde{\chi}_1^0 \text{ (supersymmetry),} \\ t\bar{t} &\rightarrow b\ell^+\nu + \bar{b}\ell^-\bar{\nu}, \quad H \rightarrow WW^* \rightarrow \ell^+\nu + \ell^-\bar{\nu} \text{ (SM), } \dots \end{aligned}$$

Pair production, two invisible particles



■ Problem:

▶ For $k_a = (k_{aT}, k_{aL})$, we don't know k_{1L} and k_{2L} .

▶ We don't know k_{1T} and k_{2T}

but know $k_{1T} + k_{2T} = P_T^{\text{miss}}$

($\because k_{1T} + k_{2T} + \sum p_T^{\text{vis}} = \mathbf{0}$ at hadron colliders)



“... there are **known knowns** ... We also know there are **known unknowns** ...
But there are also **unknown unknowns** ...”

Pair production, two invisible particles: M_{T2}

$$M_{T2} = \min_{\mathbf{k}_{1T}, \mathbf{k}_{2T} \in \mathbb{R}^2} \left[\max \left\{ M_{1T}, M_{2T} \right\} \right]$$

subject to $\mathbf{k}_{1T} + \mathbf{k}_{2T} = \mathbf{P}_T$

Lester, Summers, PLB (1999), Barr, Lester, Stephens, J. Phys. G (2003).

where M_{aT} are transverse masses,

$$\begin{aligned} M_{aT}^2 &= (E_{aT} + e_{aT})^2 - (\mathbf{p}_{aT} + \mathbf{k}_{aT})^2 \\ &= m_a^2 + M_\chi^2 + 2(E_{aT}e_{aT} - \mathbf{p}_{aT} \cdot \mathbf{k}_{aT}) \quad (a = 1, 2) \end{aligned}$$

■ Why *transverse* mass?

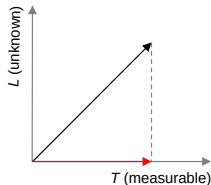
— because we **don't know the longitudinal components** (k_{aL}).

■ Why *max*?

— to access the **heaviest physics scale** of the decay
(the mass of the heaviest parent particle mass, M_Y).

■ Why *min*?

— to get an event-by-event **lower bound on M_Y** .



$$M_{T2} \leq M_Y \quad (\text{if } M_\chi = M_\chi^{\text{true}})$$

Eur. Phys. J. C (2020) 80:3
<https://doi.org/10.1140/epjc/s10052-019-7493-x>

THE EUROPEAN
PHYSICAL JOURNAL C



Regular Article - Experimental Physics

Searches for physics beyond the standard model with the M_{T2} variable in hadronic final states with and without disappearing tracks in proton–proton collisions at $\sqrt{s} = 13$ TeV

CMS Collaboration*

CERN, 1211 Geneva 23, Switzerland

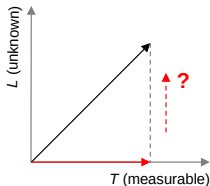
Received: 8 September 2019 / Accepted: 15 November 2019 / Published online: 3 January 2020
© CERN for the benefit of the CMS collaboration 2019

- In the current LHC analyses, it often serves as the **main variable** in searching for new particles from **missing energy events**.

Pair production, two invisible particles: M_2

Q: Should we use the transverse mass?

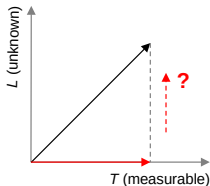
Can we extend it to $(1+3)$ -dim and minimize over three-momenta (k_{aT}, k_{aL}) ?



Pair production, two invisible particles: M_2

Q: Should we use the transverse mass?

Can we extend it to $(1+3)$ -dim and minimize over three-momenta $(\mathbf{k}_{aT}, k_{aL})$?



$$M_2 = \min_{\mathbf{k}_1, \mathbf{k}_2 \in \mathbb{R}^3} \left[\max \left\{ M(p_1, k_1), M(p_2, k_2) \right\} \right]$$

subject to $\mathbf{k}_{1T} + \mathbf{k}_{2T} = \mathbf{P}_T^{\text{miss}}$

where $M(p_a, k_a)$ are invariant masses,

$$M(p_a, k_a) = (p_a + k_a)^2 = (E_a + e_a)^2 - (\mathbf{p}_a + \mathbf{k}_a)^2 \quad (a = 1, 2)$$

Barr *et al.*, PRD 2011, Cho *et al.*, JHEP 2014

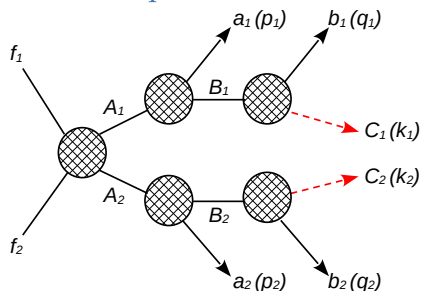
■ We can add **more kinematic constraints** to the definition of M_2

⇒ a family of M_2 variables.

$$M_2 = \min_{\mathbf{k}_1, \mathbf{k}_2 \in \mathbb{R}^3} \left[\max \left\{ M(p_1, k_1), M(p_2, k_2) \right\} \right]$$

subject to $\begin{cases} \mathbf{k}_{1T} + \mathbf{k}_{2T} = \mathbf{P}_T^{\text{miss}}, \\ \text{more constraints} \end{cases}$

Pair production, two invisible particles: M_2



- For two-step symmetric decay chains where

$$M_{A_1} = M_{A_2}, M_{B_1} = M_{B_2}, M_{C_1} = M_{C_2},$$

$$M_2 = \min_{k_1, k_2 \in \mathbb{R}^3} \left[\max \left\{ M(p_1 + q_1, k_1, M_C), M(p_2 + q_2, k_2, M_C) \right\} \right]$$

subject to

$$\begin{cases} k_{1T} + k_{2T} = P_T^{\text{miss}}, \\ (p_1 + q_1 + k_1)^2 = (p_2 + q_2 + k_2)^2, \\ (q_1 + k_1)^2 = (q_2 + k_2)^2. \end{cases}$$

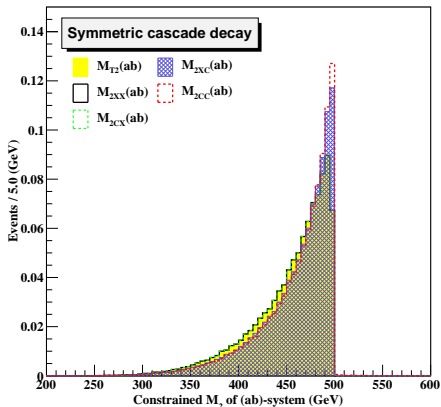
- “Constrained” minimization

Pair production, two invisible particles: M_2

- The distribution of M_2 is bounded by M_Y (\because min). Furthermore,

$$M_{T2} \leq M_2 \leq M_Y$$

- The addition of kinematic constraints generally increases the value of M_2
 \implies the distribution becomes sharper.



Outline

1. The M_{T2} and M_2 variables
2. Searching for a new invisible particle: $\tau \rightarrow \ell + \phi$
3. Search for rare B decays: $B \rightarrow K\tau\mu$
4. Conclusions

$$\tau \rightarrow \ell + \phi$$

- Consider a new invisible particle ϕ in the MeV–GeV range.

- E.g., axion-like particle,

$$\mathcal{L}_{\text{int}} = \frac{\partial_\mu a}{2f_a} \bar{\ell}_i \gamma^\mu (c_V + c_A \gamma^5) \ell_j$$

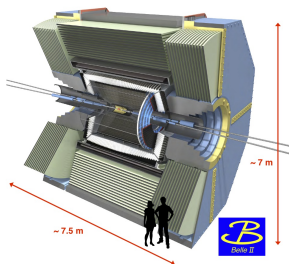
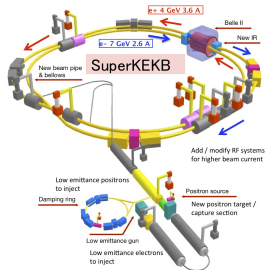
- Such a light invisible particle can be searched for from lepton flavor violating

$$\tau \rightarrow \ell + \phi \quad (\ell = e, \mu).$$

- searches performed at

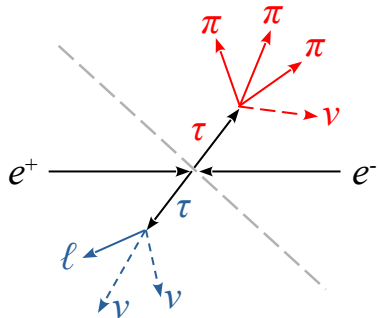
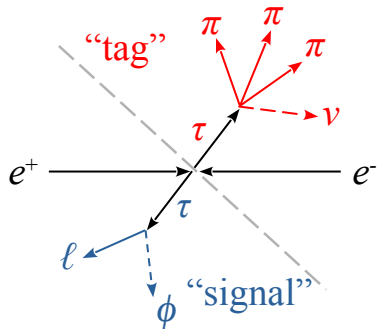
Mark III (SLAC) (1985), ARGUS (DESY) (1995), and Belle II (2212.03634)

by using $e^+e^- \rightarrow \tau^+\tau^-$ data.



- At SuperKEKB, $\sigma(e^+e^- \rightarrow \tau^+\tau^-) = 0.9 \text{ nb} \implies \sim 5 \times 10^{10} \tau$ pairs for $L = 50 \text{ ab}^{-1}$

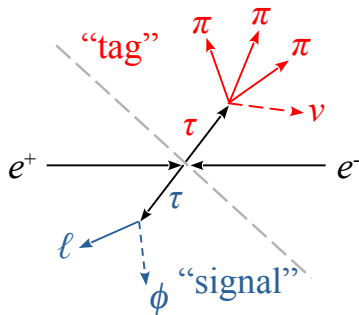
$$\tau \rightarrow \ell + \phi$$



- Signal and background have the identical event topology:

$$\tau^{\text{sig}}(\rightarrow \text{visible} + \text{invisible}) + \tau^{\text{tag}}(\rightarrow \text{visible} + \text{invisible})$$

$$\tau \rightarrow \ell + \phi$$



- If we *could* reconstruct the momentum of τ_{sig} ,

$$|\mathbf{p}_\ell| = \frac{m_\tau^2 - m_\phi^2}{2m_\tau}$$

in the rest frame of τ_{sig} .

- At lepton colliders, \sqrt{s} is fixed (At Belle, $\sqrt{s} = 10.58$ GeV).

In the center-of-mass (CM) frame of e^+e^- collision, $E_\tau \approx \sqrt{s}/2$, and

$$p_\tau = \frac{\sqrt{s}}{2} \left(1, \hat{\mathbf{p}}_\tau \sqrt{1 - \frac{4m_\tau^2}{s}} \right) \quad (\hat{\mathbf{p}}_\tau : \text{the flying direction of } \tau)$$

- $\hat{\mathbf{p}}_\tau \approx ?$ \implies approximate τ -rest frame.

$\tau \rightarrow \ell + \phi$: ARGUS and thrust method

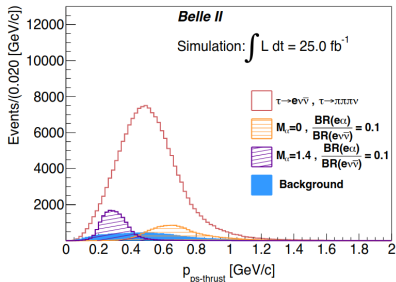
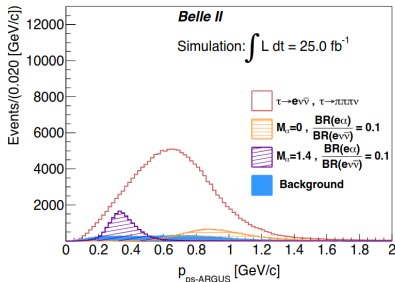
■ **ARGUS** method: $\hat{p}_\tau^{\text{sig}} = -\hat{p}_{3\pi}$ (\cdot : $\hat{p}_\tau^{\text{sig CM}} = -\hat{p}_\tau^{\text{tag}} \approx -\hat{p}_{3\pi}$)

■ **Thrust** method: $\hat{p}_\tau^{\text{sig}} = \hat{n}$, where \hat{n} is the thrust axis of

$$T = \max_{\hat{n}} \frac{\sum_i |\hat{n} \cdot \mathbf{p}_i|}{\sum_i |\mathbf{p}_i|}$$

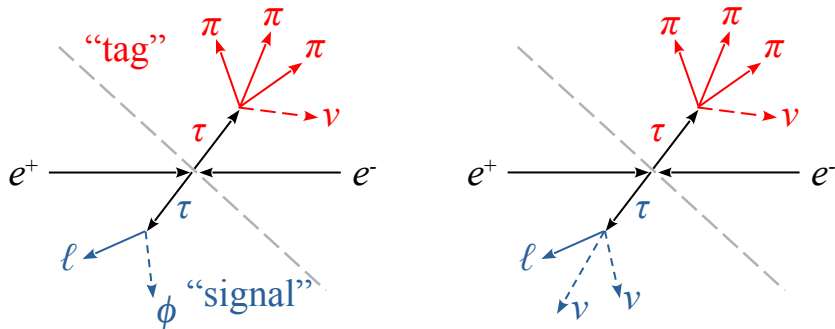
($T \rightarrow 1$ for back-to-back and $T \rightarrow 0.5$ for spherically symmetric events)

► The thrust axis \hat{n} is used to define the *hemisphere* of each tau decay products.



from Tenchini *et al.* (Belle II), ICHEP 2020

$$\tau \rightarrow \ell + \phi$$



- Signal has **two** invisibles: ϕ and ν , while background has **three** invisibles: 3 ν 's. We should solve the problem of

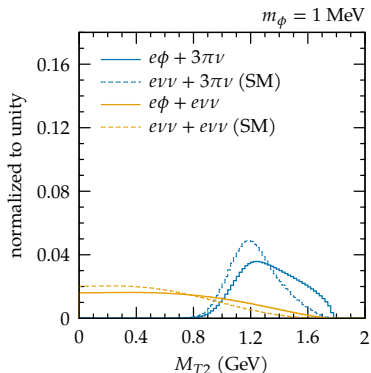
2 vs 3

- ▶ Kinematic features sensitive to the number of invisibles?

$$\tau \rightarrow \ell + \phi: M_{T2}$$

- The shape of the M_{T2} distribution depends on the number of invisibles!

(Agashe, Kim, Walker, Zhu, PRD 2011, Giudice, Gripaos, Mahbubani, PRD 2012)

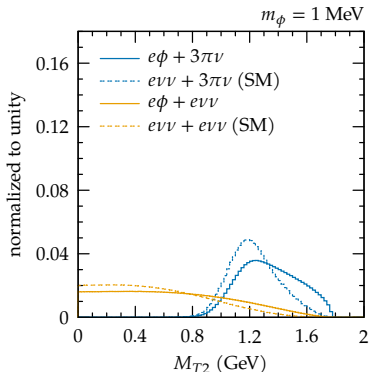


- The *smaller* the number of invisibles, the *more* the M_{T2} distribution is populated *towards the upper edge*.

$$\tau \rightarrow \ell + \phi: M_{T2}$$

- The shape of the M_{T2} distribution depends on the number of invisibles!

(Agashe, Kim, Walker, Zhu, PRD 2011, Giudice, Gripanos, Mahbubani, PRD 2012)



- ▶ The *smaller* the number of invisibles, the *more* the M_{T2} distribution is populated *towards the upper edge*.

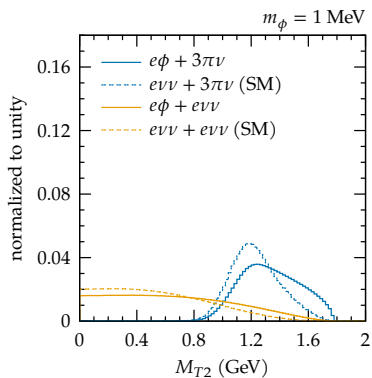
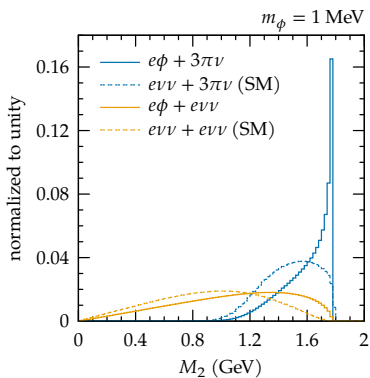
- How about M_2 ? — How to define M_2 for $e^+e^- \rightarrow \tau\tau \rightarrow \ell\phi + 3\pi\nu$?

$\tau \rightarrow \ell + \phi: M_2$

■ M_2 for lepton collider (where \sqrt{s} is fixed):

$$M_2 = \min_{k_1, k_2 \in \mathbb{R}^3} \left[\max \left\{ M(p_1, k_1), M(p_2, k_2) \right\} \right]$$

subject to $\begin{cases} k_1 + k_2 = p^{\text{miss}}, \\ (p_1 + p_2 + k_1 + k_2)^2 = s. \end{cases}$



■ M_2 is an “invisible-savvy” variable.

$\tau \rightarrow \ell + \phi$: MAOS method

$$M_2 = \min_{\mathbf{k}_1, \mathbf{k}_2 \in \mathbb{R}^3} \left[\max \left\{ M(p_1, k_1), M(p_2, k_2) \right\} \right]$$

subject to $\begin{cases} \mathbf{k}_1 + \mathbf{k}_2 = \mathbf{p}^{\text{miss}}, \\ (p_1 + p_2 + k_1 + k_2)^2 = s. \end{cases}$

- The solution to the minimization can be used to an **estimate of the invisible momenta k_1, k_2** ,

$$k_a^{\text{maos}} \approx k_a^{\text{true}}$$

$\implies M_2$ -assisted on-shell (MAOS) invisible momentum

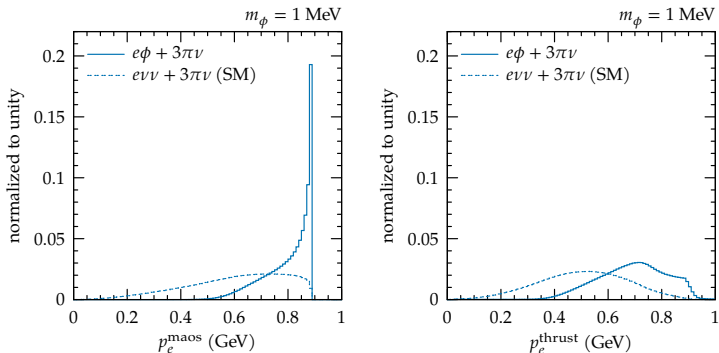
(Cho, Choi, Kim, CBP, PRD 2009, Kim, Matchev, Moortgat, Pape, JHEP 2017)

$\tau \rightarrow \ell + \phi$: MAOS method

- With the MAOS momenta we can reconstruct $|\mathbf{p}_\ell|$ in the rest frame of τ_{sig} .

$$|\mathbf{p}_\ell| = \frac{m_\tau^2 - m_\phi^2}{2m_\tau}$$

for the signal events.



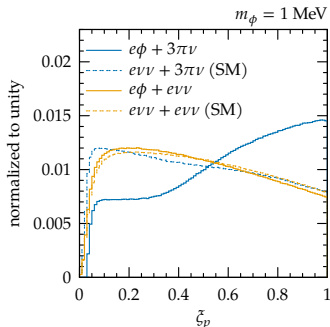
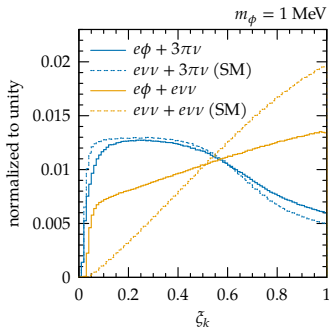
- ▶ The MAOS method performs much better than the thrust method.
- ▶ $|\mathbf{p}_\ell|$ is not invisible-savvy as it doesn't solve the problem of 2 vs 3.

$\tau \rightarrow \ell + \phi$: Invisible-savvy variables

- Using $k_{1,2}^{\text{maos}}$, we can construct the ratio

$$\zeta_k = \frac{\min\{|k_1|, |k_2|\}}{\max\{|k_1|, |k_2|\}} \in [0, 1]$$

- The distribution of ζ_k is populated around 1 for symmetric decay chains:
this is the case for the $\ell\nu\nu + \ell\nu\nu$ background.
- We can also construct ζ_p of visible particle momenta.



- Earlier literature proposed “max / min” to distinguish 2 and 3

$\tau \rightarrow \ell + \phi$: Invisible-savvy variables

■ We also include variables that do not require MAOS momenta.

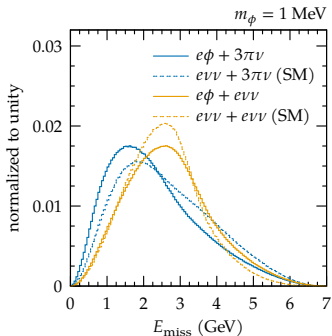
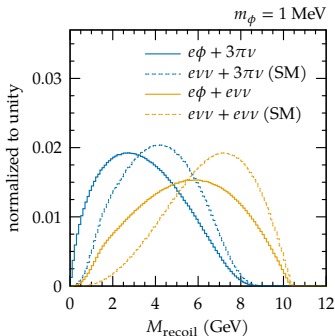
▶ $M_{\text{recoil}}^2 = (p^{\text{CMS}} - p_1 - p_2)^2$: invariant mass of the full invisible system

$$(p^{\text{CMS}} = p_1 + p_2 + k_1 + k_2).$$

▶ Backgrounds have more invisibles than the signal $\Rightarrow M_{\text{recoil}}(\text{bkg}) > M_{\text{recoil}}(\text{sig})$

▶ $E_{\text{miss}} = |\mathbf{p}^{\text{miss}}| = |\mathbf{k}_1 + \mathbf{k}_2| = |\mathbf{p}^{\text{CMS}} - \mathbf{p}_1 - \mathbf{p}_2|$

▶ the more symmetric the two decay chains (as in $\ell\nu\nu + \ell\nu\nu$), the more the invisible momenta tends to cancel



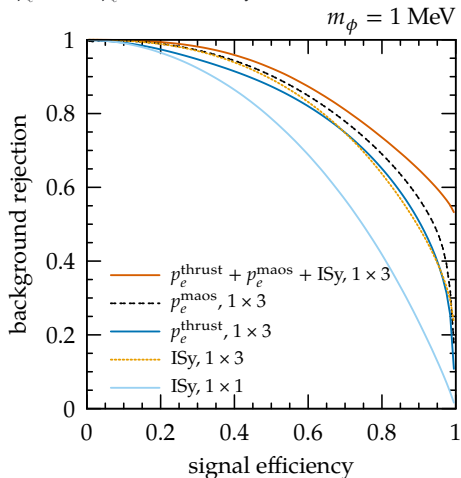
$$\tau \rightarrow \ell + \phi$$

- We collectively denote the kinematic variables sensitive to the number of invisibles

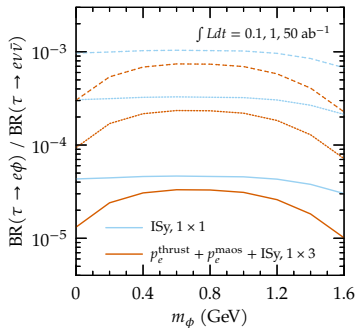
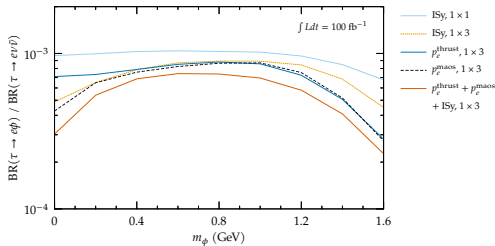
$$M_2, \zeta_k, \zeta_p, M_{\text{recoil}}, E_{\text{miss}}$$

as “Invisible-Savvy” or ‘ISy’ classifiers.

- We also include p_ℓ^{maos} and p_ℓ^{thrust} in our analysis.



$$\tau \rightarrow \ell + \phi$$



■ With 3 benchmark Belle II luminosities we get

$$\text{BR}(\tau \rightarrow e\phi) \leq$$

$$5.4 \times 10^{-5} \quad (L = 0.1 \text{ ab}^{-1})$$

$$1.7 \times 10^{-5} \quad (L = 1 \text{ ab}^{-1})$$

$$2.4 \times 10^{-6} \quad (L = 50 \text{ ab}^{-1})$$

for $m_\phi = 1 \text{ MeV}$.

► improvement by a factor of 3 than p_ℓ^{thrust} .

Outline

1. The M_{T2} and M_2 variables
2. Searching for a new invisible particle: $\tau \rightarrow \ell + \phi$
3. Search for rare B decays: $B \rightarrow K\tau\mu$
4. Conclusions

$B \rightarrow K\tau\mu$

- “**B anomalies**” suggest new physics dominantly coupled to the third generation of down-type fermions (Glashow, Guadagnoli, Lane, PRL 2015).

$$\mathcal{H}_{\text{NP}} = \frac{1}{\Lambda_{\text{NP}}} \bar{b}_L \gamma^\lambda b_L \bar{\tau}_L \gamma_\lambda \tau_L.$$

- Flavor mixing \implies dominant effects in $b \rightarrow s$ transitions and in final states with τ including lepton-flavor violating ones.
- These observations were made properly $SU(2)_L$ -compliant
(Bhattacharya, Datta, London, Shivashankara, PLB 2015),
thus paving the way for joint explanations of $b \rightarrow s$ and $b \rightarrow c$ data
(See also Greljo, Isidori, Marzocca, JHEP 2015).
- Another avenue is a minimally broken $U(2)^5$ global symmetry
(Barbieri *et al.*, EPJC 2011, JHEP 2012).
- One of the most dramatic signatures of new physics explaining the B anomalies is

$$B^\pm \rightarrow K^\pm \tau \mu$$

which can be searched at Belle and Belle II.

$B \rightarrow K\tau\mu$

■ At Belle, B mesons are produced in a pair, $e^+e^- \rightarrow Y(4S) \rightarrow B^+B^-$, and

signal-side : $B_{\text{sig}}^+ \rightarrow K_{\text{sig}}^+ \tau \ell_{\text{sig}}$

tag-side : $B_{\text{tag}}^- \rightarrow D^0 (\rightarrow K_{\text{tag}}^- \pi^+) \pi^-$

► τ decays into the final states including invisible neutrino(s): e.g., $\tau \rightarrow \pi\nu/\ell\nu\nu$.

$B \rightarrow K\tau\mu$

■ At Belle, B mesons are produced in a pair, $e^+e^- \rightarrow Y(4S) \rightarrow B^+B^-$, and

$$\text{signal-side : } B_{\text{sig}}^+ \rightarrow K_{\text{sig}}^+ \tau \ell_{\text{sig}}$$

$$\text{tag-side : } B_{\text{tag}}^- \rightarrow D^0 (\rightarrow K_{\text{tag}}^- \pi^+) \pi^-$$

► τ decays into the final states including invisible neutrino(s): e.g., $\tau \rightarrow \pi\nu/\ell\nu\nu$.

► The search reduces to a “bump hunt” by employing M_{recoil} for τ :

$$\begin{aligned} p_{e^+e^-} &= p_{B_{\text{sig}}} + p_{B_{\text{tag}}} = (p_{K_{\text{sig}}\ell_{\text{sig}}} + p_{\tau}) + p_{B_{\text{tag}}} \\ \implies M_{\text{recoil}}^2 &= p_{\tau}^2 = (p_{e^+e^-} - p_{K_{\text{sig}}\ell_{\text{sig}}} - p_{B_{\text{tag}}})^2 \\ &= \boxed{m_{B_{\text{tag}}}^2 + m_{K_{\text{sig}}\ell_{\text{sig}}}^2 - 2 \left(E_{B_{\text{tag}}} E_{K_{\text{sig}}\ell_{\text{sig}}} + |p_{B_{\text{tag}}}| |p_{K_{\text{sig}}\ell_{\text{sig}}}| \cos\theta \right)} \\ &\qquad \qquad \qquad \cos\theta = \hat{p}_{B_{\text{tag}}} \cdot \hat{p}_{K_{\text{sig}}\ell_{\text{sig}}} \end{aligned}$$

► All quantities are in the CM frame. $\therefore E_{B_{\text{sig}}} = E_{B_{\text{tag}}} = \sqrt{s}/2$ and $p_{B_{\text{sig}}} = -p_{B_{\text{tag}}}$.

► “Hadronic” tag: $p_{B_{\text{tag}}}$ can be fully reconstructed.

\implies we can get event-by-event $\cos\theta$ value. ☺

$B \rightarrow K\tau\mu$

- At Belle, B mesons are produced in a pair, $e^+e^- \rightarrow Y(4S) \rightarrow B^+B^-$, and

$$\text{signal-side : } B_{\text{sig}}^+ \rightarrow K_{\text{sig}}^+ \tau \ell_{\text{sig}}$$

$$\text{tag-side : } B_{\text{tag}}^- \rightarrow D^0 (\rightarrow K_{\text{tag}}^- \pi^+) \pi^-$$

- τ decays into the final states including invisible neutrino(s): e.g., $\tau \rightarrow \pi\nu/\ell\nu\nu$.
- The search reduces to a “bump hunt” by employing M_{recoil} for τ :

$$\begin{aligned} p_{e^+e^-} &= p_{B_{\text{sig}}} + p_{B_{\text{tag}}} = (p_{K_{\text{sig}} \ell_{\text{sig}}} + p_{\tau}) + p_{B_{\text{tag}}} \\ \Rightarrow M_{\text{recoil}}^2 &= p_{\tau}^2 = (p_{e^+e^-} - p_{K_{\text{sig}} \ell_{\text{sig}}} - p_{B_{\text{tag}}})^2 \\ &= \boxed{m_{B_{\text{tag}}}^2 + m_{K_{\text{sig}} \ell_{\text{sig}}}^2 - 2 \left(E_{B_{\text{tag}}} E_{K_{\text{sig}} \ell_{\text{sig}}} + |p_{B_{\text{tag}}}| |p_{K_{\text{sig}} \ell_{\text{sig}}}| \cos \theta \right)} \\ &\qquad \qquad \qquad \cos \theta = \hat{p}_{B_{\text{tag}}} \cdot \hat{p}_{K_{\text{sig}} \ell_{\text{sig}}} \end{aligned}$$

- All quantities are in the CM frame. $\therefore E_{B_{\text{sig}}} = E_{B_{\text{tag}}} = \sqrt{s}/2$ and $p_{B_{\text{sig}}} = -p_{B_{\text{tag}}}$.
- “Hadronic” tag: $p_{B_{\text{tag}}}$ can be fully reconstructed.
 \Rightarrow we can get event-by-event $\cos \theta$ value. ☺
- “Semi-leptonic” (SL) tag: $p_{B_{\text{tag}}}$ CANNOT be reconstructed due to invisible neutrino.

$$\text{tag-side : } B_{\text{tag}}^- \rightarrow D^0 (\rightarrow K_{\text{tag}}^- \pi^+) \ell^- \bar{\nu}$$

How can we get the $\cos \theta$ value in the SL tag?

$$B \rightarrow K\tau\mu$$

$$\blacksquare \cos\theta \longleftarrow \mathbf{p}_{B_{\text{tag}}} = \mathbf{p}_2 + \mathbf{k}_2 \longleftarrow \mathbf{k}_2$$

$$B_{\text{sig}}B_{\text{tag}} \rightarrow V_1(p_1)\chi_1(k_1) + V_2(p_2)\chi_2(k_2)$$

- ▶ V_i are visible, χ_i are invisible (sets of) particles.

$B \rightarrow K\tau\mu$

■ $\cos \theta \leftarrow p_{B_{\text{tag}}} = p_2 + k_2 \leftarrow k_2$

$$B_{\text{sig}} B_{\text{tag}} \rightarrow V_1(p_1)\chi_1(k_1) + V_2(p_2)\chi_2(k_2)$$

▶ V_i are visible, χ_i are invisible (sets of) particles.

■ We can construct M_2 ,

$$M_2 = \min_{k_1, k_2} \left[\max \left\{ M_{(1)}, M_{(2)} \right\} \right] \quad (M_{(i)}^2 = (p_i + k_i)^2)$$

subject to constraints,

- ▶ and use the MAOS momenta $k_{1,2}^{\text{maos}}$ as the estimator of $k_{1,2}$.
- ▶ Which constraints for M_2 ?

$B \rightarrow K\tau\mu$

■ $\cos\theta \leftarrow p_{B_{\text{tag}}} = p_2 + k_2 \leftarrow k_2$

$$B_{\text{sig}}B_{\text{tag}} \rightarrow V_1(p_1)\chi_1(k_1) + V_2(p_2)\chi_2(k_2)$$

► V_i are visible, χ_i are invisible (sets of) particles.

■ We can construct M_2 ,

$$M_2 = \min_{k_1, k_2} \left[\max \left\{ M_{(1)}, M_{(2)} \right\} \right] \quad (M_{(i)}^2 = (p_i + k_i)^2)$$

subject to constraints,

► and use the MAOS momenta $k_{1,2}^{\text{maos}}$ as the estimator of $k_{1,2}$.

► Which constraints for M_2 ?

■ At lepton colliders (such as Belle),

$$k_1 + k_2 = \mathbf{P}^{\text{miss}}, \quad (p_1 + p_2 + k_1 + k_2)^2 = s.$$

$$\boxed{\begin{aligned} M_{2s} &= \min_{k_1, k_2} \left[\max \left\{ M_{(1)}, M_{(2)} \right\} \right] \\ &\text{subject to } \begin{cases} k_1 + k_2 = \mathbf{P}^{\text{miss}}, \\ (p_1 + p_2 + k_1 + k_2)^2 = s. \end{cases} \end{aligned}}$$

$B \rightarrow K\tau\mu: M_{2sB}$

- Furthermore, because we know m_B ,

$$(p_1 + k_1)^2 = (p_2 + k_2)^2 = m_B^2,$$

$$M_{2sB} = \min_{k_1, k_2} \left[\max \left\{ M_{(1)}, M_{(2)} \right\} \right]$$

subject to $\begin{cases} k_1 + k_2 = P^{\text{miss}}, \\ (p_1 + p_2 + k_1 + k_2)^2 = s, \\ (p_1 + k_1)^2 = (p_2 + k_2)^2 = m_B^2. \end{cases}$

- The constraints reduce to *zero* the number of d.o.f.

$$\boxed{4 + 4 = 8} \text{ unknowns}$$

$$\xrightarrow{\text{choose } M_{X_i}} 6 \xrightarrow{k_1 + k_2 = P^{\text{miss}}} 3 \xrightarrow{(p_1 + p_2 + k_1 + k_2)^2 = s} 2 \xrightarrow{(p_1 + k_1)^2 = (p_2 + k_2)^2 = m_B^2} \boxed{0}$$

- M_{2sB} is not a distribution — its minimum is a solver of the constraint equations.

$B \rightarrow K\tau\mu: M_{2sV}$

- At present and upcoming high-intensity colliders, accurate vertex information is available. \implies constraints on the flight direction of parent B ,

$$\hat{v}_{\text{sig}} = \frac{\mathbf{r}_{\text{sig}} - \mathbf{r}_0}{|\mathbf{r}_{\text{sig}} - \mathbf{r}_0|}$$

- ▶ \mathbf{r}_0 : the location of the primary vertex (interaction point),
 \mathbf{r}_{sig} : the location of the B_{sig} -decay vertex

$B \rightarrow K\tau\mu: M_{2sV}$

- At present and upcoming high-intensity colliders, accurate vertex information is available. \implies constraints on the flight direction of parent B ,

$$\hat{v}_{\text{sig}} = \frac{\mathbf{r}_{\text{sig}} - \mathbf{r}_0}{|\mathbf{r}_{\text{sig}} - \mathbf{r}_0|}$$

- \mathbf{r}_0 : the location of the primary vertex (interaction point),
 \mathbf{r}_{sig} : the location of the B_{sig} -decay vertex

- The constraint could be implemented as

$$\arccos\left(\hat{\mathbf{p}}_{B_{\text{sig}}} \cdot \hat{\mathbf{v}}_{\text{sig}}\right) \leq \delta_{\text{sig}} \quad (\mathbf{p}_{B_{\text{sig}}} = \mathbf{p}_1 + \mathbf{k}_1)$$

- δ_{sig} parametrizes the experimental uncertainties of \mathbf{r}_0 and \mathbf{r}_{sig} .
- Constraint on \hat{v}_{tag} is redundant since $\mathbf{p}_{B_{\text{tag}}} = -\mathbf{p}_{B_{\text{sig}}}$ in the CM frame.

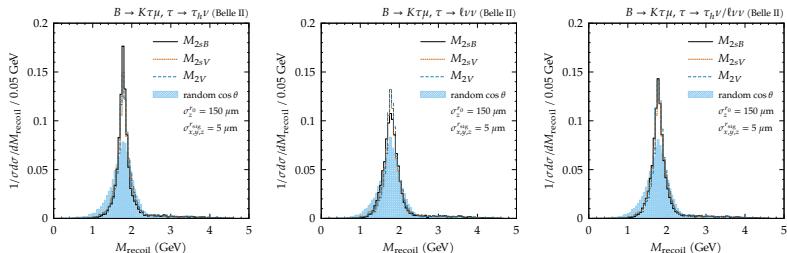
$$M_{2sV} = \min_{k_1, k_2} \left[\max \left\{ M_{(1)}, M_{(2)} \right\} \right]$$

subject to

$$\begin{cases} \mathbf{k}_1 + \mathbf{k}_2 = \mathbf{p}^{\text{miss}}, \\ (p_1 + p_2 + k_1 + k_2)^2 = s, \\ \arccos\left(\hat{\mathbf{p}}_{B_{\text{sig}}} \cdot \hat{\mathbf{v}}_{\text{sig}}\right) \leq \delta_{\text{sig}}. \end{cases}$$

- We can omit the “ s ” constraint if it’s unavailable (such as in LHCb) $\implies M_{2V}$.
- For simplicity, we replace the true \hat{v}_{sig} with a vector estimated by smearing \mathbf{r}_0 and \mathbf{r}_{sig} and take $\delta_{\text{sig}} \rightarrow 0$ (inequality \rightarrow equality constraint).

$B \rightarrow K\tau\mu$



- At Belle and Belle II, the beam has a non-negligible size mostly in the z axis:
 At Belle, $\sigma_z^{\text{IP}} \sim 4 \text{ mm} \implies \hat{v}_{\text{sig}}$ constraint is ineffectual.
 At Belle II, $\sigma_z^{\text{IP}} \simeq 350 \text{ }\mu\text{m}$ (to further improve to $150 \text{ }\mu\text{m}$).

► M_{2sV} would be useful when the precise vertex information is available.

- With some simplifications, we get a 90% CL upper bound:

$$\mathcal{B}(B^{\pm} \rightarrow K^{\pm}\tau^{\pm}\mu^{\mp}) \leq 1.2 \times 10^{-5}$$

using M_{2sB} alone at Belle II ($L = 710 \text{ fb}^{-1}$).

► Cf. If we use the *true* momenta of invisible particles, $\mathcal{B}(B^{\pm} \rightarrow K^{\pm}\tau^{\pm}\mu^{\mp}) \leq 0.6 \times 10^{-5}$.

Outline

1. The M_{T2} and M_2 variables
2. Searching for a new invisible particle: $\tau \rightarrow \ell + \phi$
3. Search for rare B decays: $B \rightarrow K\tau\mu$
4. Conclusions

Conclusions

- The M_{T2} and its generalizations M_2 were conceived from high- p_T events such as the pair productions of heavy particles.

- ▶ We port these ideas to low-energy processes at high-intensity colliders.

- We devise a novel search strategy that we apply to pair productions of τ and B mesons,

$$\tau \rightarrow \ell\phi \quad (\phi : \text{light invisible particle, } m_\phi \text{ in MeV-GeV})$$

$$B \rightarrow K\tau\mu \quad (\text{rare } B \text{ decay})$$

at Belle II.

- Our strategy has a vast domain of applicability: $B \rightarrow K\nu\nu$, $B \rightarrow \tau\mu$, etc. at Belle II and LHCb.

Thank you for your attention!

Backup

- In the leptonic decays of τ , we have two neutrinos (*cf.* $\tau \rightarrow \pi\nu$),

$$B \rightarrow K\tau\mu \rightarrow K\ell\mu + \nu\bar{\nu}$$

- ▶ A simple ansatz is to take $\underline{m_{\nu\bar{\nu}}} = 0$.

- We can get an approximate $m_{\nu\bar{\nu}}$ value, assuming the back-to-back momentum of B - \bar{B} pair is negligible ($m_B = 5.279$ GeV $\sqrt{s} = 10.58$ GeV at Belle II).

1. B is assumed to be at rest, $p_B = (m_B, \mathbf{0})$.
2. Boost the B momentum to the LAB frame ($p_{e^-} = 7$ GeV, $p_{e^+} = 4$ GeV at Belle II).
3. Then, $m_{\nu\bar{\nu}}^2 = (p_B - p_{K\ell\mu})^2$.

